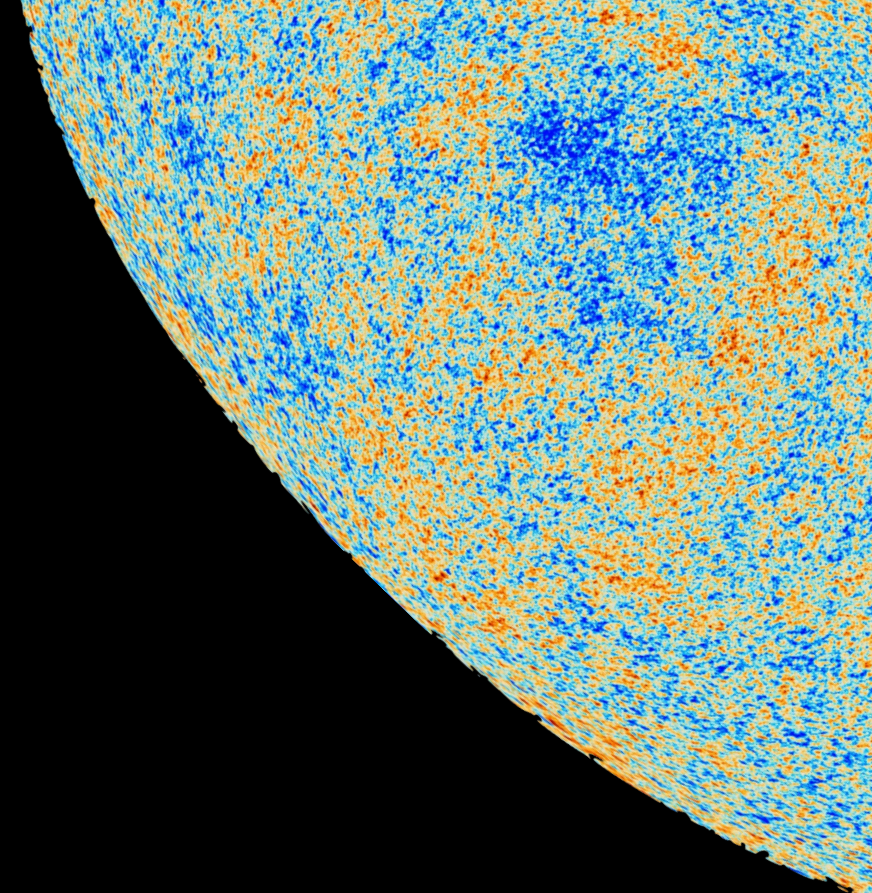
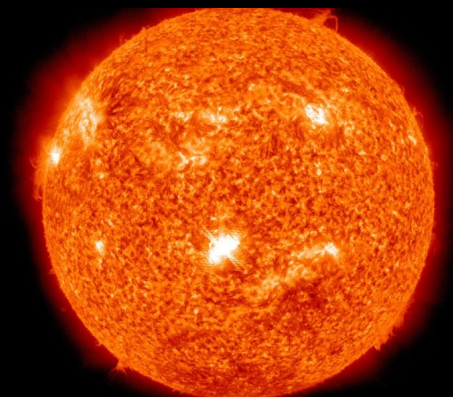


astrophysical
and
cosmological
probes of axions

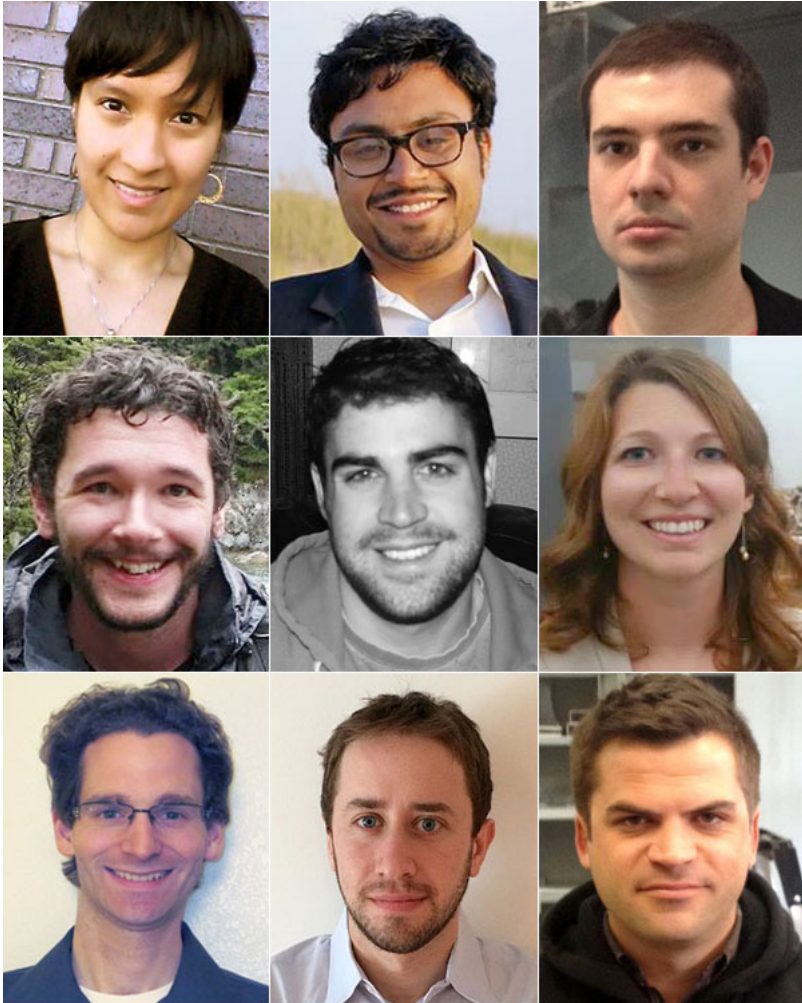


Andrew Long
Rice University

*KICP Birthday Bash
June 6, 2024*

the dream team

KICP Fellows circa 2015



fond memories

- KICP Jamboree + PD symposium
- Thunch ... journal club
- KICP seminar run by fellows
- lunch with colloquium speakers
- the stitch + coffee
- support for workshops
- outreach: life-long learning
- interdisciplinary: particle physics + cosmology + astrophysics

A triumph of science!

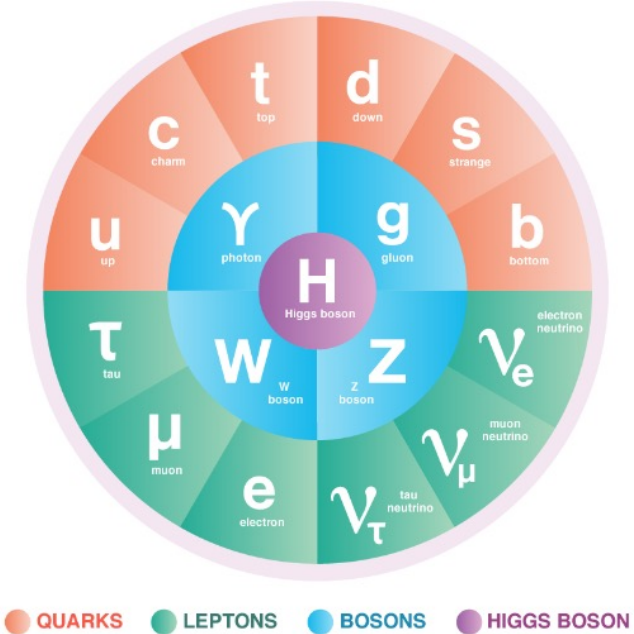
Successes known physics

describes the properties of the known **elementary particles** and the **forces** by which they interact

allows for **precision** calculation

a **predictive** framework

Standard Model of the Elementary Particles



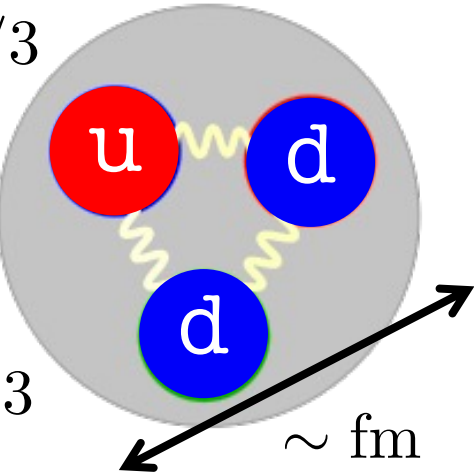
Puzzles hints of *new* physics

- Why is the **Higgs** light?
- Why don't couplings **unify**?
- Why are **neutrinos** massive?
- Why **three generations**?
- Why is there **dark matter**?
- Why is there **dark energy**?
- Why less **antimatter**?
- Why **homogenous & isotropic**?
- Why no **strong CP** violation?

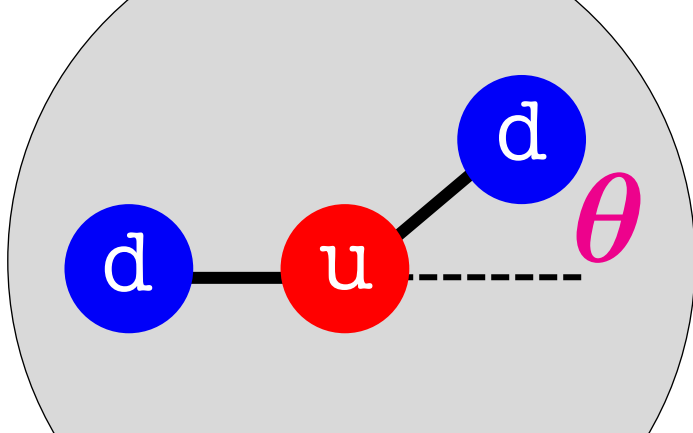
A puzzle with the neutron's electric dipole moment

$q_u = +2e/3$

$q_d = -e/3$



consider this configuration:



$d_n \rightarrow 0$ as $\theta \rightarrow 0$

naïve dimensional analysis

$d_n \sim e \times \text{fm} \sim 10^{-13} e \text{ cm}$

experiment

$d_n < 10^{-26} e \text{ cm}$

the strong nuclear force exhibits a symmetry (CP)

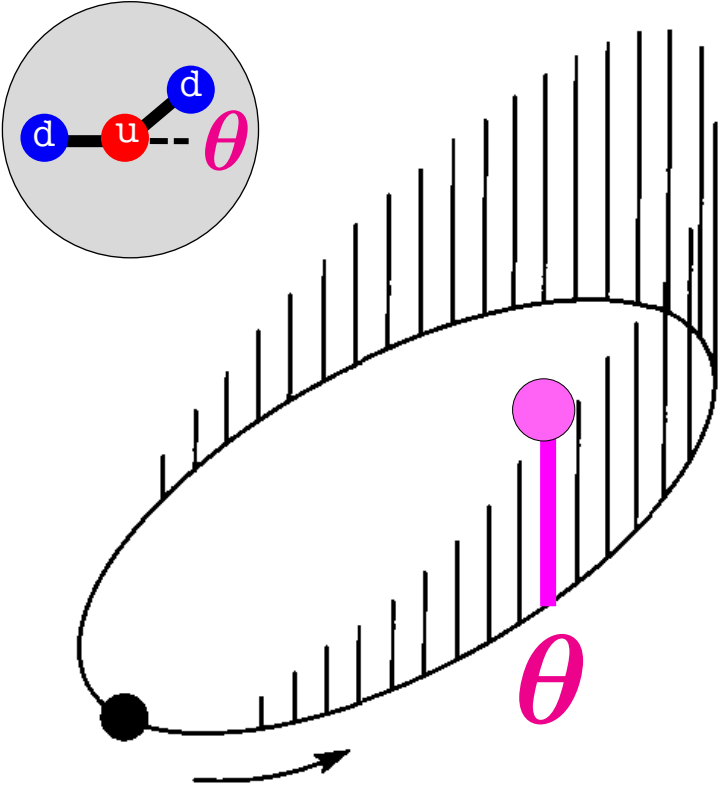
Why does the strong nuclear force exhibit CP symmetry?
this is called the *Strong CP Problem*

* more precisely: why is $\bar{\Theta} = \Theta + \text{Arg det } M_q \ll 1$ fine-tuned?

Dynamical relaxation to zero

[Peccei, Quinn, Weinberg, Wilczek 1977-78]

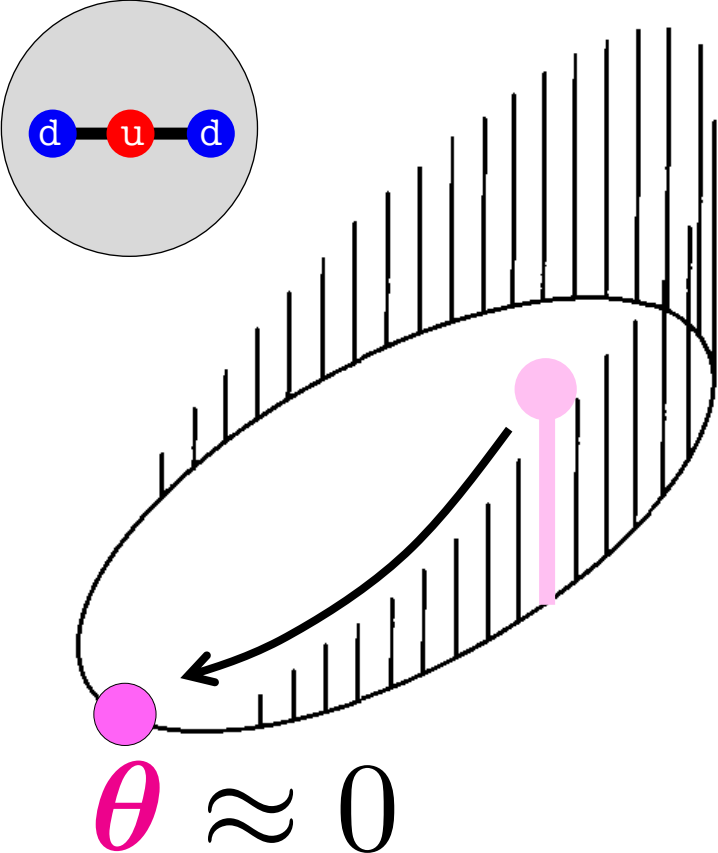
It turns out that θ costs energy:



promote θ to a field



A dynamical θ relaxes to zero:



By-product: a new particle

Quantum excitations around $\theta=0$
are a new kind of particle



Axion Fact Sheet

- SPIN = 0
- CHARGE = 0
- COLOR = 0

~~~~~

(model-dep)

- MASS = ultralight ( $\mu\text{eV}$ )
- INTERACTIONS = feeble
- LIFETIME = cosmological

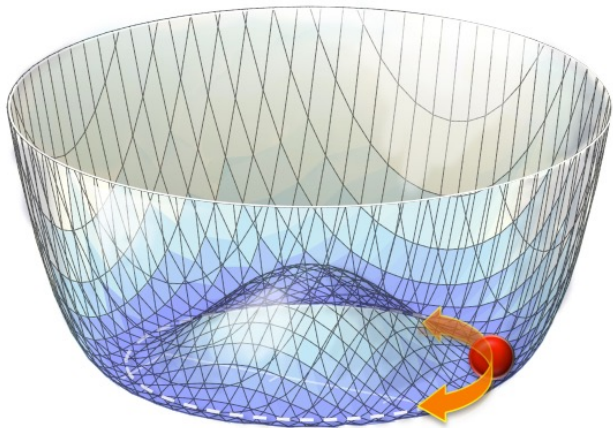


# The QCD Axion's cousins: axion-like particles

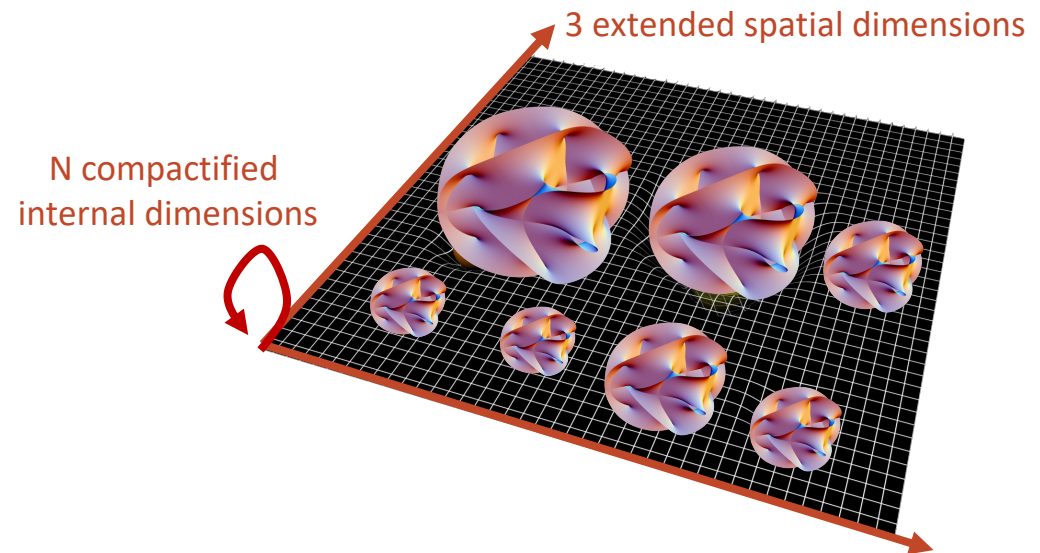
[axions in string theory: Svrcek & Witten (2006), Arvanitaki et al (2009)]

Whereas the **QCD Axion** plays a special role of solving the Strong CP Problem, **axion-like particles (ALPs)** are generic in theories Beyond the Standard Model.

ALPs from symmetry breaking  
(similar to pions in QCD)



ALPs from extra dimensions  
(such as string theory)



Does the QCD axion or an ALP exist in nature?

What is its mass scale?

How does it interact with the SM?

Is it stable, or otherwise, what is its lifetime?

How is it produced in the Universe today?

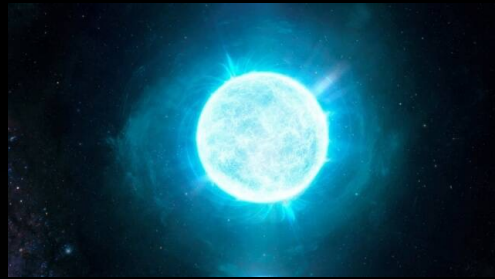
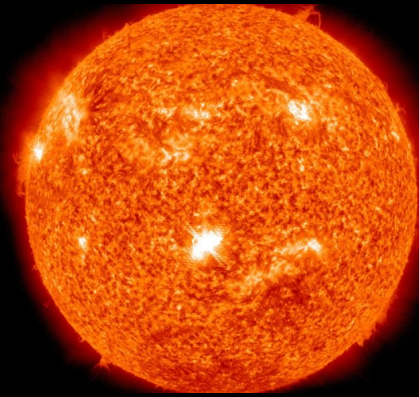
How was it produced in the early Universe?

Is it connected to dark matter, baryogenesis, inflation, etc?

...

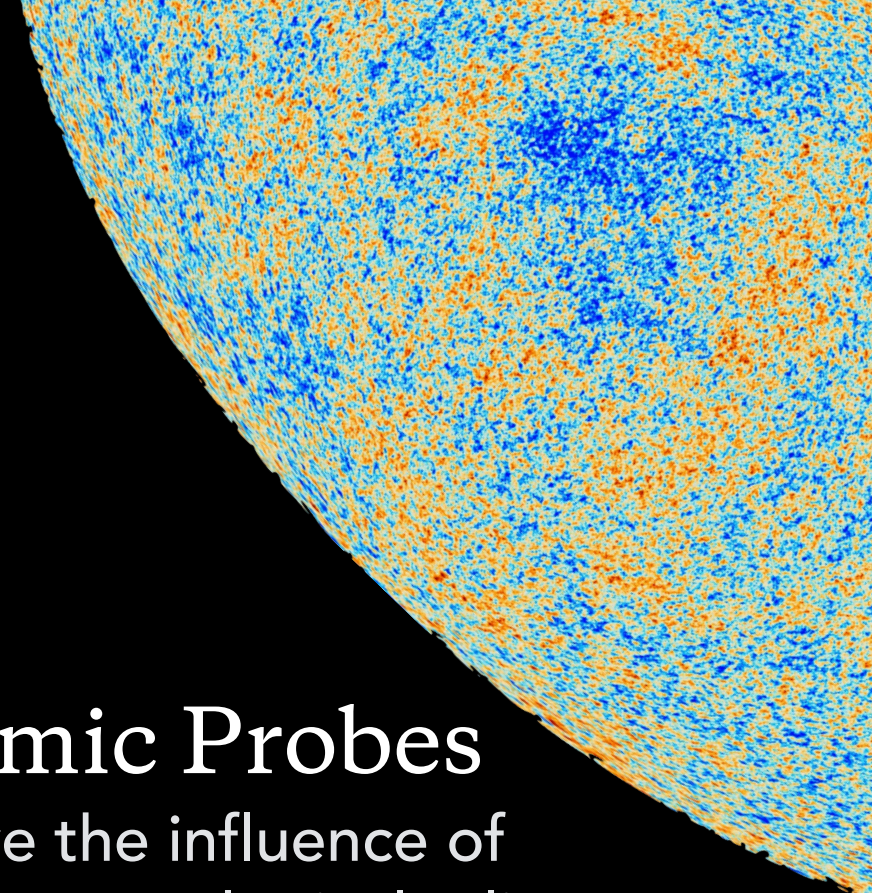
# Astrophysical Probes

observe the influence of axions on stars, gas, & compact objects



# Cosmic Probes

observe the influence of axions on cosmological relics



# Terrestrial Probes

create axions on Earth or detect axions as they pass by the Earth

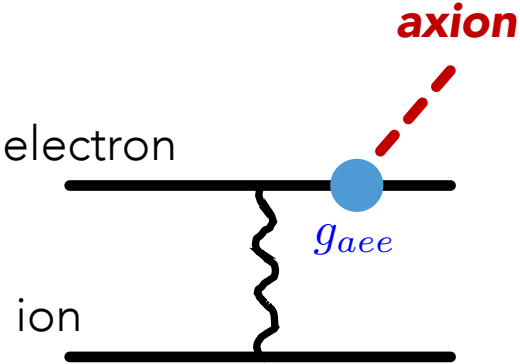




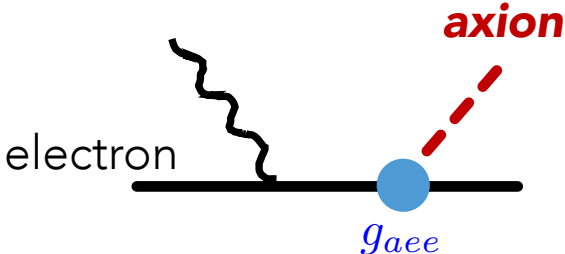
# Stars emit axions

Various channels for axion emission  
(different channels dominate for different star types)

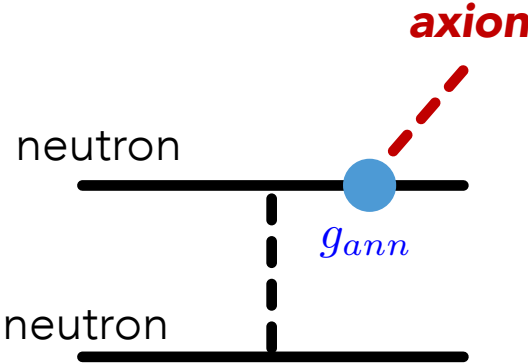
electron  
bremstrahlung  
(white dwarf)



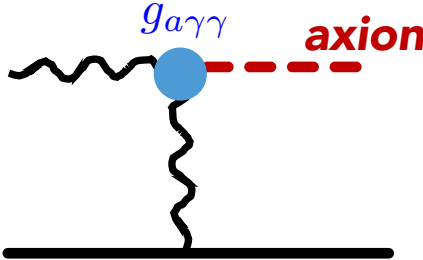
Compton  
(main sequence, giants)



neutron  
bremstrahlung  
(neutron star)



Primakoff effect  
(main sequence, giants)



What kinds of stars emit axions?

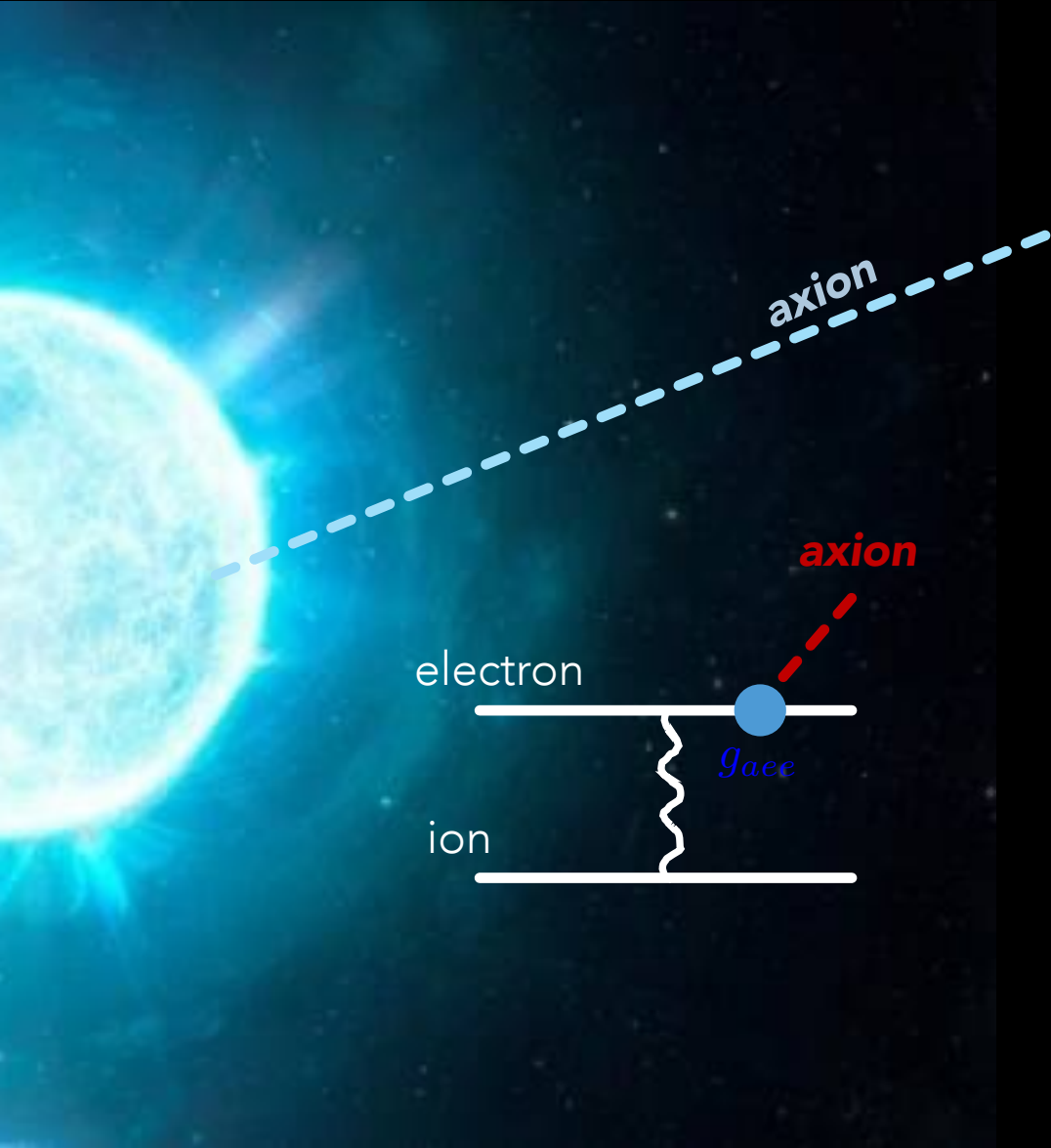
let's look at some examples

# Example: white dwarf stars

[Krauss, Moody, & Wilczek (1984)] [Raffelt (1986)]  
 [Nakagawa, Adachi, Kohyama, & Itoh (1987,88)]

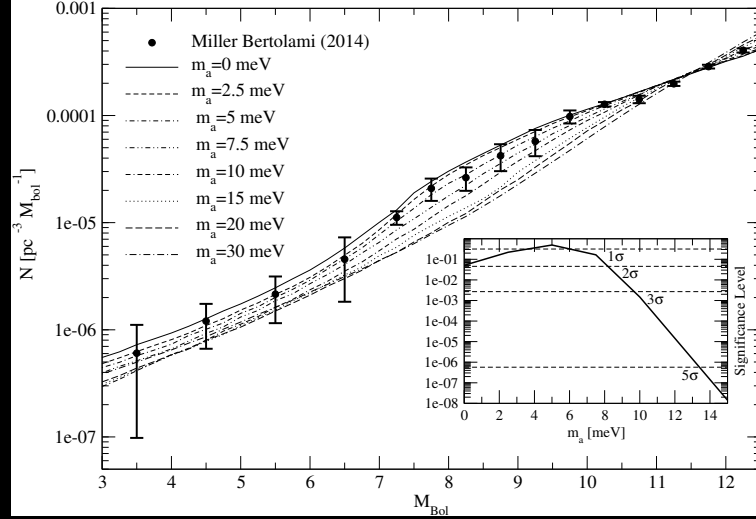
axion luminosity (for white dwarf stars)

$$L_a \simeq (1.6 \times 10^{-4} L_\odot) \left( \frac{g_{aee}}{10^{-13}} \right)^2 \left( \frac{M_{WD}}{1 M_\odot} \right) \left( \frac{T_c}{10^7 \text{ K}} \right)^4$$



## constraints

[Miller Bertolami et. al. (2014)]



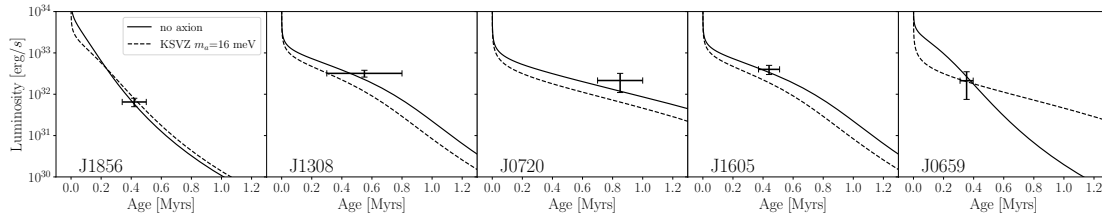
$$g_{aee} < 3 \times 10^{-13} \quad (3\sigma)$$



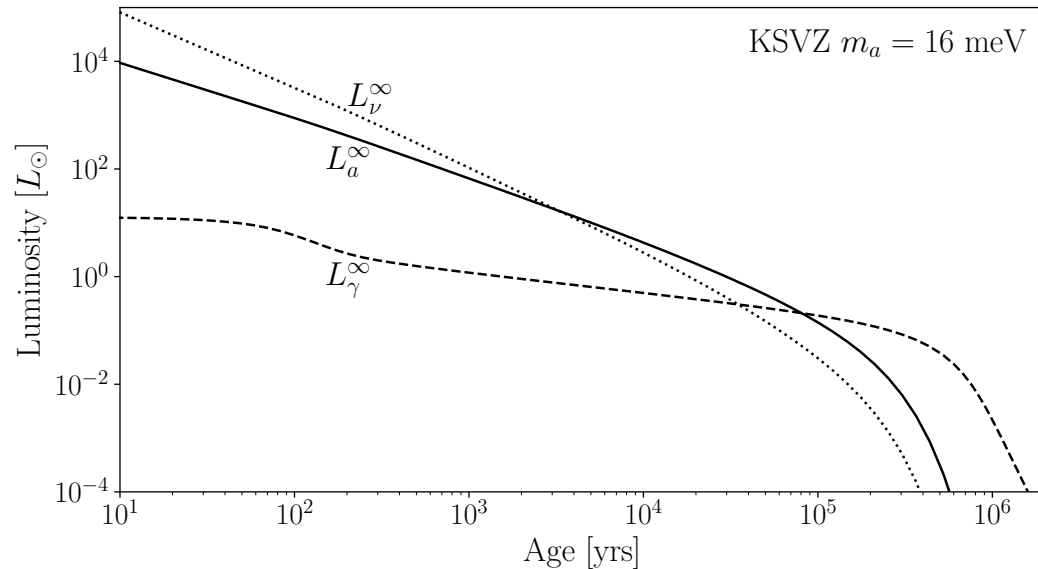
# Example: neutron stars

[Buschmann, Dessert, Foster, AL, & Safdi (2021)]

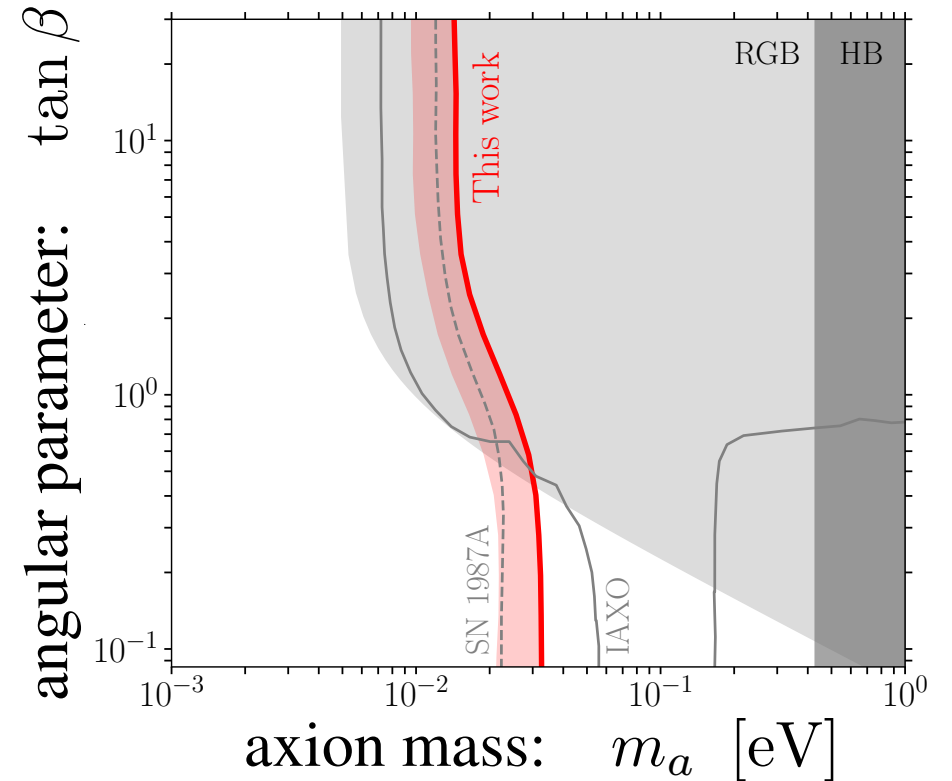
(a few of) The Magnificent 7  
robust luminosity & age measurements



Comparison of emission channels



QCD Axion constraints

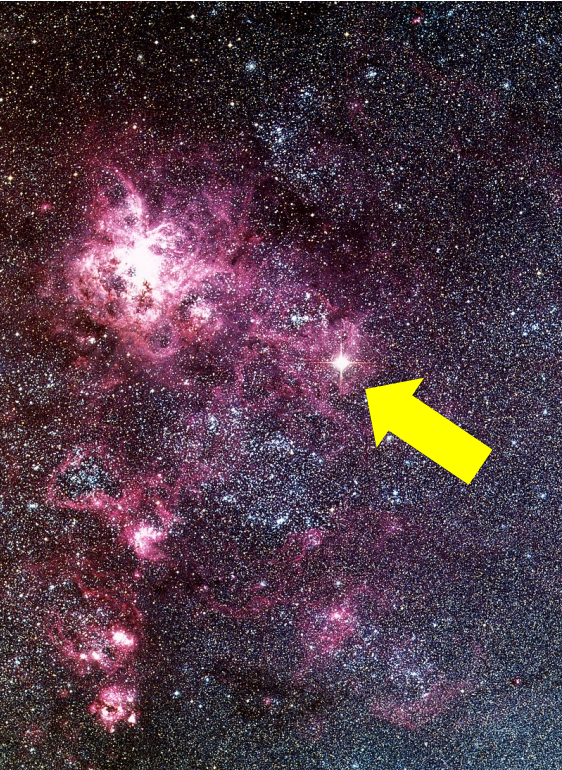


$$g_{ann} \lesssim 5 \times 10^{-10}$$

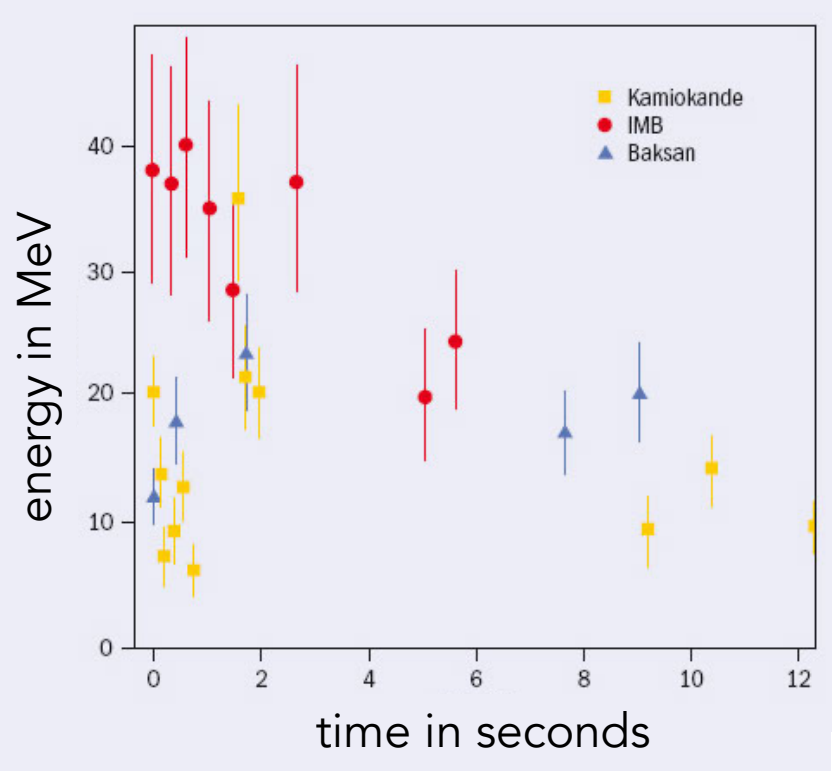
# Example: supernovae

[constraints: Chang, Essig, McDermott (2018)]

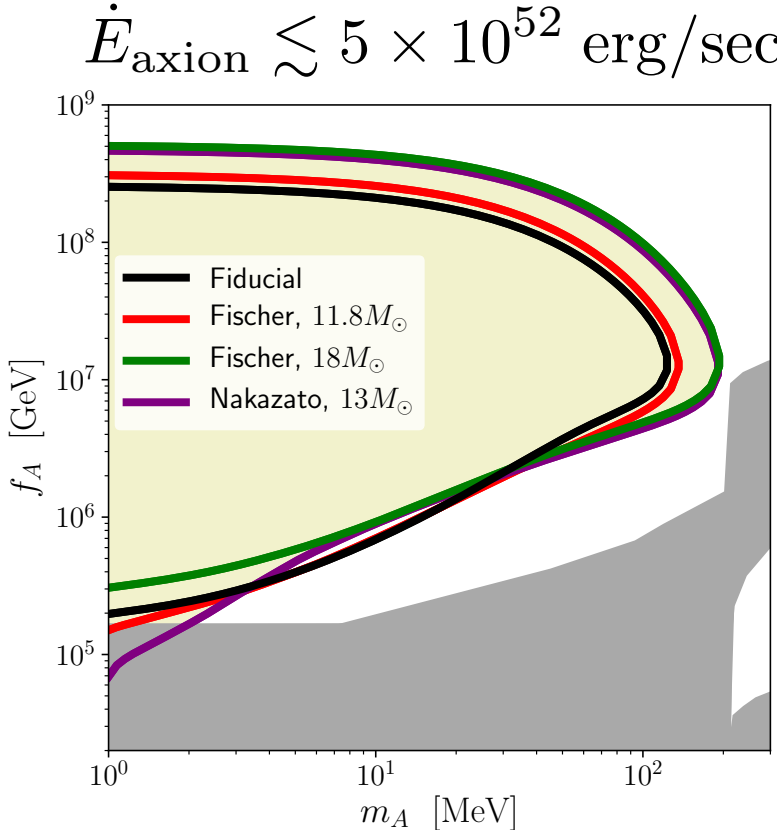
## SN 1987A



## Neutrino burst



## Constraints



how to test that stars emit axions?

*we want a signal, not just a constraint!*

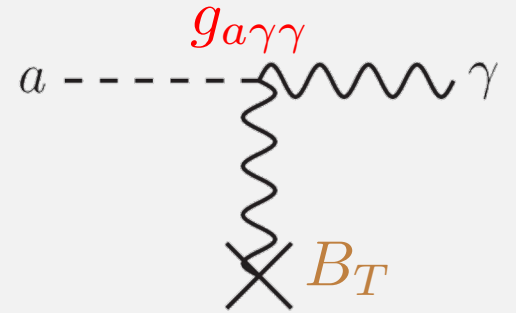
# Axions convert to photons in a B-field

axion

$$\Gamma \approx (10^{-19} \text{ photons/sec}) \left( \frac{g_{aee}}{10^{-13}} \right)^2 \left( \frac{g_{a\gamma\gamma}}{10^{-11}/\text{GeV}} \right)^2 \\ \times \left( \frac{B_T}{5 \text{ T}} \right)^2 \left( \frac{L}{100 \text{ cm}} \right)^2 \left( \frac{d_{\text{WD}}}{10 \text{ pc}} \right)^{-2}$$

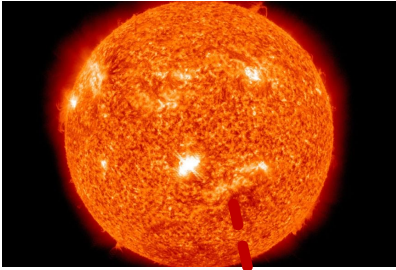
**~zero signal at earth from a nearby WD**

$$\mathcal{L}_{\text{int}} = -\frac{1}{4} g_{a\gamma\gamma} a F \tilde{F}$$



$$p_{a \rightarrow \gamma} \approx g_{a\gamma\gamma}^2 B_T^2 L^2 / 4$$

# Example: our Sun

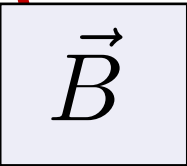


our Sun may be emitting axions

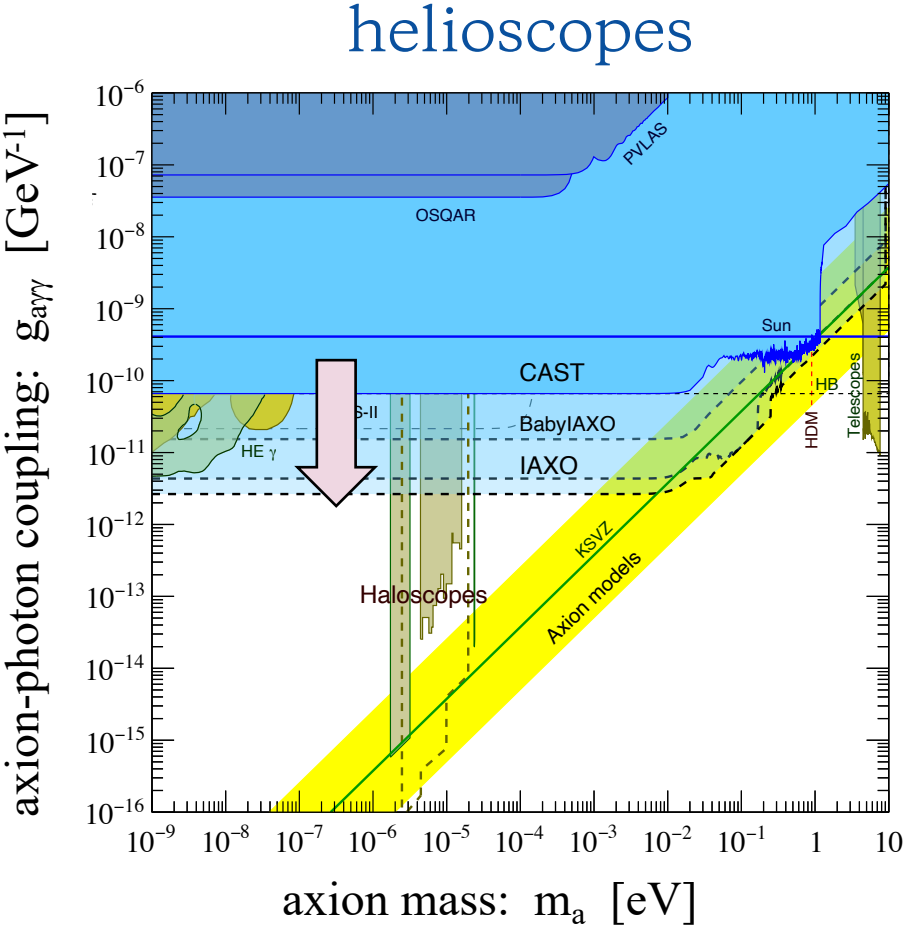
*axion*

we are searching for these axions in laboratories on Earth  
axion-photon interconversion  
in a strong magnetic field

**CAST**



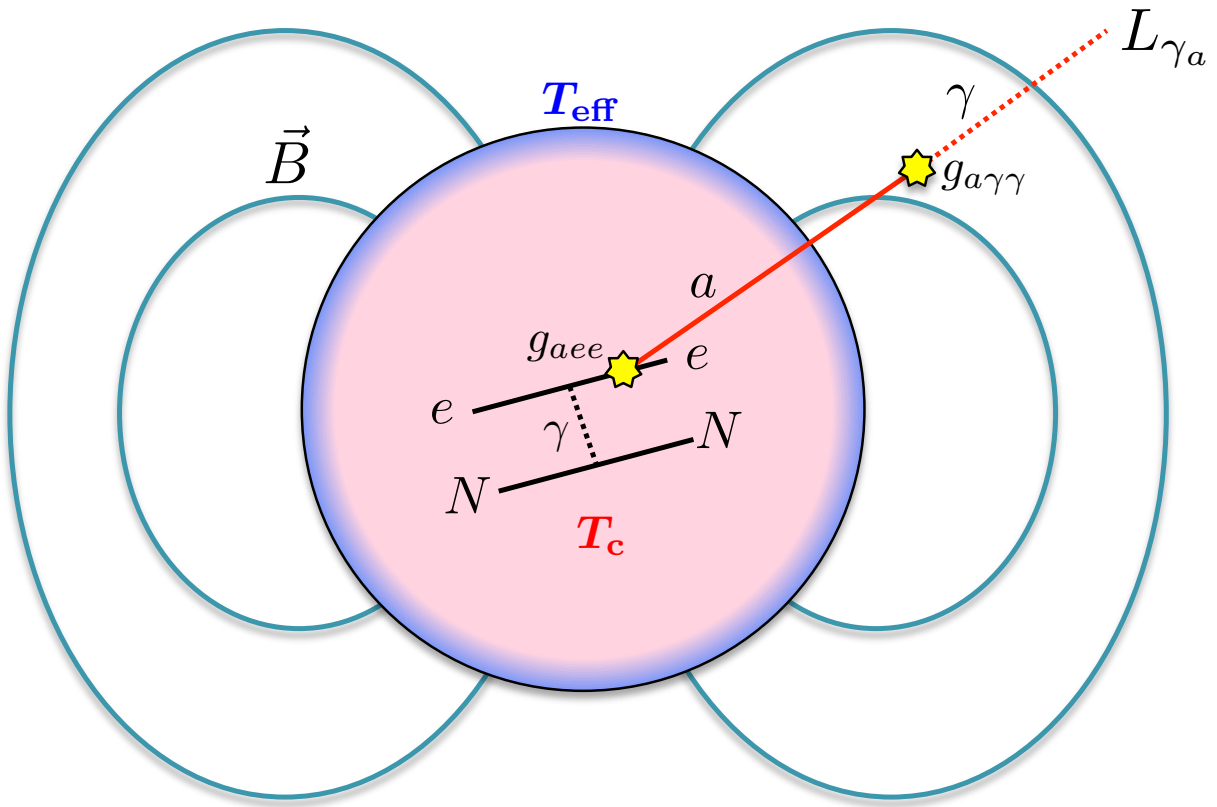
X-ray





# Axion-photon conversion at compact stars

[D. E. Morris (1986)] [Raffelt & Stodolsky (1987)]  
 [Gill & Heyl (2011)] [Fortin & Sinha (2018)]



**Strong magnetic field:**

- Neutron stars (magnetars):  $\sim 10^{12} - 10^{15}$  G
- Magnetic white dwarfs:  $\sim 10^6 - 10^9$  G

**Filling large volume:**

- Neutron stars (magnetars):  $\sim 10$  km
- Magnetic white dwarfs:  $\sim 0.01 R_{\text{sun}}$

**Hot plasma radiates axions:**

- Core temperature:  $10^7$  K  $\sim$  few keV

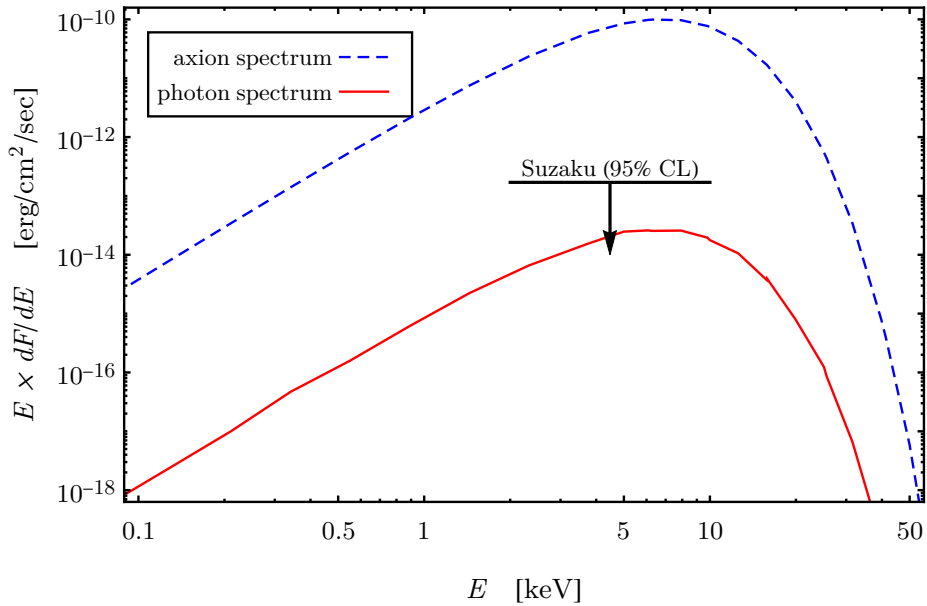
$$E_a = T_{\text{core}} = E_\gamma = \text{X-ray}$$

signal = thermal X-ray emission ( $T_{\text{core}} \sim 10^7$  K  $\sim$  keV)  
 background = surface emission negligible ( $T_{\text{surface}} \sim 10^4$  K)

# Expected X-ray signal from MWDs

[Dessert, AL, Safdi, arXiv:1903.04088]

## quasi-thermal spectrum



## top 10 magnetic white dwarf candidates

|                          | $M_{\text{WD}} [M_{\odot}]$ | $R_{\text{WD}} [R_{\odot}]$ | $L_{\gamma} [L_{\odot}]$ | $T_{\text{eff}} [\text{K}]$ | $B [\text{MG}]$ | $d_{\text{WD}} [\text{pc}]$ | $F_{2-10} [\text{erg/cm}^2/\text{s}]$ |
|--------------------------|-----------------------------|-----------------------------|--------------------------|-----------------------------|-----------------|-----------------------------|---------------------------------------|
| RE J0317-853             | 1.32                        | 0.00405                     | 0.0120                   | 30000                       | 200             | 29.54                       | $6.8 \times 10^{-14}$                 |
| WD 2010+310              | 1*                          | 0.00643*                    | 0.00566                  | 19750                       | 520             | 30.77                       | $4.4 \times 10^{-14}$                 |
| WD 0041-102 (Feige 7)    | 1.05                        | 0.00756                     | 0.00635                  | 18750                       | 35              | 31.09                       | $3.0 \times 10^{-14}$                 |
| WD 1031+234              | 0.937                       | 0.00872                     | 0.0109                   | 20000                       | 200             | 64.09                       | $2.3 \times 10^{-14}$                 |
| WD 1533-057              | 0.717                       | 0.0114                      | 0.0121                   | 18000                       | 31              | 68.96                       | $1.3 \times 10^{-14}$                 |
| WD 1017+367              | 0.730                       | 0.0111                      | 0.0082                   | 16500                       | 65              | 79.24                       | $7.1 \times 10^{-15}$                 |
| WD 1043-050              | 1.02                        | 0.00787                     | 0.00388                  | 16250                       | 820             | 83.33                       | $5.4 \times 10^{-15}$                 |
| WD 1211-171              | 1.06                        | 0.00754                     | 0.00992                  | 21000                       | 50              | 92.61                       | $5.4 \times 10^{-15}$                 |
| SDSS 131508.97+093713.87 | 0.848                       | 0.00968                     | 0.01347                  | 20000                       | 14              | 101.7                       | $3.5 \times 10^{-15}$                 |
| WD 1743-520              | 1.13                        | 0.00681                     | 0.00184                  | 14500                       | 36              | 38.93                       | $2.9 \times 10^{-15}$                 |

1000's of known WDs (Gaia), but only 100's have B-field measurements



rank by expected X-ray flux

rising through 1-10 keV where backgrounds are falling

$g_{aee} = 10^{-13}$   
 $g_{a\gamma\gamma} = 10^{-11} \text{ GeV}^{-1}$   
 $M_{\text{WD}} = 1.32 M_{\odot}$   
 $d_{\text{WD}} = 29.54 \text{ pc}$   
 $T_c = 2 \times 10^7 \text{ K}$   
 $= 1.7 \text{ keV}$

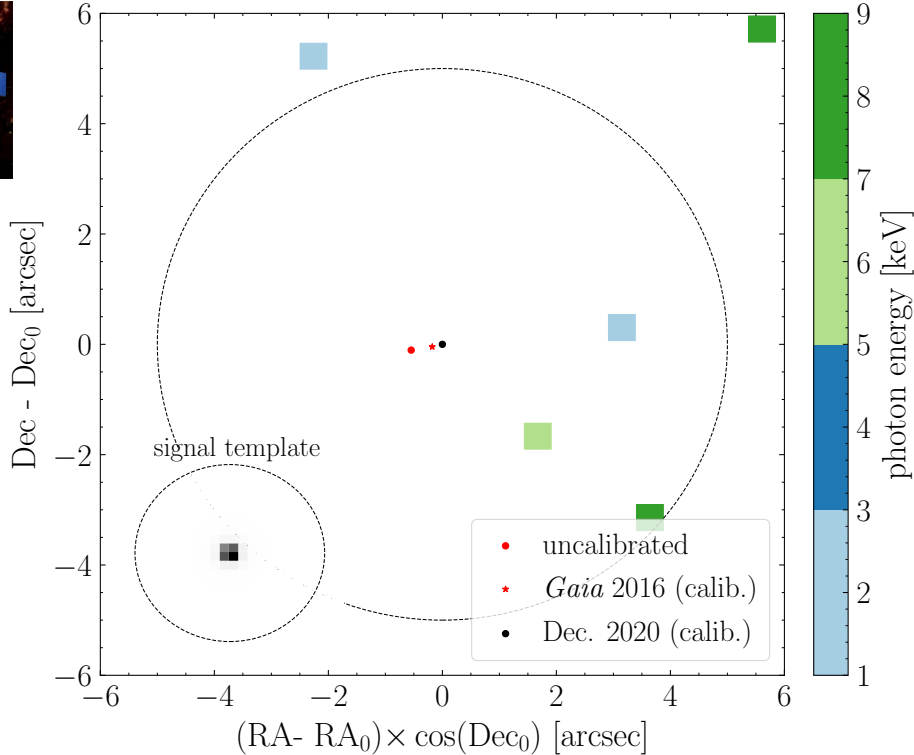
(for  $m_a = 10^{-9} \text{ eV}$  and  $|g_{aee} g_{a\gamma\gamma}| = 10^{-24} \text{ GeV}^{-1}$ )

# Searching for X-rays from Magnetic White Dwarfs

[Dessert, AL, Safdi (2019, 2021)]

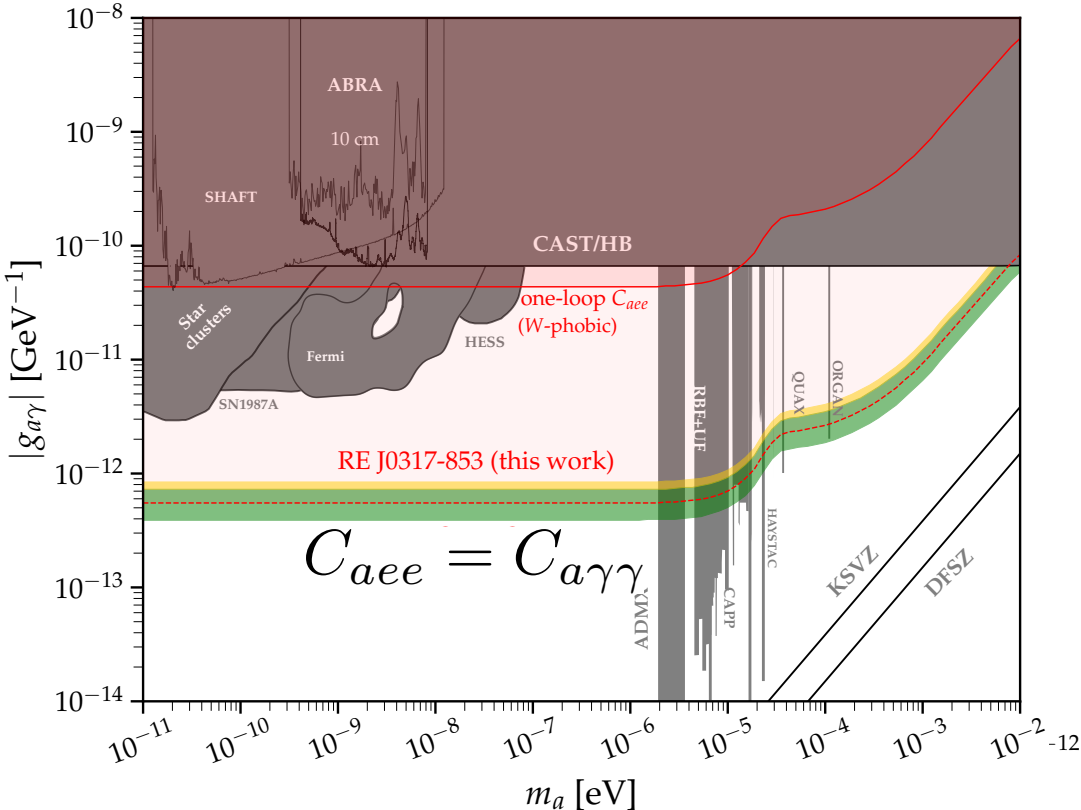
## Chandra observation

- 37.42 ks (~10 hr) of data, Dec 18, 2020
- No photon counts observed near source



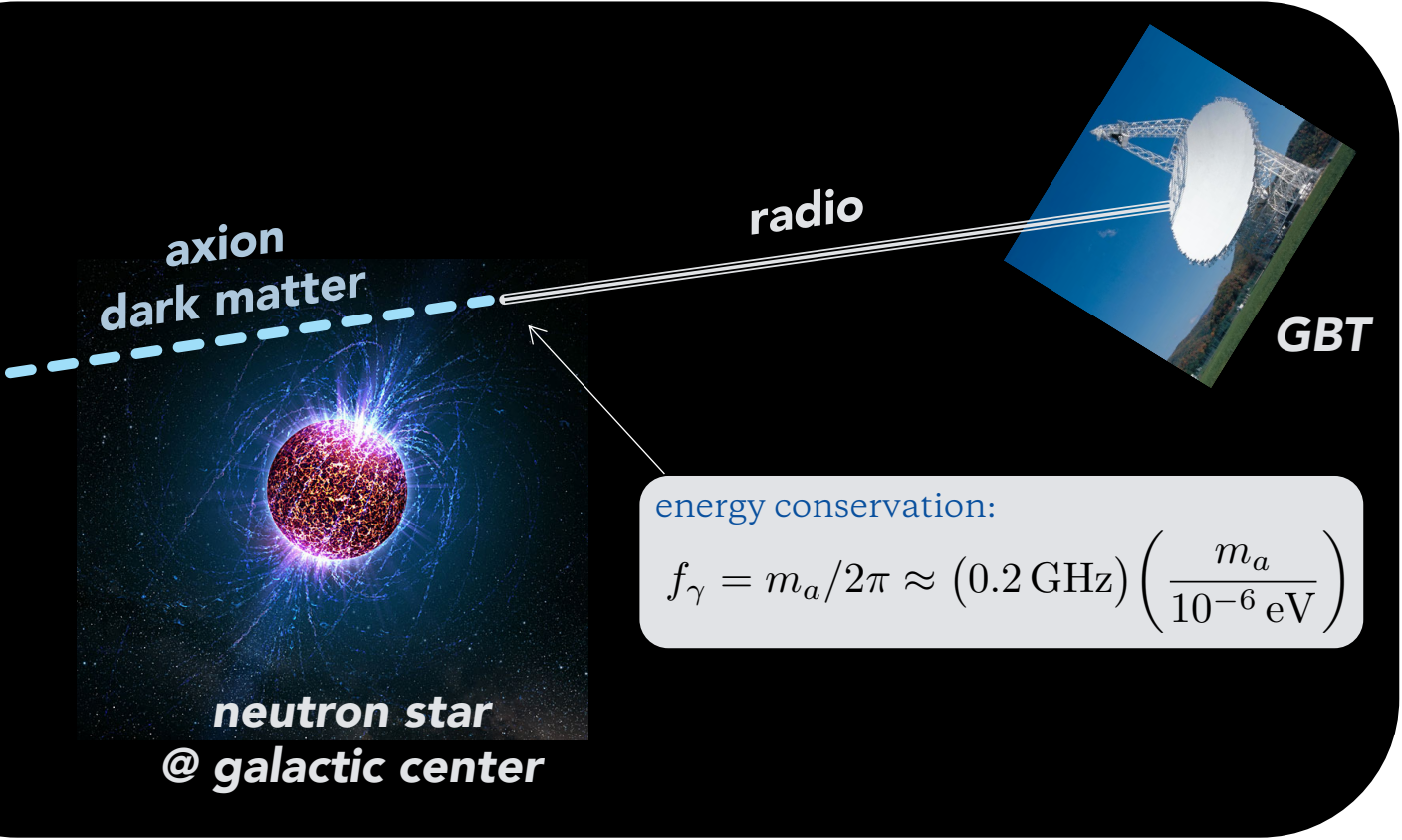
## Constraints on axion emission / X-ray conversion

- Upper limit on product of couplings  $g_{aee} * g_{a\gamma\gamma}$
- Can be recast as a limit in  $g_{a\gamma\gamma}$  alone

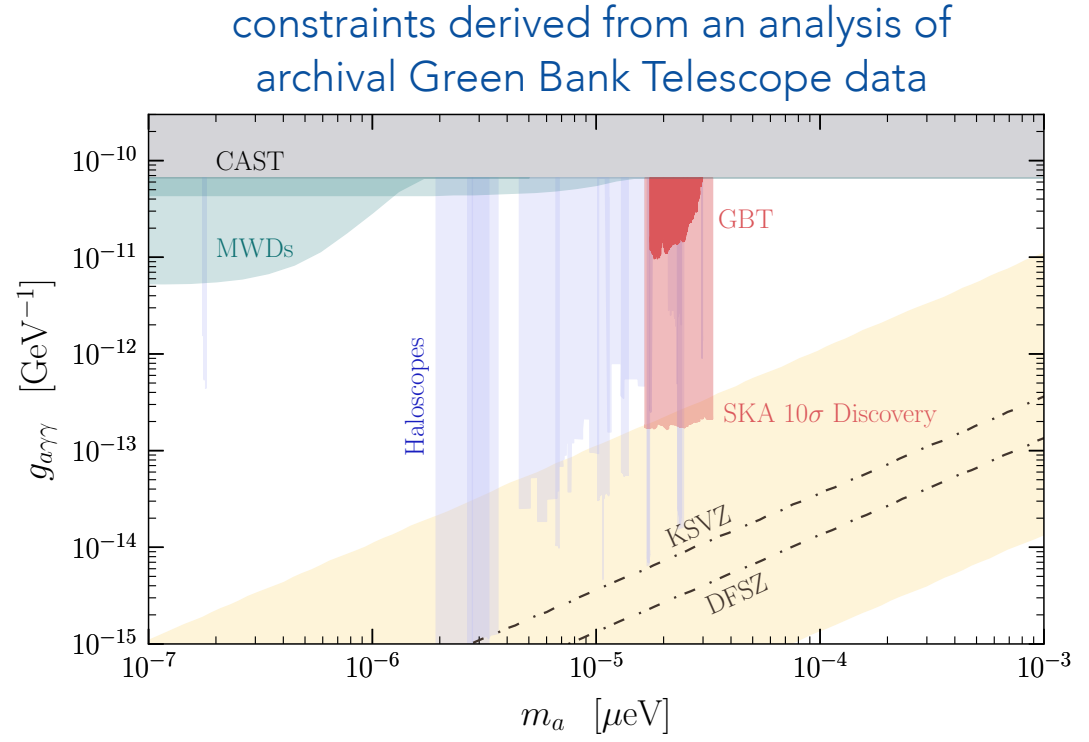


# Radio from the galactic center probes axion dark matter

[Hook, Kahn, Safdi, Sun (2018)], [Safdi, Sun, Chen (2018)], [Foster et al (2022)]



The galactic center neutron star population provides a strong magnetic field to resonantly convert axion dark matter into radio emission



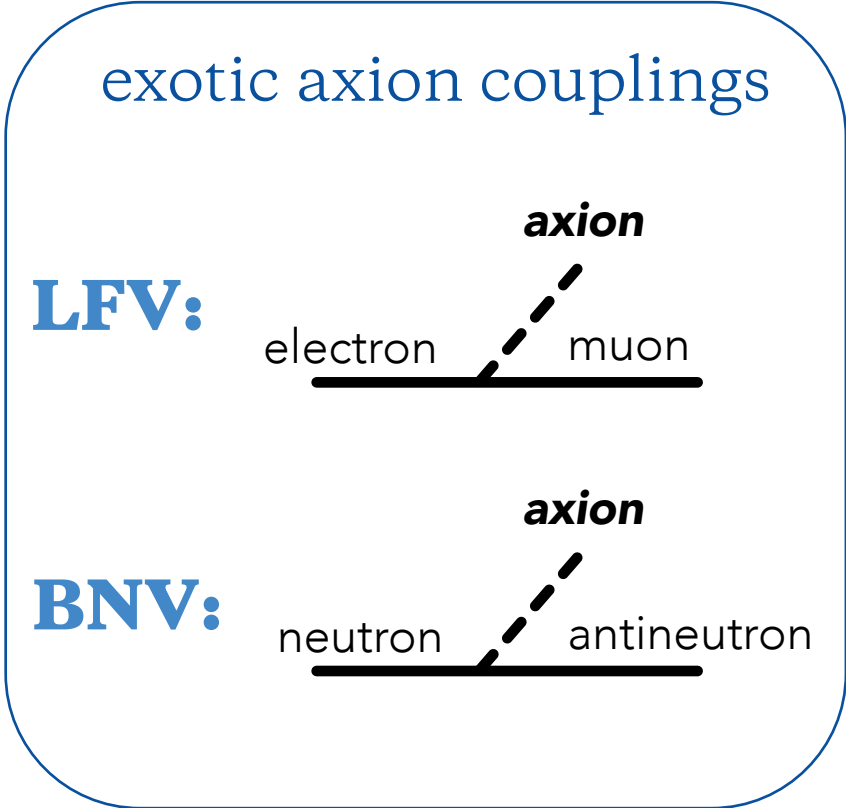
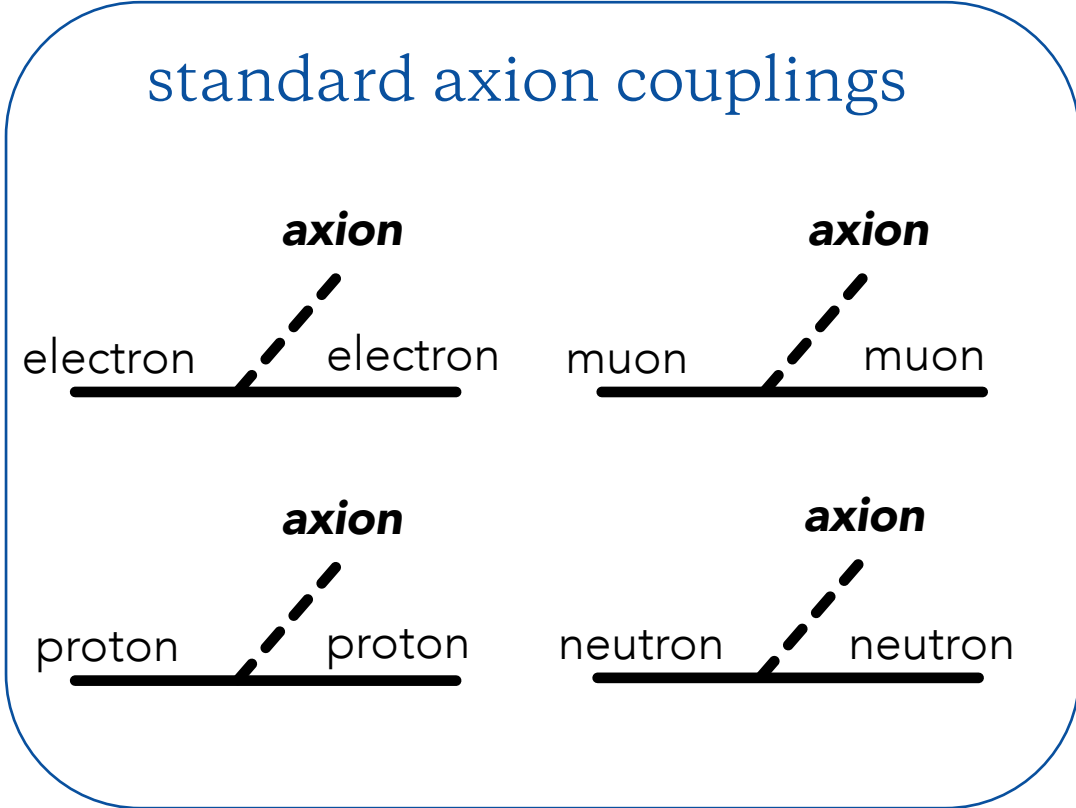


have we missed any interesting channels?

*let's look at exotic axion couplings*

# ALP emission from exotic couplings

[Zhang, Hagimoto, & AL, 2309.03889]



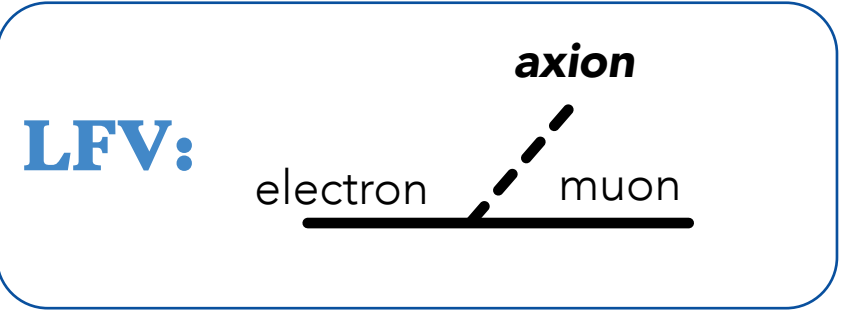
astro implications:

- axion emission off of muons in a neutron star
- baryon-destruction in a neutron star & heating
- connections with lab probes of axion LFV & BNV interactions

$$\mathcal{L}_{\text{int}} = g_{a\psi\psi} \partial_\mu a \bar{\psi} \gamma^\mu \gamma_5 \psi / 2m_\psi$$

# ALP emission from exotic couplings

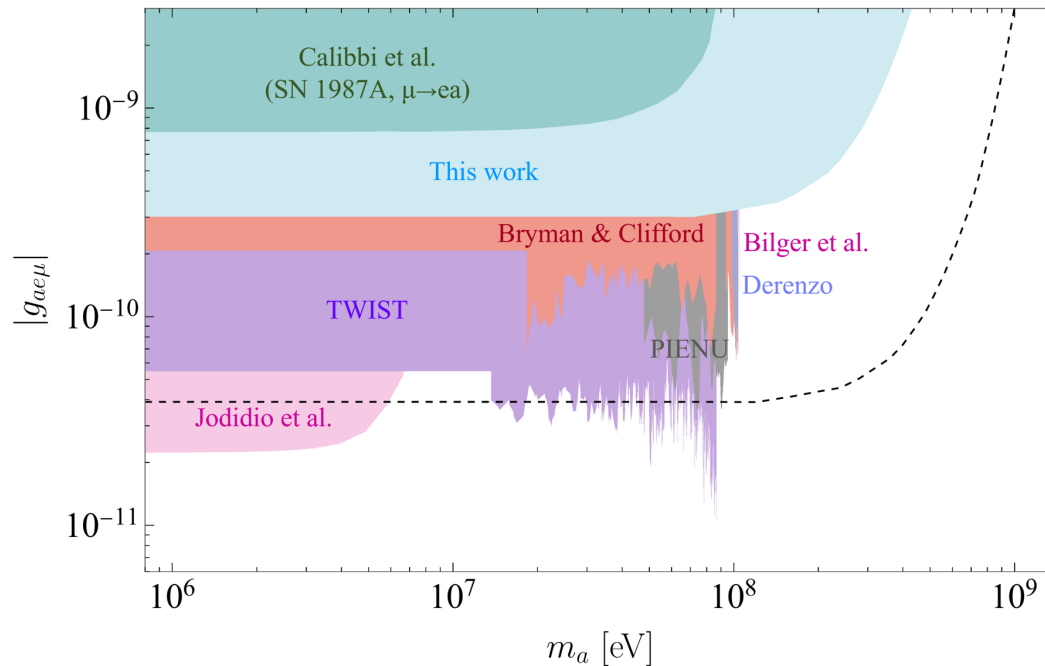
[Zhang, Hagimoto, & AL, 2309.03889]



axion emissivity

$$\epsilon_a^{\text{LFV}} \approx (4.8 \times 10^{10} \text{ erg/cm}^3/\text{sec}) \left( \frac{g_{ae\mu}}{10^{-11}} \right)^2 \left( \frac{T}{10^9 \text{ K}} \right)^8$$

constraints on axion-LFV interactions



- for a neutron star, strong lab limits imply that axion emission is subdominant to standard neutrino emission via the Murca processes
- due to the strong temperature dependence, much stronger limits can be derived from SN 1987A by considering its hot proto-neutron star

$$|g_{ae\mu}| \lesssim (4 \times 10^{-11}) \left( \frac{T}{50 \text{ MeV}} \right)^{-4}$$

$10^9 \text{ K} \approx 86.2 \text{ keV}$

can axions source their own electromagnetic radiation

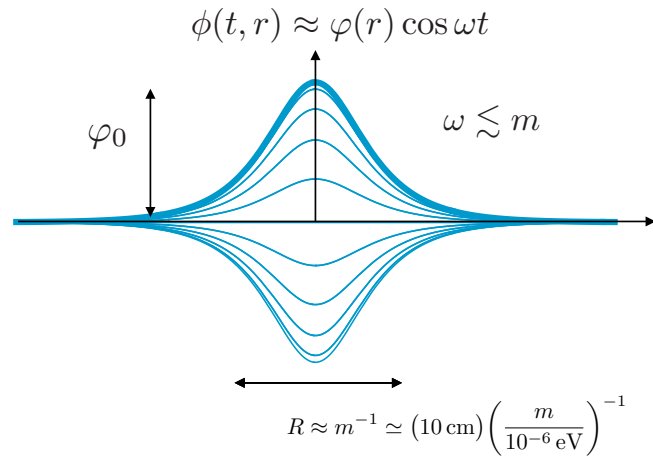
*let's look at compact clumps of cold axions*



# What if the axion DM is clumped up?

[Amin, AL, Mou, Saffin, arXiv:2103.12082]

dense axion star:  
a coherent “clump” of axion dark matter



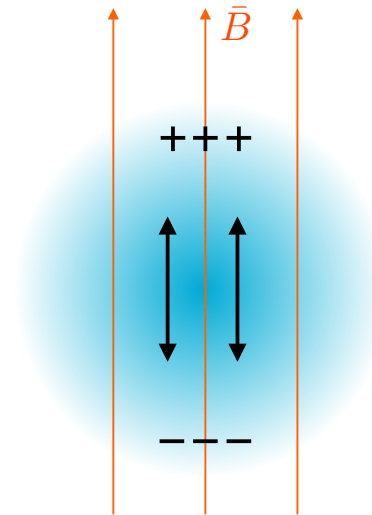
coupling to electromagnetism:  
new terms in Maxwell's equations

$$\mathcal{L}_{\text{int}} = -\frac{1}{4} g_{a\gamma} \phi F \tilde{F} \left\{ \begin{array}{l} \ddot{\phi} - \nabla^2 \phi + \partial_\phi V = g_{a\gamma} \mathbf{E} \cdot \mathbf{B}, \\ \dot{\mathbf{E}} = \nabla \times \mathbf{B} - g_{a\gamma} \left( \dot{\phi} \mathbf{B} + \nabla \phi \times \mathbf{E} \right), \\ \dot{\mathbf{B}} = -\nabla \times \mathbf{E}, \\ \nabla \cdot \mathbf{E} = -g_{a\gamma} \nabla \phi \cdot \mathbf{B}, \\ \nabla \cdot \mathbf{B} = 0. \end{array} \right.$$

effective current density

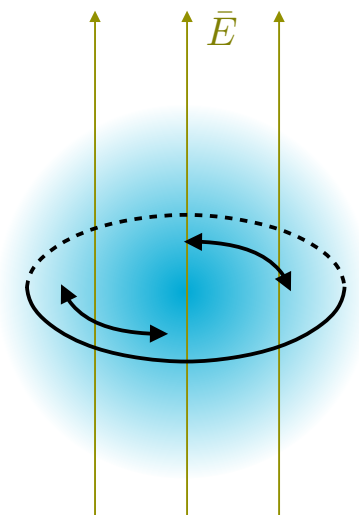
effective charge density

background  
magnetic field



induced  
electric dipole

background  
electric field



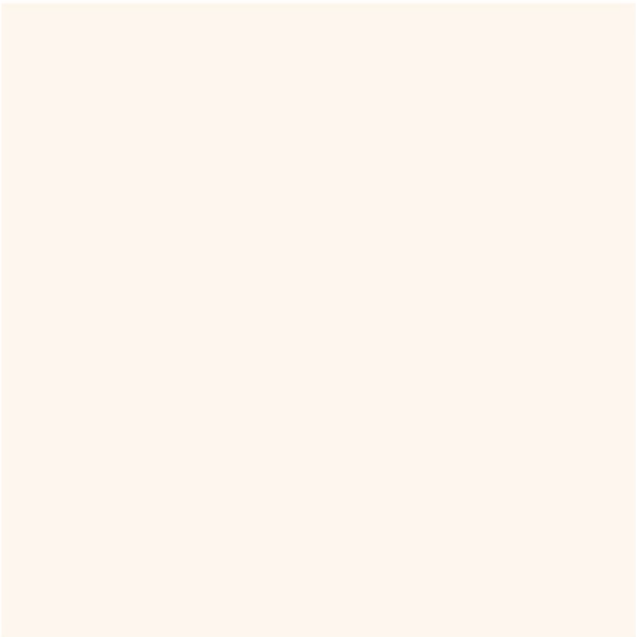
induced  
magnetic dipole

**a source of EM radiation!**

# EM radiation from an axion clump

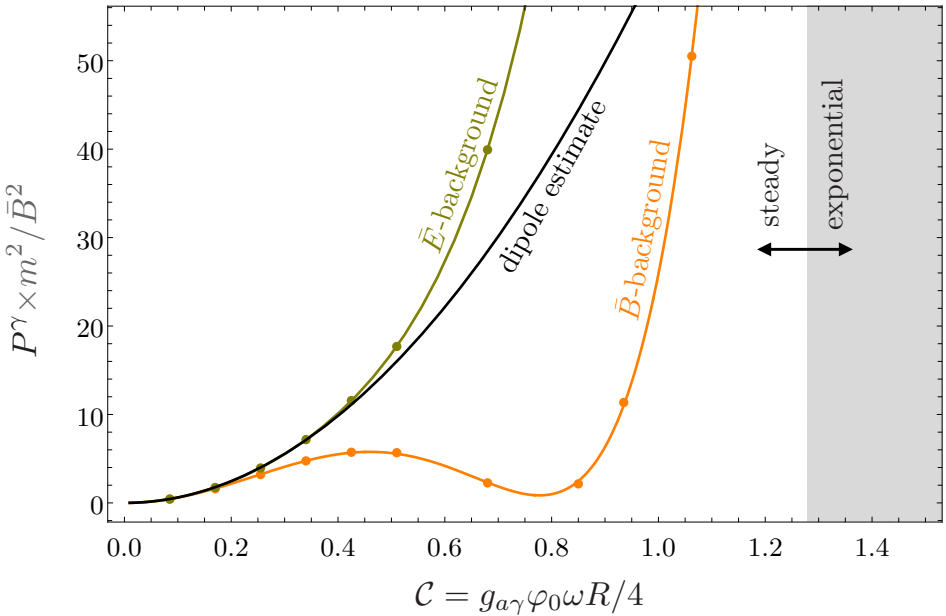
[Amin, AL, Mou, Saffin, arXiv:2103.12082]

lattice simulation:  
radiation from clump in external B/E fields



shading shows intensity of EM field

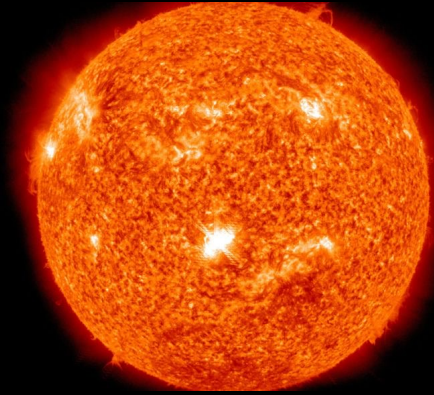
EM power radiated:  
departure from dipole approx. at larger coupling



$$P_{\text{dipole}} = \frac{g_{a\gamma}^2 \omega^4 \tilde{\varphi}^2(\omega)}{12\pi} (|\bar{\mathbf{B}}|^2 + |\bar{\mathbf{E}}|^2)$$

# Astrophysical Probes

observe the influence of axions on stars, gas, & compact objects

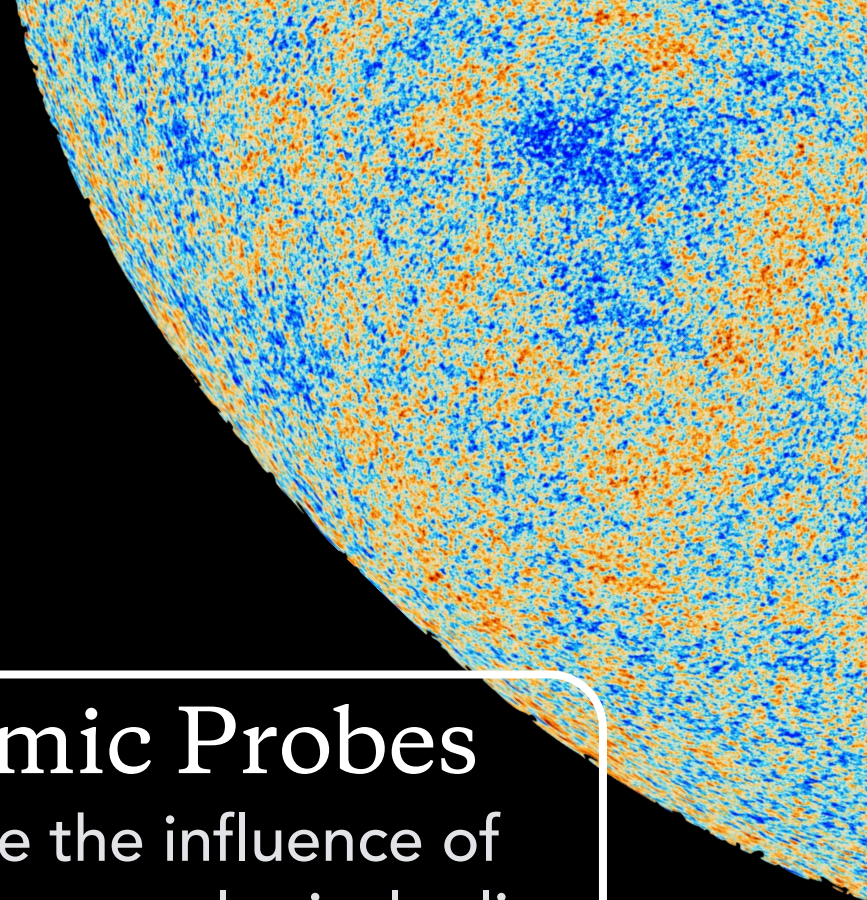


# Cosmic Probes

observe the influence of axions on cosmological relics

# Terrestrial Probes

create axions on Earth or detect axions as they pass by the Earth



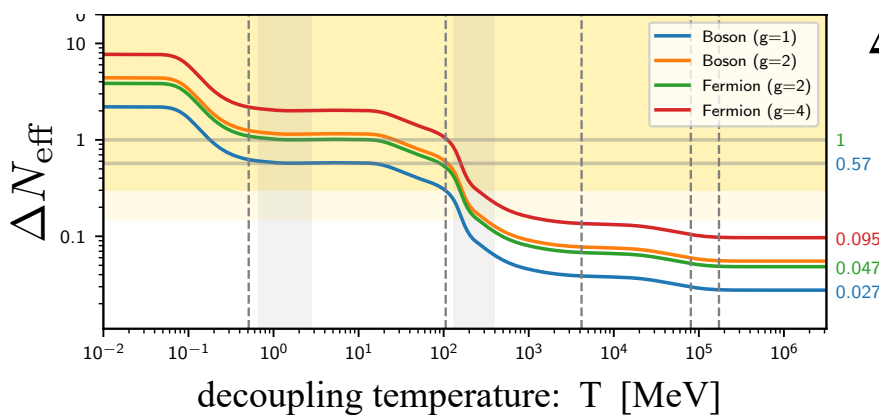
# Axion dark radiation influence on CMB

[Baumann, Green, & Wallisch (2016)]  
[CMB S4 Science Book (2016)]

Precision CMB measurements constrain the presence of a “dark radiation” in the Universe

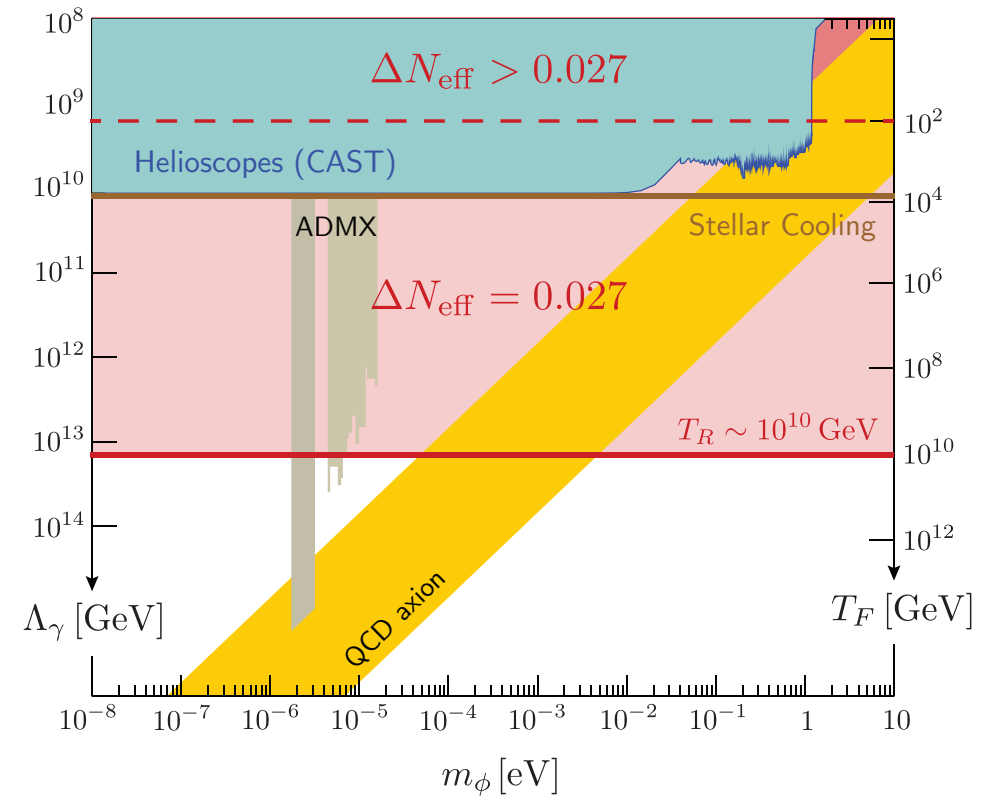
$$\Delta N_{\text{eff}} \approx \frac{\rho_{\text{dark}}}{\rho_{\text{one } \nu}} \lesssim 0.3 \quad (\text{Planck 2018})$$

For thermalized axions we expect:



$$\Delta N_{\text{eff}} > 0.027$$

testable parameter space

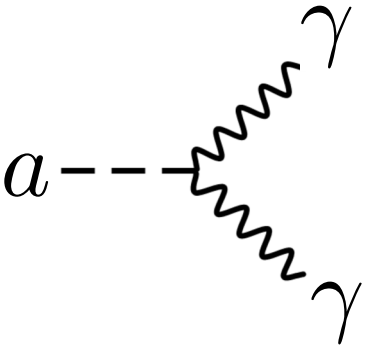




# Decaying axion radiation & BBN

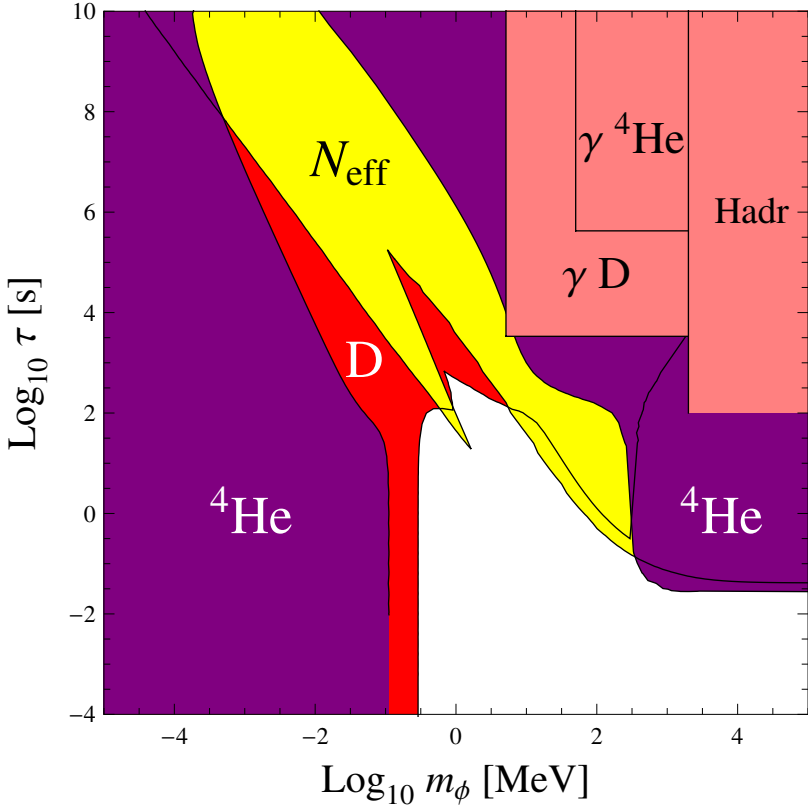
[Cadamuro & Redondo (2011)]

Axions decay through their coupling to photons



$$\Gamma_a \propto g_{a\gamma\gamma}^2 m_a^3$$

Axion decays during **nucleosynthesis** would disrupt the abundance of light elements.



# Another way of probing axions with the CMB

[Harvey & Naculich (1989)], [Carroll, Field, Jackiw (1990,91)], [Harari, Sikivie (1992)]  
 [Fedderke, Graham, Rajendran (2019)], [Agrawal, Hook, Huang (2019)]  
 [Yin, Dai, Ferraro (2021) & (2023)]

assume interaction  
 with electromagnetism:  
 standard Chern-Simons coupling

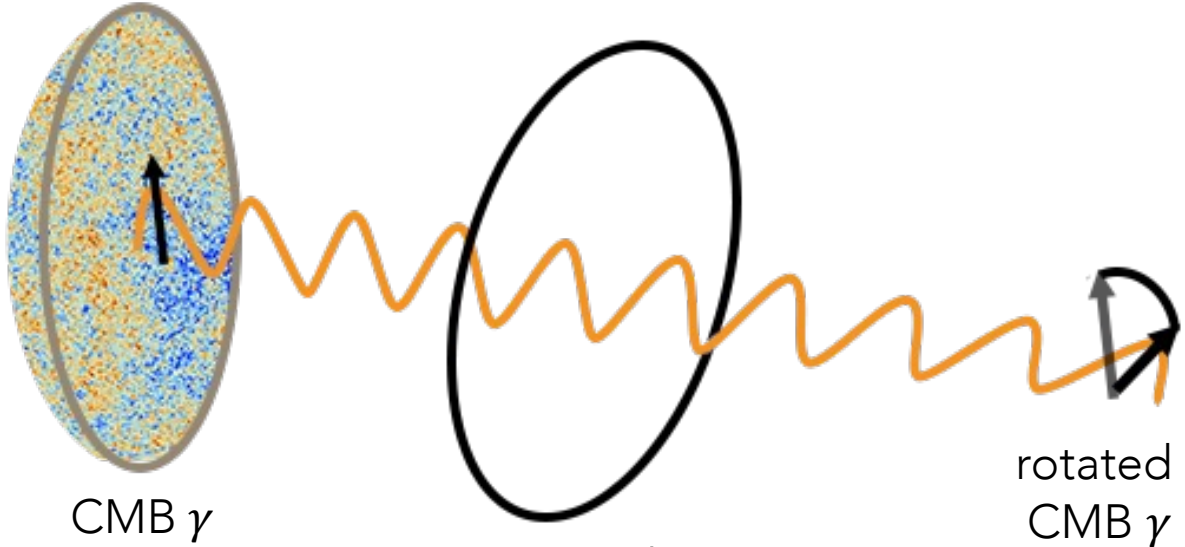
$$\mathcal{L}_{\text{int}} = -\frac{1}{4} g_{a\gamma\gamma} a F \tilde{F}$$

$$g_{a\gamma\gamma} = -\mathcal{A} \frac{\alpha_{\text{em}}}{\pi f_a}$$

$$\mathcal{A} = \sum Q_{\text{PQ}} Q_{\text{em}}^2 \sim \#/9$$

axion-induced birefringence:  
 an electromagnetic wave  
 traveling through a varying axion field  
 has its plane of polarization rotated

$$\alpha = \frac{1}{2} g_{a\gamma\gamma} \int_C dX^\mu \partial_\mu a(X)$$



rotation angle

$$\alpha = g_{a\gamma\gamma} \pi f_a$$

$$\equiv -\mathcal{A} \alpha_{\text{em}}$$

$$\approx -0.42^\circ \mathcal{A}$$

axion string loop

$$\Delta a = 2\pi f_a$$

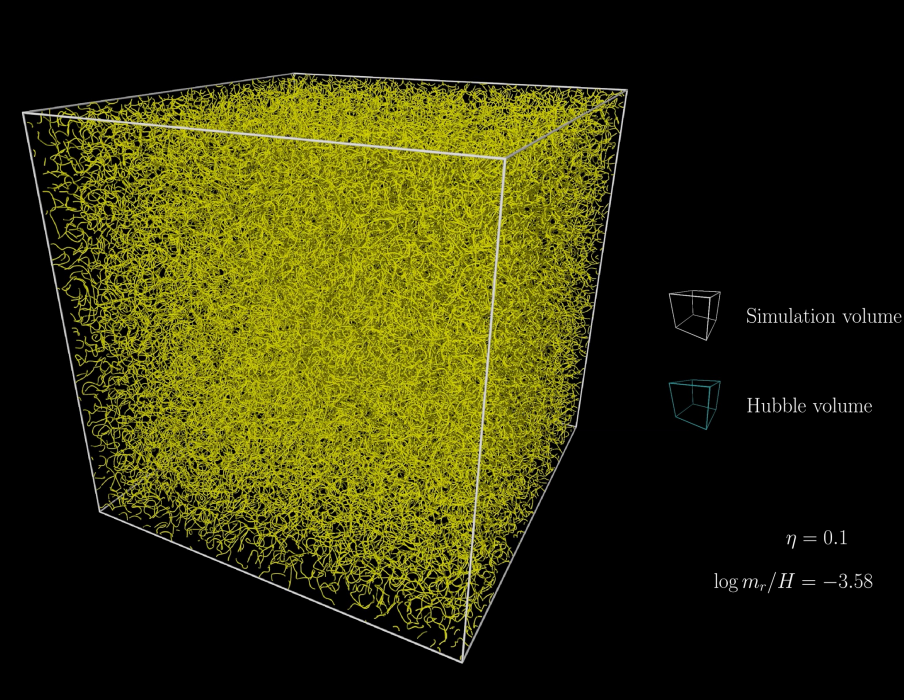
rotated  
 CMB  $\gamma$

\* birefringence can be measured through E-B cross correlation

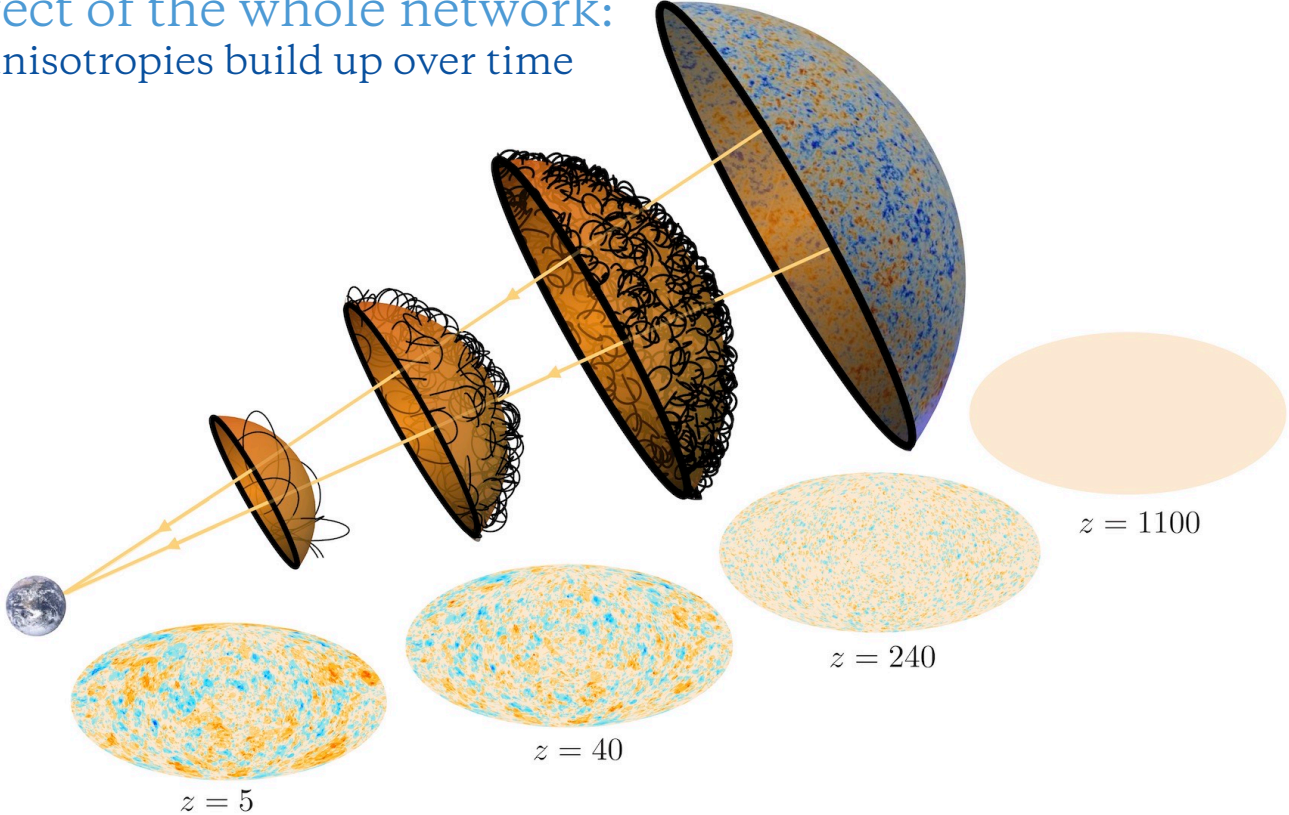
# Birefringence from an axion string network

[Jain, Hagimoto, AL, Amin]  
[simulation: Buschmann et. al. (2022)]

axions can form cosmic strings  
network evolves throughout the cosmic history



effect of the whole network:  
anisotropies build up over time



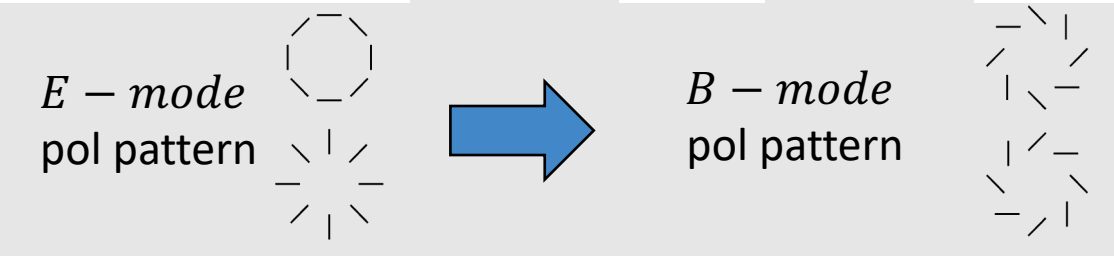
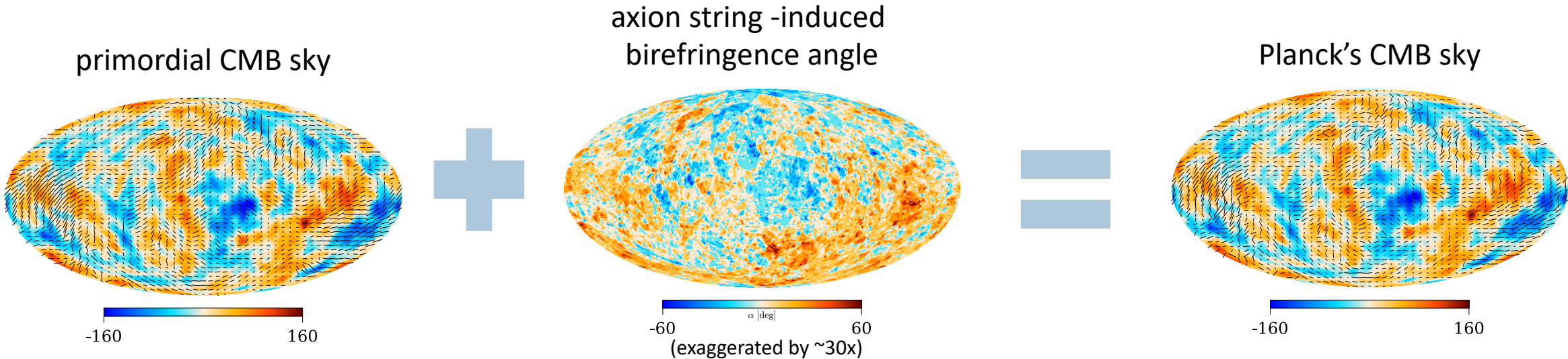
\* need  $m_a \lesssim 3H_{\text{cmb}} \approx 10^{-28}$  eV for the network to survive until after recombination

# Effect on CMB polarization

How does birefringence affect the CMB's temperature and polarization?

$$T(\hat{n}) \rightarrow T(\hat{n})$$

$$[Q \pm iU](\hat{n}) \rightarrow [(Q \pm iU)e^{\pm 2i\Delta\Phi}](\hat{n})$$



Signal of axion string-induced cosmological birefringence

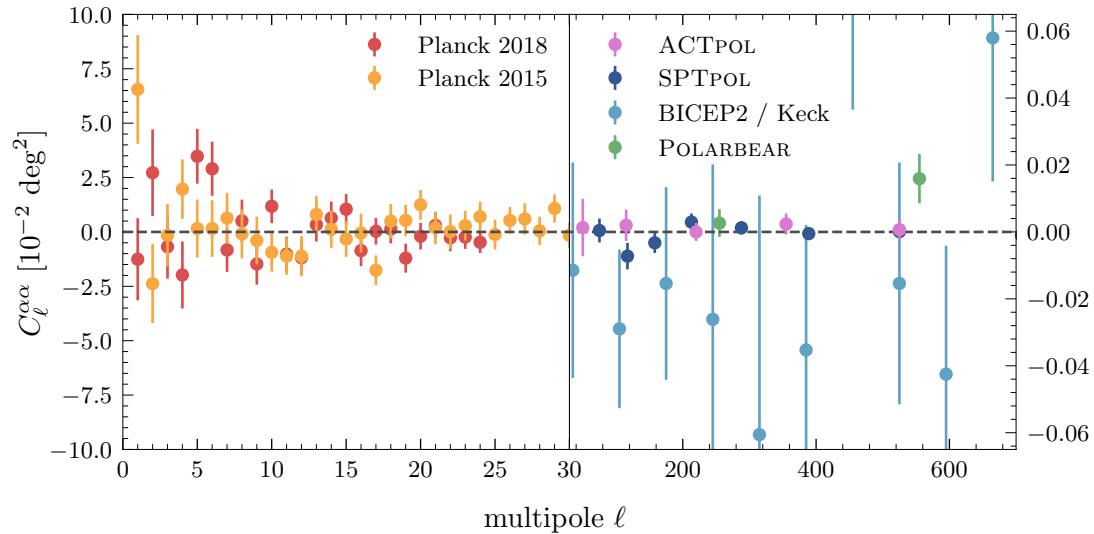
$$C_l^{EB} \sim \sin(4\alpha) (C_l^{EE} - C_l^{BB})$$

$$\begin{cases} \langle TB \rangle \neq 0 \\ \langle EB \rangle \neq 0 \end{cases}$$

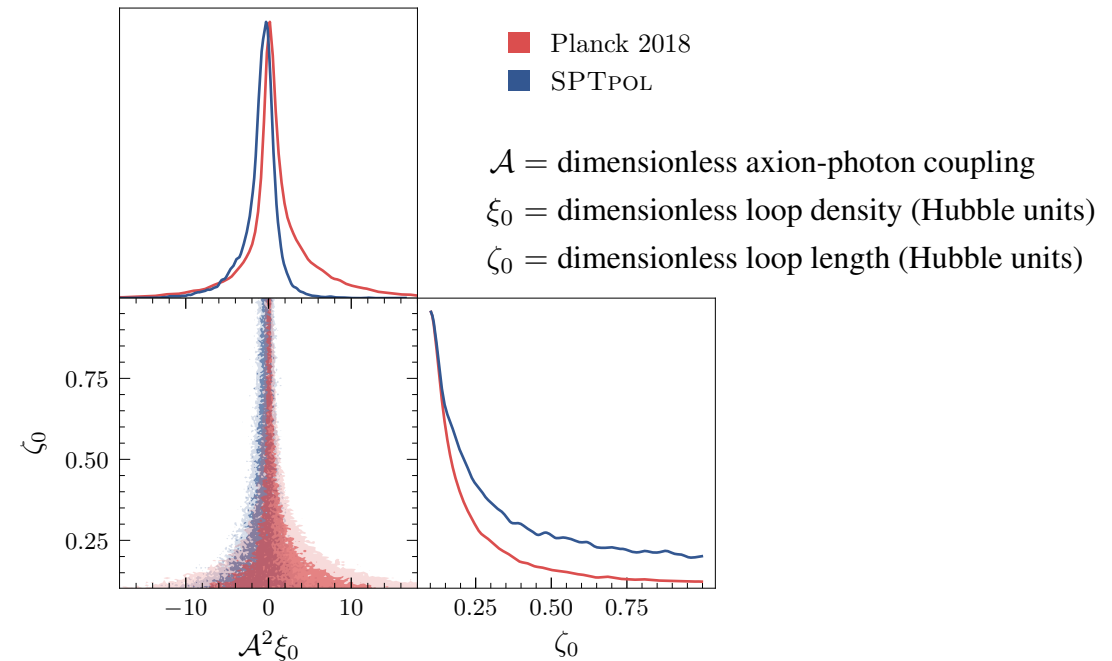
# Constraints on axion string networks

[Jain, Hagimoto, AL, Amin]

measurements of CMB polarization:  
no evidence for anisotropic birefringence



a constraint on axion strings networks  
& their coupling to electromagnetism:



already valuable constraints: **SPTPOL:  $\mathcal{A}^2 \xi_0 < 3.7$  at 95% CL**



# Implications

CMB observations constrain:

$$\text{SPTPOL: } \mathcal{A}^2 \xi_0 < 3.7 \text{ at 95\% CL}$$

Typical axion-photon coupling:

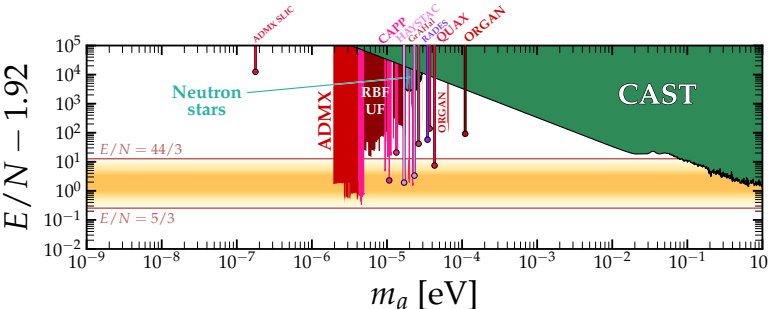
$$\mathcal{A} = 1/3$$

Typical loop abundance:

$$\xi_0 = 30$$

$$\mathcal{A}^2 \xi_0 \approx 3.3$$

... already probing an O(1) anomaly coefficient!  
... but still large uncertainties in  $\xi_0$  (from sims)





# Projected sensitivity

future telescopes  
probes of isotropic + aniso. birefringence

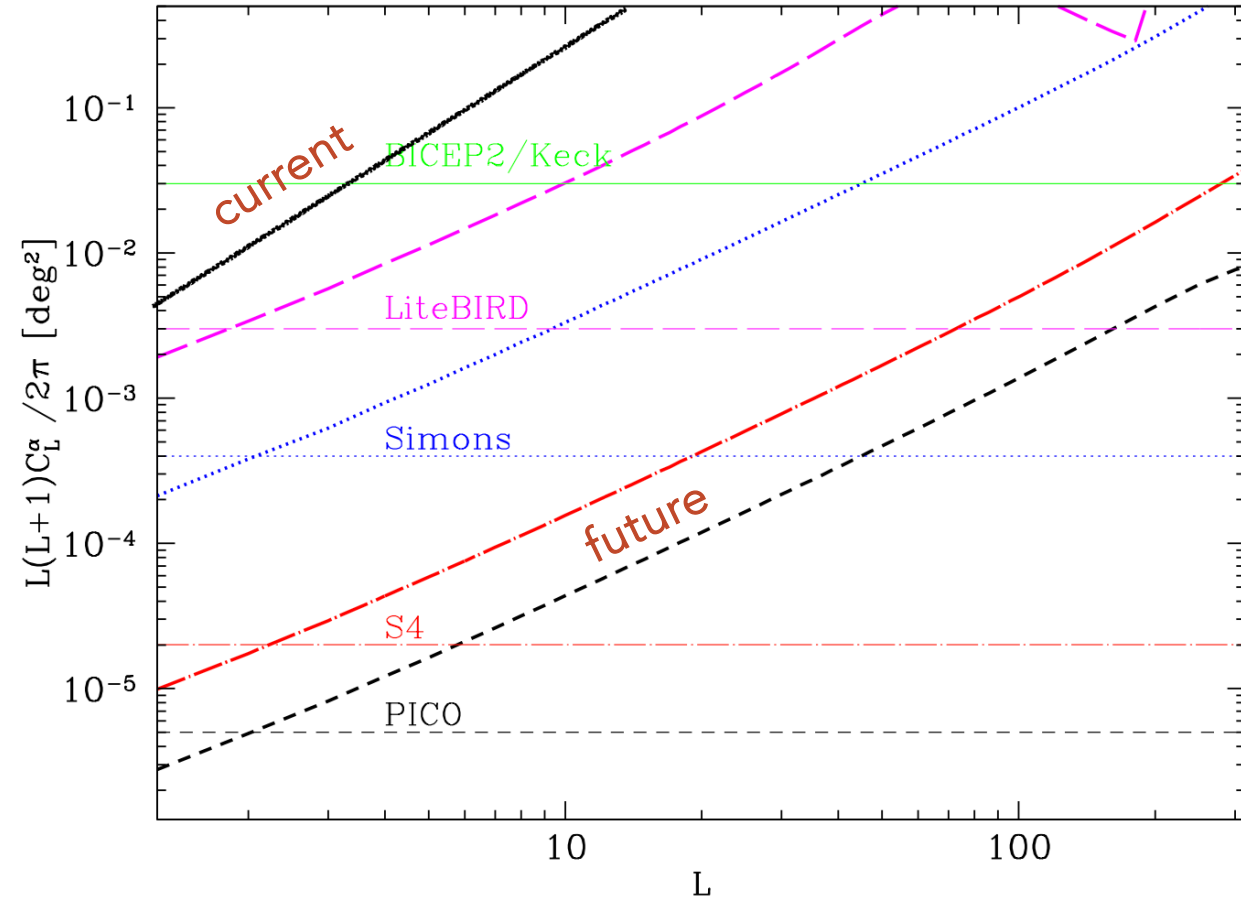
| Current  |                        |                     | LiteBIRD |                        |                     | SO       |                        |                     | CMB-S4-like |                        |                     | PICO     |                        |                     |
|----------|------------------------|---------------------|----------|------------------------|---------------------|----------|------------------------|---------------------|-------------|------------------------|---------------------|----------|------------------------|---------------------|
| $\alpha$ | $A_\alpha$             | $\sqrt{C_2^\alpha}$ | $\alpha$ | $A_\alpha$             | $\sqrt{C_2^\alpha}$ | $\alpha$ | $A_\alpha$             | $\sqrt{C_2^\alpha}$ | $\alpha$    | $A_\alpha$             | $\sqrt{C_2^\alpha}$ | $\alpha$ | $A_\alpha$             | $\sqrt{C_2^\alpha}$ |
| /        | $10^{-2} \text{deg}^2$ | $/$                 | /        | $10^{-3} \text{deg}^2$ | $/$                 | /        | $10^{-4} \text{deg}^2$ | $/$                 | /           | $10^{-5} \text{deg}^2$ | $/$                 | /        | $10^{-5} \text{deg}^2$ | $/$                 |
| -        | -                      | -                   | 1.3      | 2.7                    | 0.9                 | 0.56     | 3                      | 0.29                | 0.1         | 1.4                    | 0.065               | 0.05     | 0.4                    | 0.035               |
| -        | -                      | -                   | 1.5      | 3.3                    | 1.0                 | 0.66     | 4                      | 0.35                | 0.11        | 2.0                    | 0.08                | 0.06     | 0.5                    | 0.04                |
| -        | -                      | -                   | 1.4      | 3.5                    | 1.0                 | 0.64     | 5.0                    | 0.4                 | 0.13        | 2.5                    | 0.09                | 0.08     | 1.2                    | 0.06                |
| 30       | 2                      | 3                   | 1.6      | 4.0                    | 1.1                 | 0.71     | 5.5                    | 0.4                 | 0.15        | 3.3                    | 0.1                 | 0.09     | 1.4                    | 0.065               |

BLE II. Current and forecasted 68% CL bounds on the uniform and the anisotropic CPR parameters.

$$A_\alpha = L(L + 1)C_L^\alpha / 2\pi$$

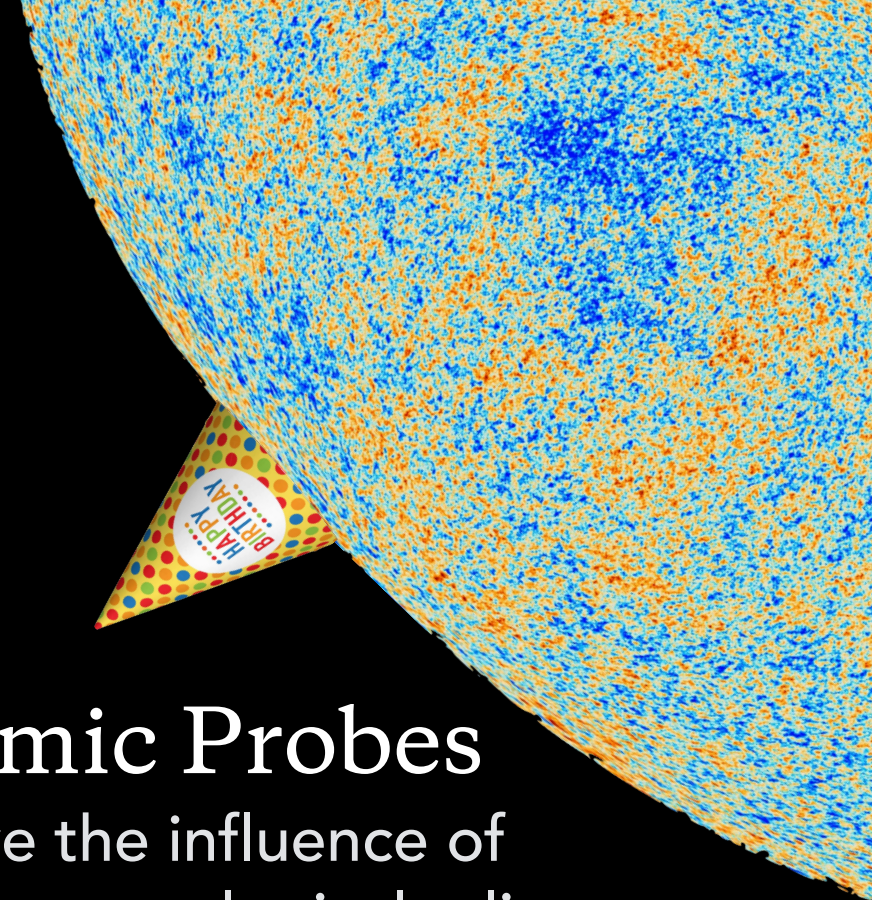
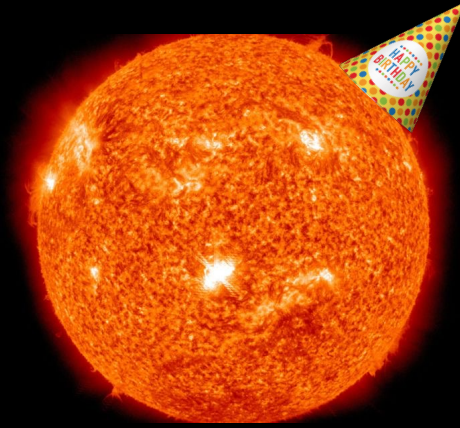
future CMB polarization measurements will drastically improve sensitivity to axion-string induced anisotropic birefringence

diagonal = allows multipoles to vary independently  
horizontal = restricts to a scale invariant spectrum



# Astrophysical Probes

observe the influence of axions on stars, gas, & compact objects



# Cosmic Probes

observe the influence of axions on cosmological relics



# Terrestrial Probes

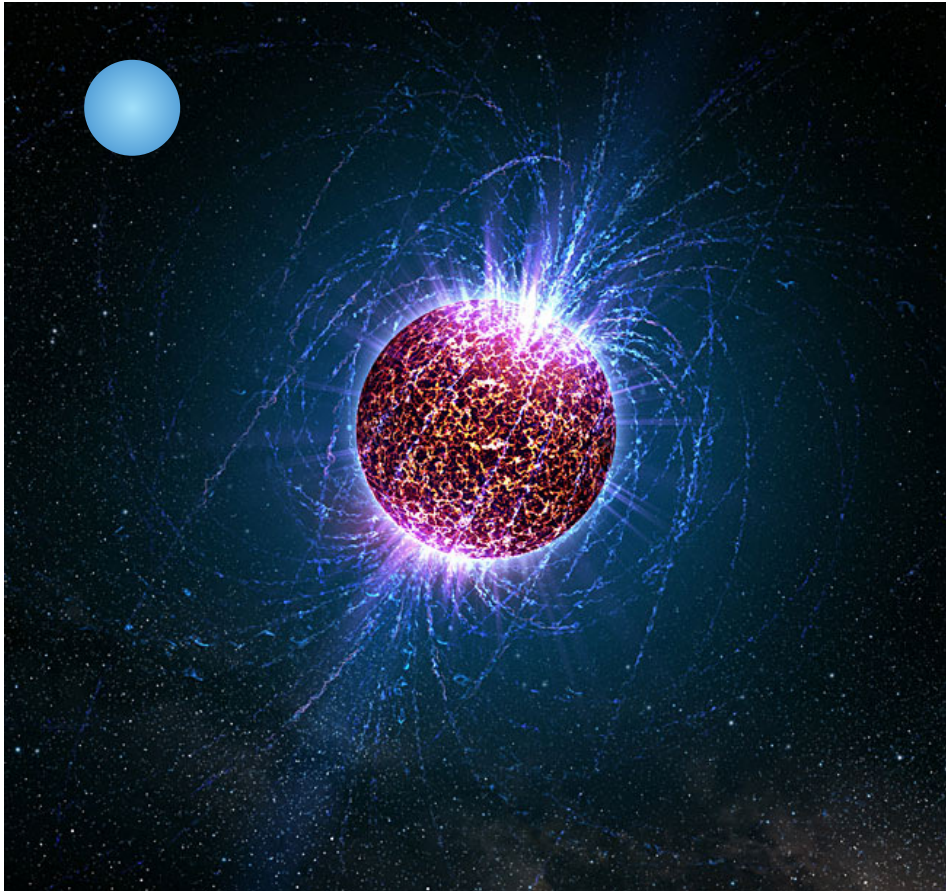
create axions on Earth or detect axions as they pass by the Earth



backup slides



# Connection with astrophysics



Astrophysical implications worth exploring more closely:

- Radio bursts from NS encounters
- Transient rather than stochastic
- NS environment contains plasma allowing for resonant conversion (not considered here)
- Robust rate estimates require careful population modeling

the loop crossing model  
simplified string network



# The loop-crossing model

## Assumptions

- All loops are circles
- Randomize loop orientation
- Randomize loop location in space
- All loops same radius at any time
- Loop radius evolves tracking Hubble

$$R(t) = \zeta_0 / H(t)$$

- Number of loops tracks Hubble

$$\rho(t) = \xi_0 \mu(t) H(t)^2$$

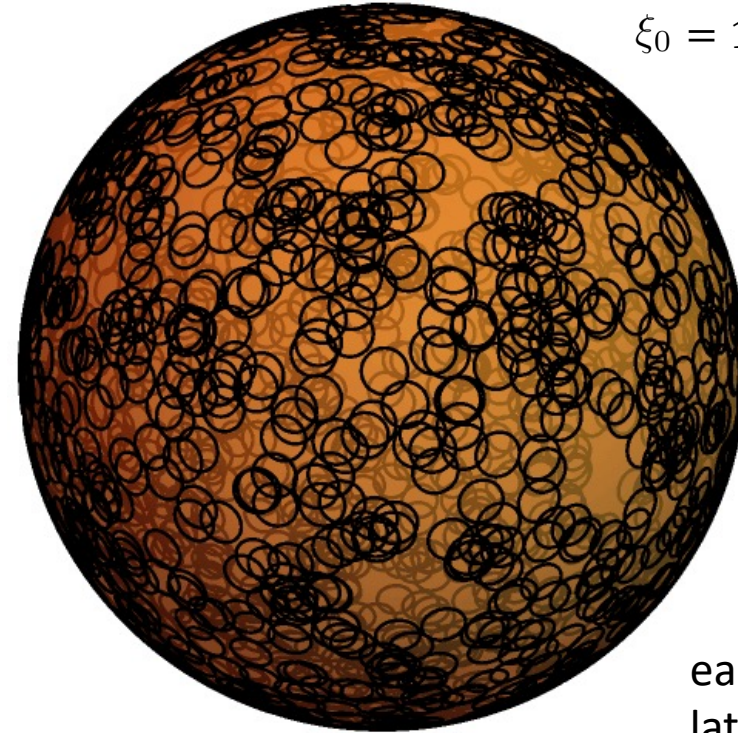
## Model Parameters

$$\{m_a, \mathcal{A}, \zeta_0, \xi_0\}$$

## loop-crossing model

$$\zeta_0 = 1.0$$

$$\xi_0 = 1.0$$



early time -> small loops  
late time -> large loops

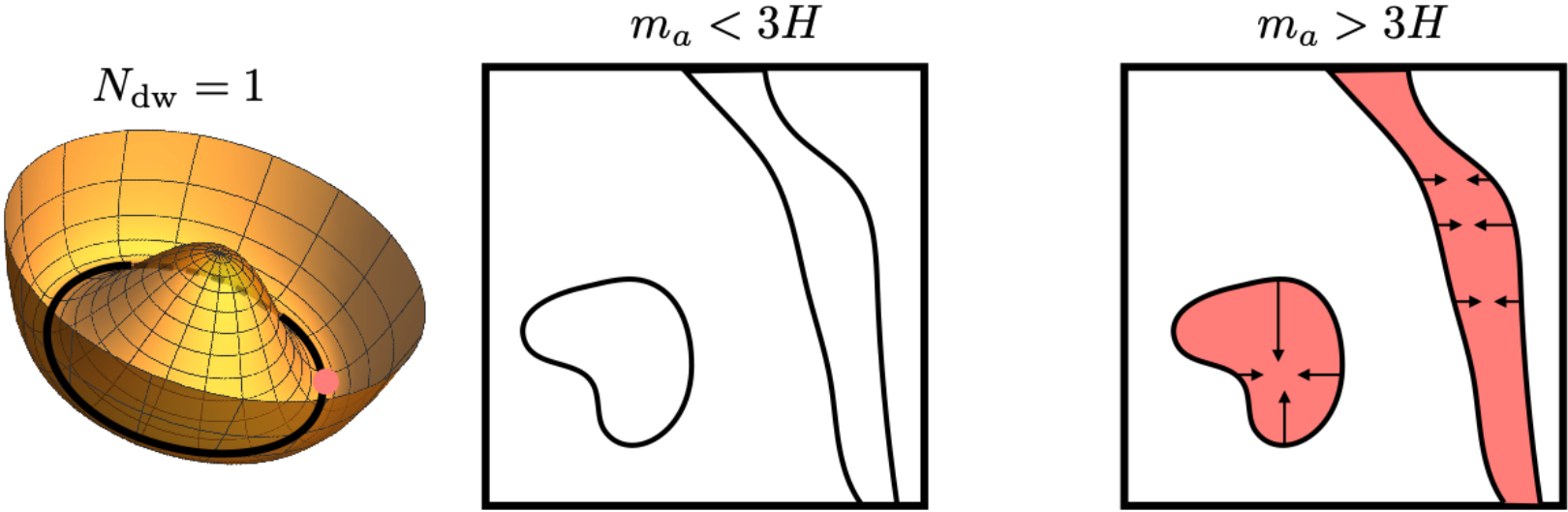
effect of  
varying ALP mass

# Collapse of the string-wall network

[Jain, Hagimoto, AL, Amin, arXiv:2208.08391]

Axion strings become connected together by domain walls

... the string-wall network collapses (for  $N_{dw} = 1$ )



let's consider:  $\begin{cases} m_a \lesssim 3H_{\text{CMB}} \simeq 3 \times 10^{-29} \text{ eV} & \text{(string network survives until after recombination)} \\ m_a \gtrsim 3H_0 \simeq 5 \times 10^{-33} \text{ eV} & \text{(string network collapses before today)} \end{cases}$

# Impact on birefringence

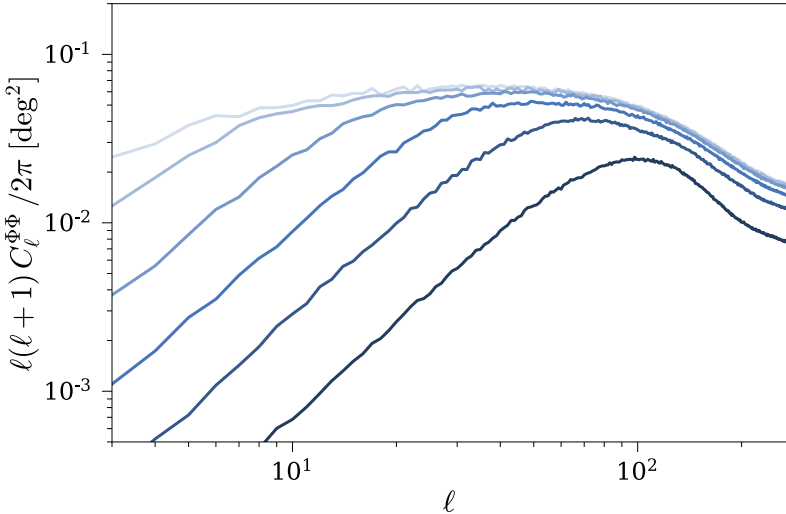
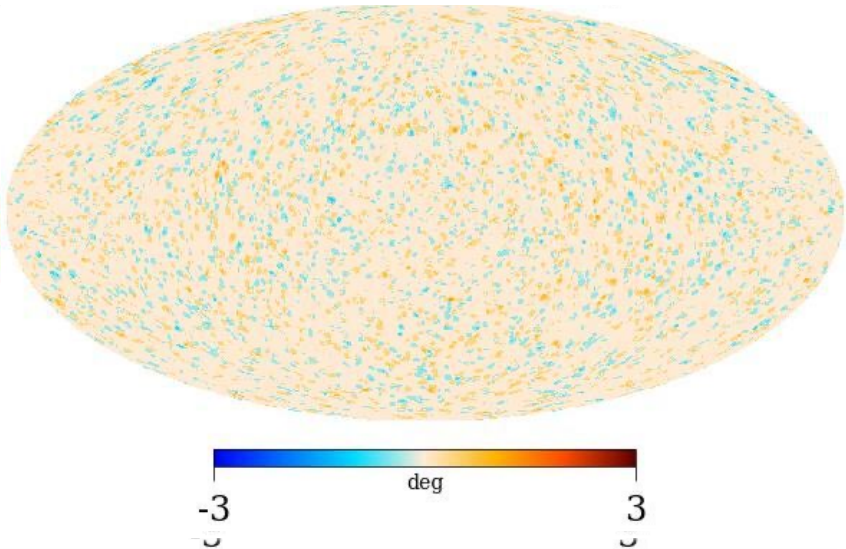
(assuming  $N_{\text{DW}} = 1$ )

raise the ALP mass  
(network collapses earlier)

[Jain, Hagimoto, AL, Amin, arXiv:2208.08391]

see also: [Ferreira, Gasparotto, Hiramatsu, Obata, & Pujolas (2023)]

$$m_a = 2 \times 10^{-29} \text{ eV} \quad (z_c = 404)$$



**strong scale dependence → possible to measure  $m_a$**

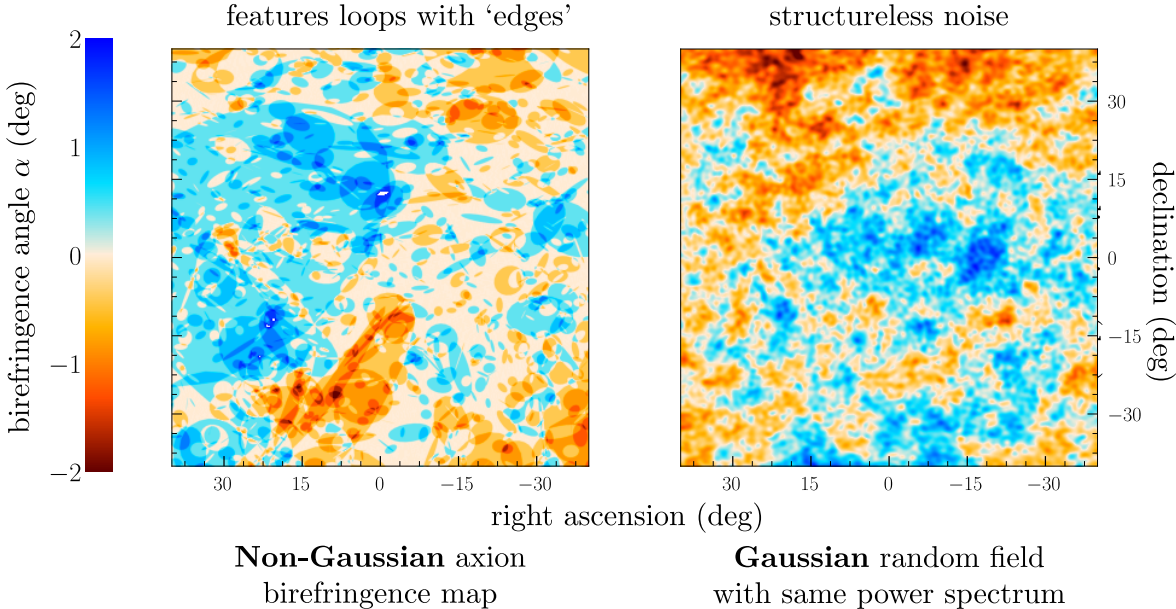
signatures of  
non-Gaussianity



# Birefringence non-Gaussianity

[Hagimoto & AL, arXiv:2306.07351]  
see also: Yin, Dai, Ferraro (2305.02318)

axion-string induced birefringence:  
loop-like features are visibly non-Gaussian



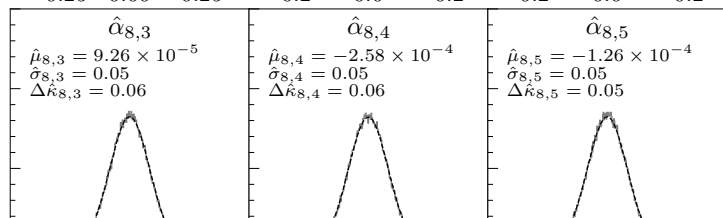
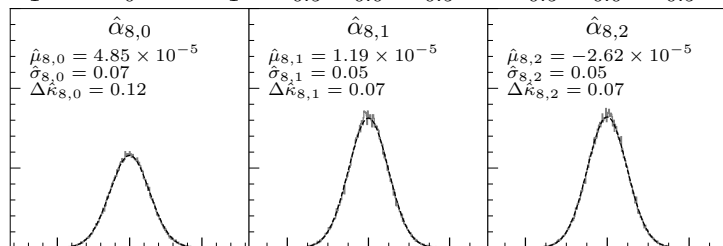
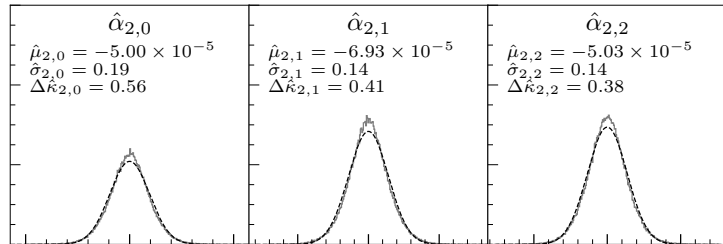
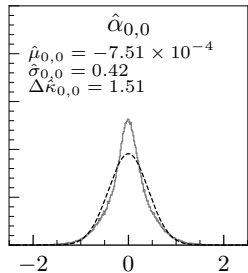
How to best quantify the non-Gaussian birefringence and develop tests to extract these features from the data?

# Measures of NG 1: kurtosis

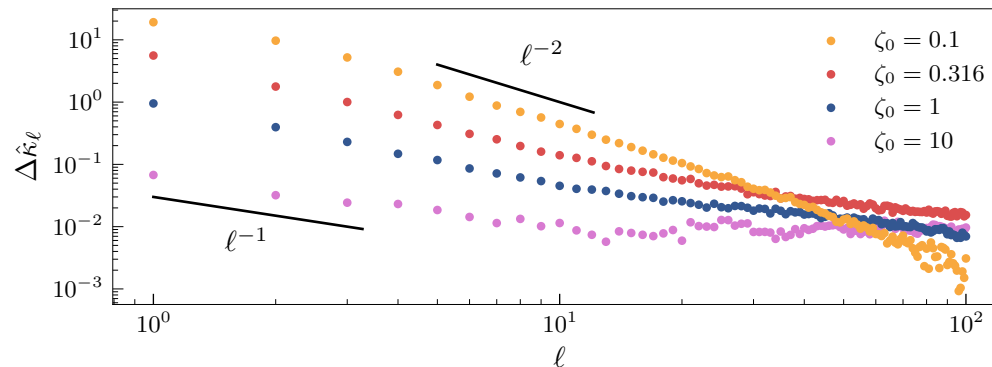
distribution over  $\hat{a}_{\ell m}$ 's  
less Gaussian at lower  $\ell$

kurtosis  
a measure of Gaussianity

$$\kappa_{\ell m} = \frac{\langle |\hat{a}_{\ell m} - \langle \hat{a}_{\ell m} \rangle|^4 \rangle}{\langle |\hat{a}_{\ell m} - \langle \hat{a}_{\ell m} \rangle|^2 \rangle^2} = 3 \text{ for Gaussian}$$



scaling with multipole index  
more Gaussian on smaller scales



analytical model  
~ inverse with # loops

$$\Delta \hat{\kappa}_\ell \sim \frac{\zeta_0}{8\xi_0} \left( 1 + \frac{\pi}{\lambda \zeta_0 \ell} \right)^2$$

recall:  $R(t) = \zeta_0/H(t)$

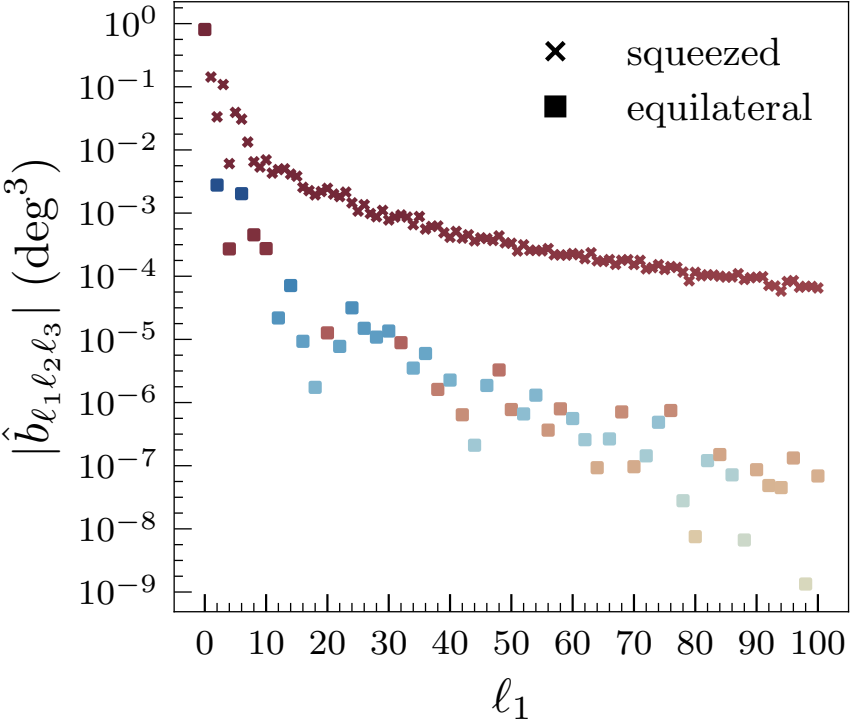
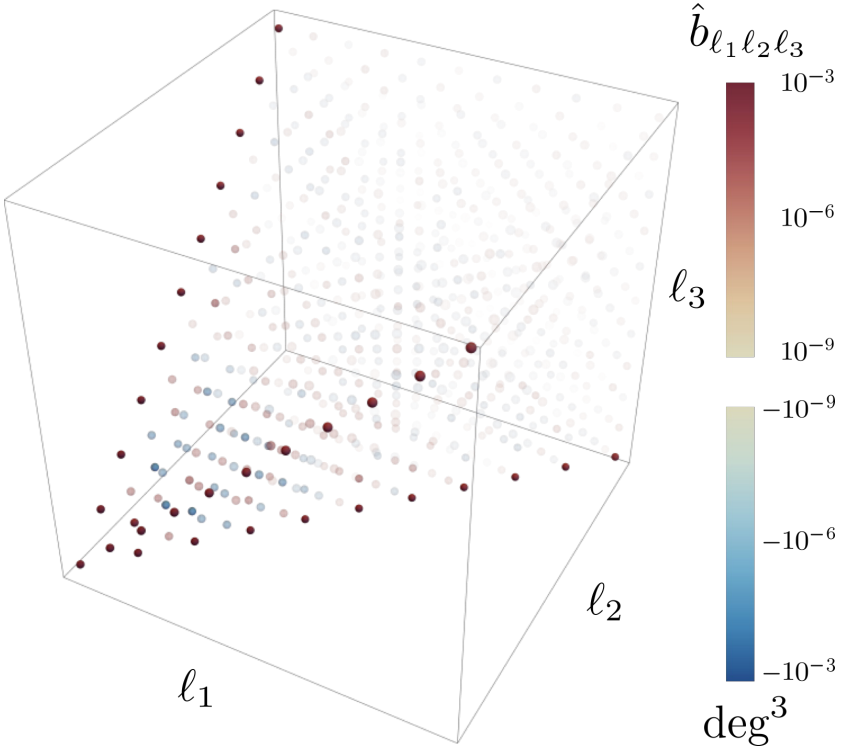
# Measures of NG 2: bispectrum

[Hagimoto & AL, arXiv:2306.07351]

bispectrum  
3-point correlations

$$\hat{b}_{\ell_1 \ell_2 \ell_3} = h_{\ell_1 \ell_2 \ell_3}^{-1} \sum_{m_1=-\ell_1}^{\ell_1} \sum_{m_2=-\ell_2}^{\ell_2} \sum_{m_3=-\ell_3}^{\ell_3} \begin{pmatrix} \ell_1 & \ell_2 & \ell_3 \\ m_1 & m_2 & m_3 \end{pmatrix} \hat{\alpha}_{\ell_1 m_1} \hat{\alpha}_{\ell_2 m_2} \hat{\alpha}_{\ell_3 m_3}$$

single realization  
largest in squeezed triangle form



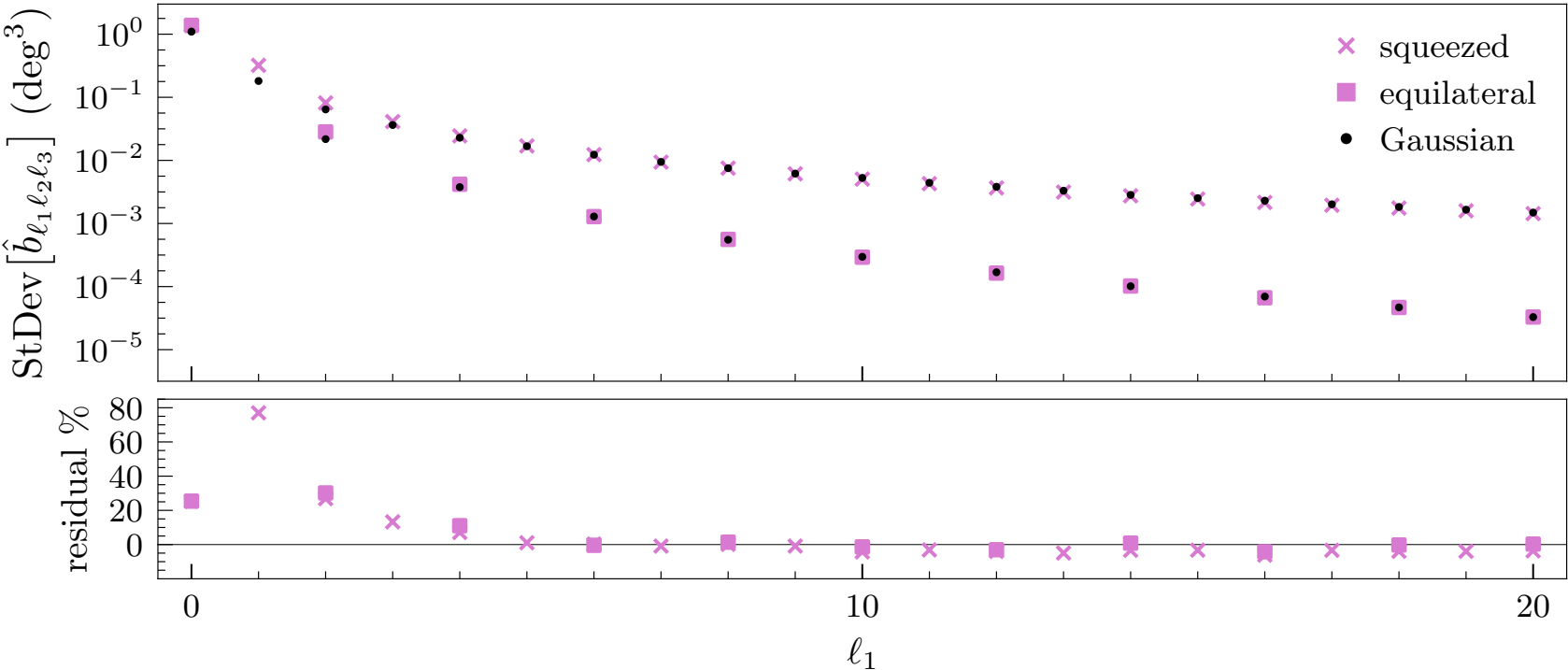
# Measures of NG 2: bispectrum

[Hagimoto & AL, arXiv:2306:07351]

bispectrum  
3-point correlations

$$\hat{b}_{\ell_1 \ell_2 \ell_3} = h_{\ell_1 \ell_2 \ell_3}^{-1} \sum_{m_1=-\ell_1}^{\ell_1} \sum_{m_2=-\ell_2}^{\ell_2} \sum_{m_3=-\ell_3}^{\ell_3} \begin{pmatrix} \ell_1 & \ell_2 & \ell_3 \\ m_1 & m_2 & m_3 \end{pmatrix} \hat{\alpha}_{\ell_1 m_1} \hat{\alpha}_{\ell_2 m_2} \hat{\alpha}_{\ell_3 m_3}$$

average bispectrum  
and comparison with Gaussian random field



# Measures of NG 3: scattering transform

Yin, Dai, Ferraro (2023)

std. method  
power spectrum

signal:  $I_0(\mathbf{x})$   
 plane wave:  $\phi_{\mathbf{k}}(\mathbf{x})$   
 $P_{\mathbf{k}}(\mathbf{x}) = \langle |I_0 * \phi_{\mathbf{k}}|^2 \rangle(\mathbf{x})$

new method  
scattering transform

wavelet:  $\psi^{j,l}(\mathbf{x})$

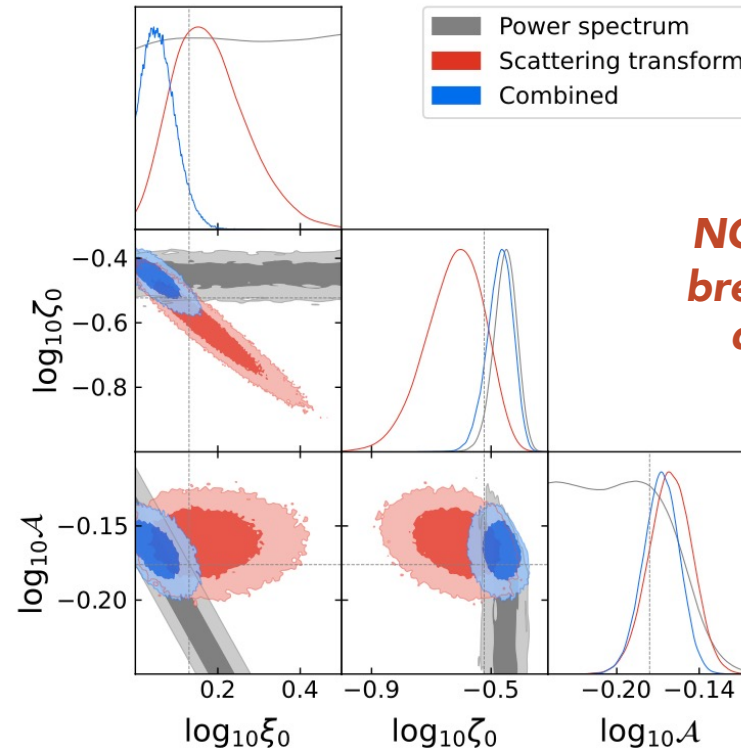
$$I_1^{j,l}(\mathbf{x}) = \langle |I_0 * \psi^{j,l}|^2 \rangle(\mathbf{x})$$

$$I_2^{j_1,l_1,j_2,l_2}(\mathbf{x}) = \langle |I_1^{j_1,l_1} * \psi^{j_2,l_2}|^2 \rangle(\mathbf{x})$$

$$s_1^j = \langle I_1^{j,l} \rangle_{\mathbf{x},l}$$

$$s_2^{j_1,j_2} = \langle I_2^{j_1,l_1,j_2,l_2} \rangle_{\mathbf{x},l_1,l_2}$$

comparison  
pow-spec vs. scatt-transform



**NG information  
breaks the  $A^2 \xi_0$   
degeneracy**

(b)  $A^2 \xi_0 = 0.6$ ,  $A = 2/3$ ,  $\zeta_0 = 0.3$

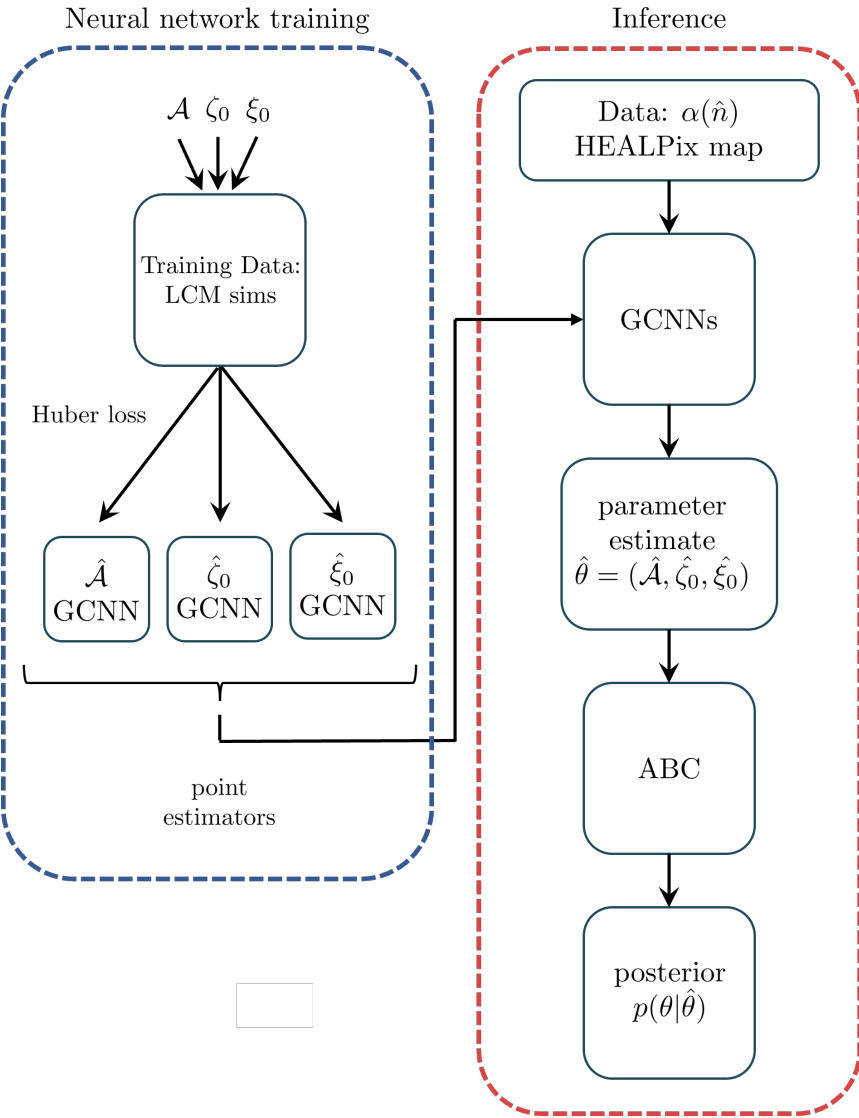


machine learning  
for axion string identification

# Machine learning for axion strings

--- early stages ---

goal: to train an AI to identify features of axion strings in CMB polarization maps



Ray Hagimoto (Rice U grad)

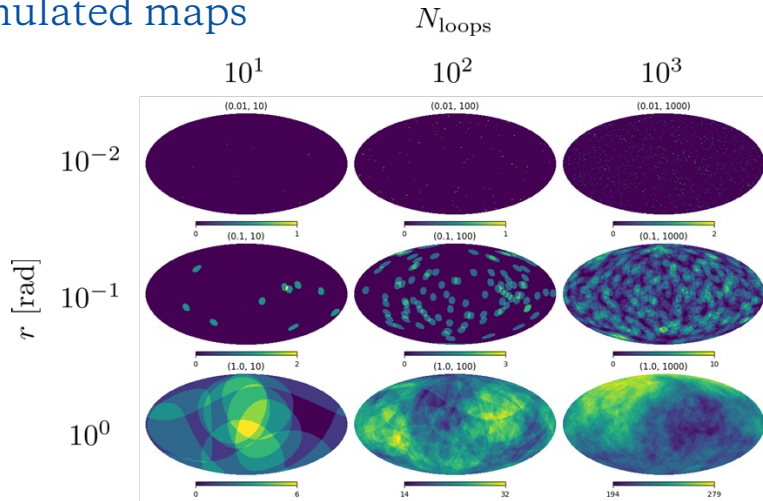
# Machine learning for axion strings

--- early stages ---

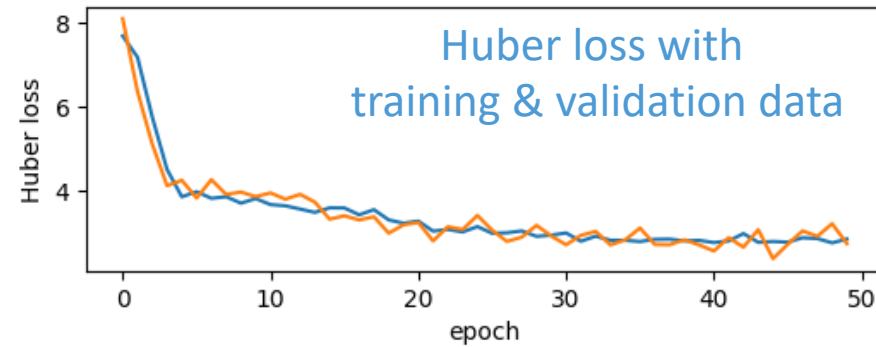


Ray Hagimoto  
(Rice U grad)

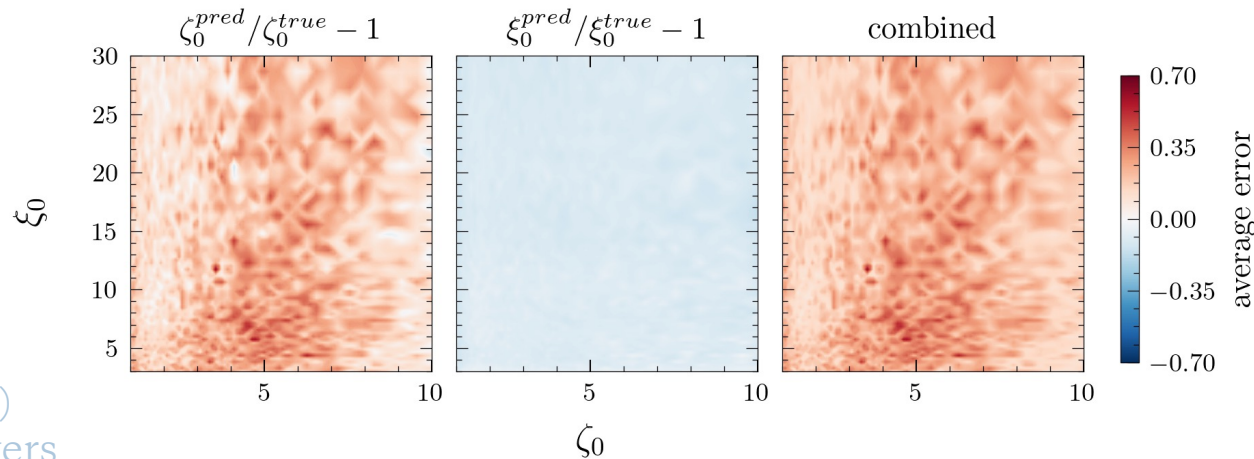
simulated maps



training



how well is it working? ... not bad!



things to do  
& where we're going:

- detector noise
- beyond LCM sims
- real CMB data
- projections

package: DeepSphere (Python)  
architecture: 3 conv + 3 pool layers

what about  
isotropic  
birefringence

# Are strings responsible for isotropic birefringence?

[Jain, Hagimoto, AL, Amin, arXiv:2208.08391]

reported detection of isotropic birefringence:  
same rotation angle across the whole sky  
(using *Planck* & *WMAP* data)

$$\alpha_{00} = -1.21^\circ \pm_{-0.32^\circ}^{+0.33^\circ} \text{ (68\% CL)}$$

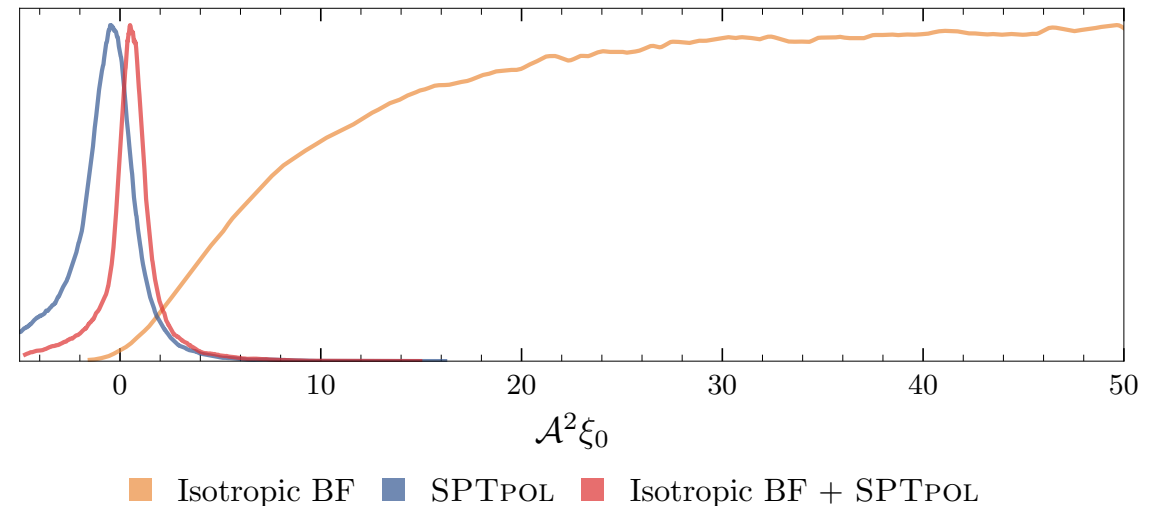
[Minami & Komatsu (2020)]

[Diego-Palazuelos et. al. (2022)]

[Eskilt (2022)], [Eskilt & Komatsu (2022)]

[Eskilt et. al. (2023)]

our conclusion: the isotropic signal is in tension  
with limits on anisotropic BF if they both arise  
from axion-string induced birefringence



note that:  $\beta = -\alpha_{00}/\sqrt{4\pi} \approx 0.34^\circ$



# Are strings responsible for isotropic birefringence?

[Ferreira, Gasparotto, Hiramatsu, Obata, & Pujolas (2023)]

reported detection of isotropic birefringence:  
same rotation angle across the whole sky  
(using *Planck* & *WMAP* data)

$$\alpha_{00} = -1.21^{\circ} {}^{+0.33^{\circ}}_{-0.32^{\circ}} \text{ (68\% CL)}$$

[Minami & Komatsu (2020)]

[Diego-Palazuelos et. al. (2022)]

[Eskilt (2022)], [Eskilt & Komatsu (2022)]

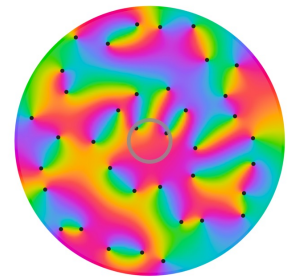
[Eskilt et. al. (2023)]

loopholes allowing large iso-BF

(1) environmental effects  
a nearby loop in our Hubble volume  
would dominate the isotropic signal

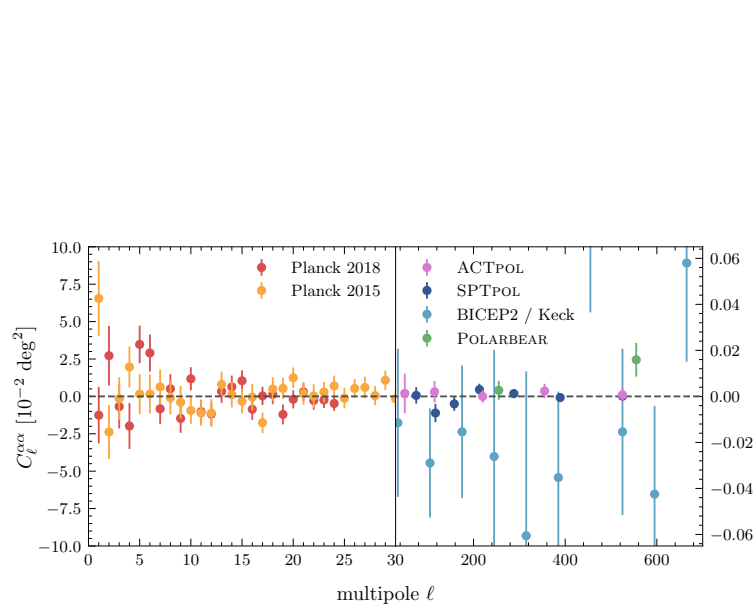
(2) Hubble-scale gradients  
the massless axion field is expected to be  
inhomogeneous on the Hubble scale

(3) late-forming network  
if the string network is not present just after  
recombination, the small-scale BF is suppressed

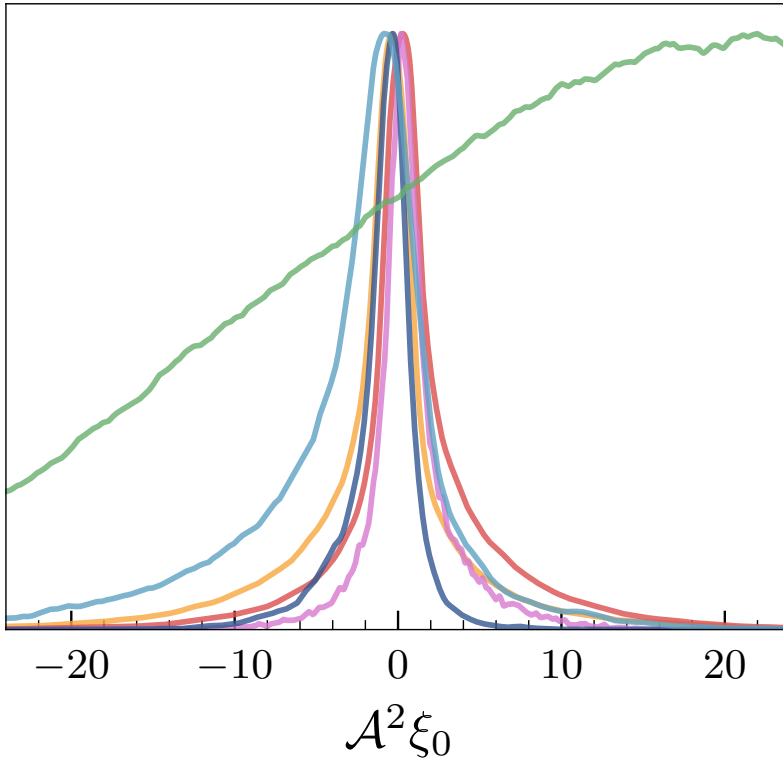


note that:  $\beta = -\alpha_{00}/\sqrt{4\pi} \approx 0.34^{\circ}$

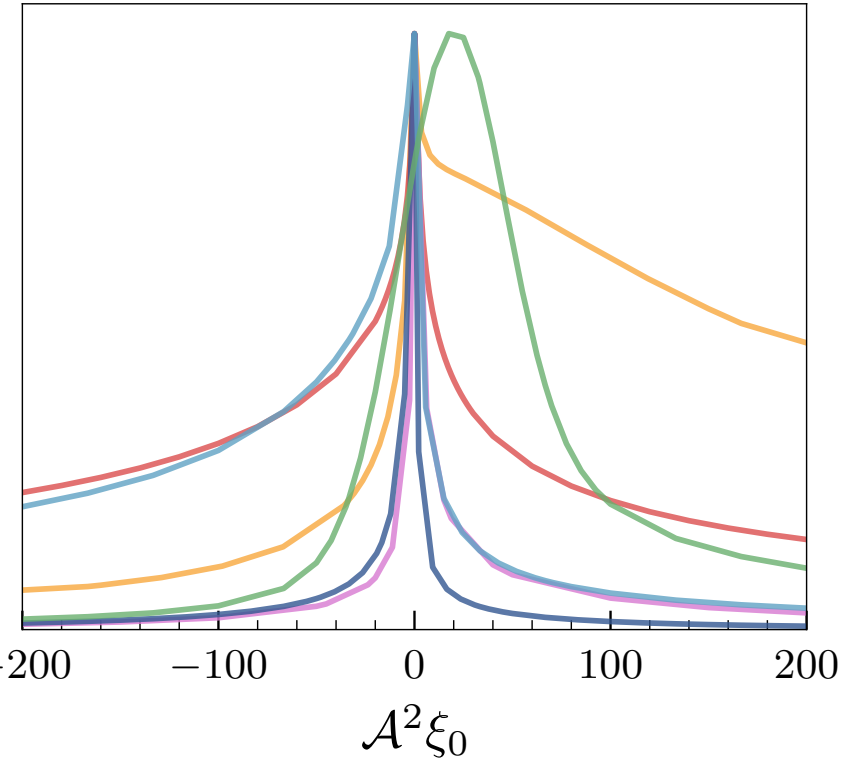
# Constraints from anisotropic birefringence



stable string network



collapsing string-wall network



■ Planck 2015  
 ■ Planck 2018  
 ■ ACTPOL  
 ■ SPTPOL  
 ■ BICEP2 / Keck  
 ■ POLARBEAR