

$$r_s = \int_0^{t_d} c_s dt / a = \int_0^{a_d} c_s \frac{da}{a^2 H(a)}$$