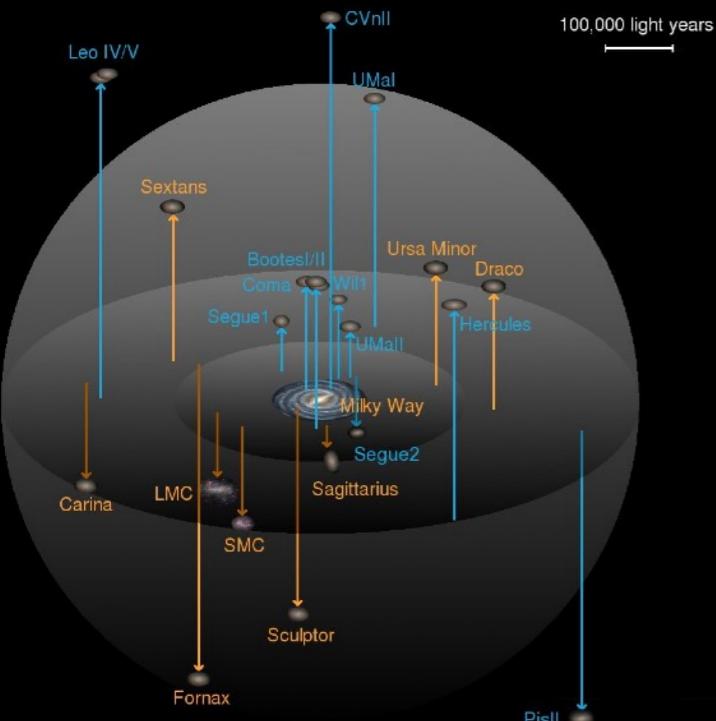


# Tidal Stripping of SIDM Halos

Kimberly Boddy  
Johns Hopkins University

# Small-Scale Structure

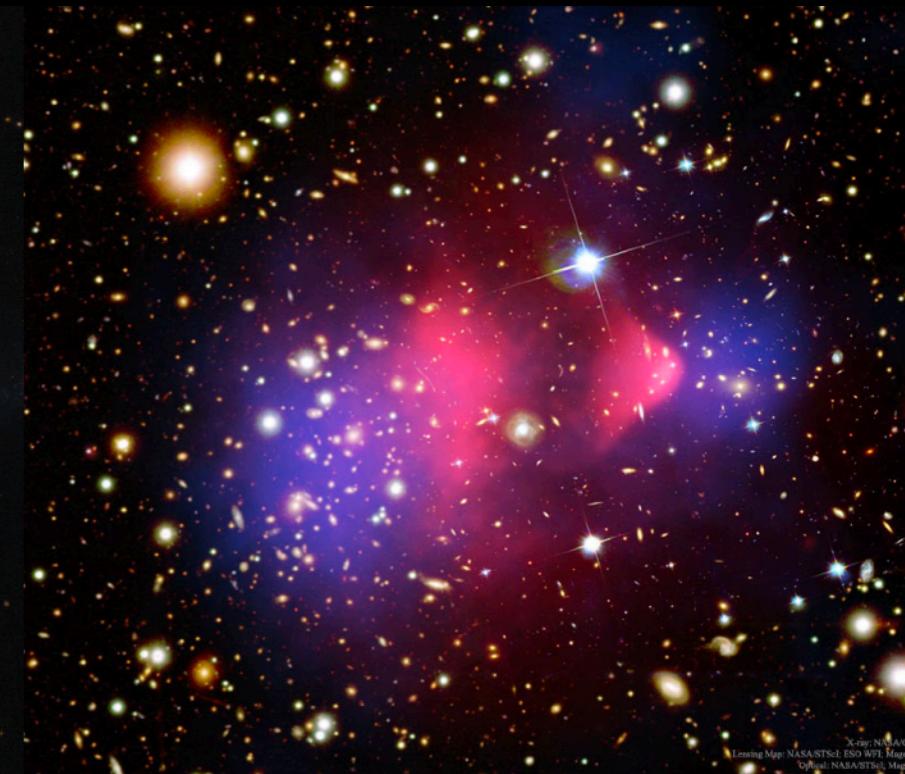
Dwarf spheroidals



LSBs



Galaxy Clusters



**small-scale structure puzzles arise in various systems:  
core-cusp, missing satellites, too-big-to-fail, diversity**

# SIDM Solution

Alleviate tensions?

*Spergel and Steinhardt, PRL (2000)*

*Rocha+, MNRAS (2013)*

*Zavala+, MNRAS (2013)*

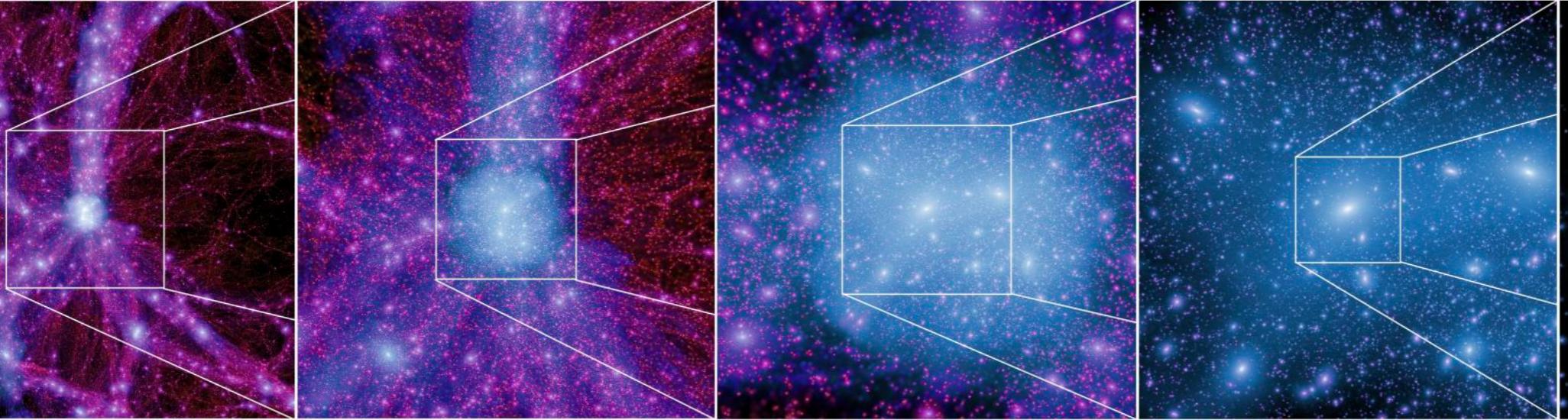
Dwarfs

LSBs

Clusters

Further investigations with  
SIDM+baryons are ongoing

Kaplinghat, Tulin, Yu, PRL (2016)



Millennium-II, Boylan-Kolchin+ (2009)

Can we understand SIDM halo evolution  
without needing to run N-body simulations?

Yes! Use semi-analytic methods.  
Gravothermal evolution.

In globular clusters:

- ♦ Lynden-Bell and Eggleton (1980)

In SIDM halos:

- ♦ Balberg, S. Shapiro, Inagaki (2002); Ahn, P. Shapiro (2004); Koda, P. Shapiro (2011)

# Gravothermal Evolution

- Mass conservation

$$\frac{\partial M}{\partial r} = 4\pi r^2 \rho$$

- Hydrostatic equilibrium

$$\frac{\partial(\rho\nu^2)}{\partial r} = -G \frac{M\rho}{r^2}$$

- Laws of thermodynamics

$$\frac{\partial L}{\partial r} = -4\pi r^2 \rho\nu^2 \left( \frac{\partial}{\partial t} \right)_M \ln \left( \frac{\nu^3}{\rho} \right)$$

- Heat conduction

$$\frac{L}{4\pi r^2} = -\kappa \frac{\partial T}{\partial r}$$

Two time scales:

$$t_r = \frac{\lambda_{\text{mfp}}}{a\nu} = \frac{\sigma/m}{a\rho\nu}$$

$$t_d = \frac{H}{\nu} = (4\pi\rho G)^{-1/2}$$

# Gravothermal Evolution

- Mass conservation

$$\frac{\partial M}{\partial r} = 4\pi r^2 \rho$$

- Hydrostatic equilibrium

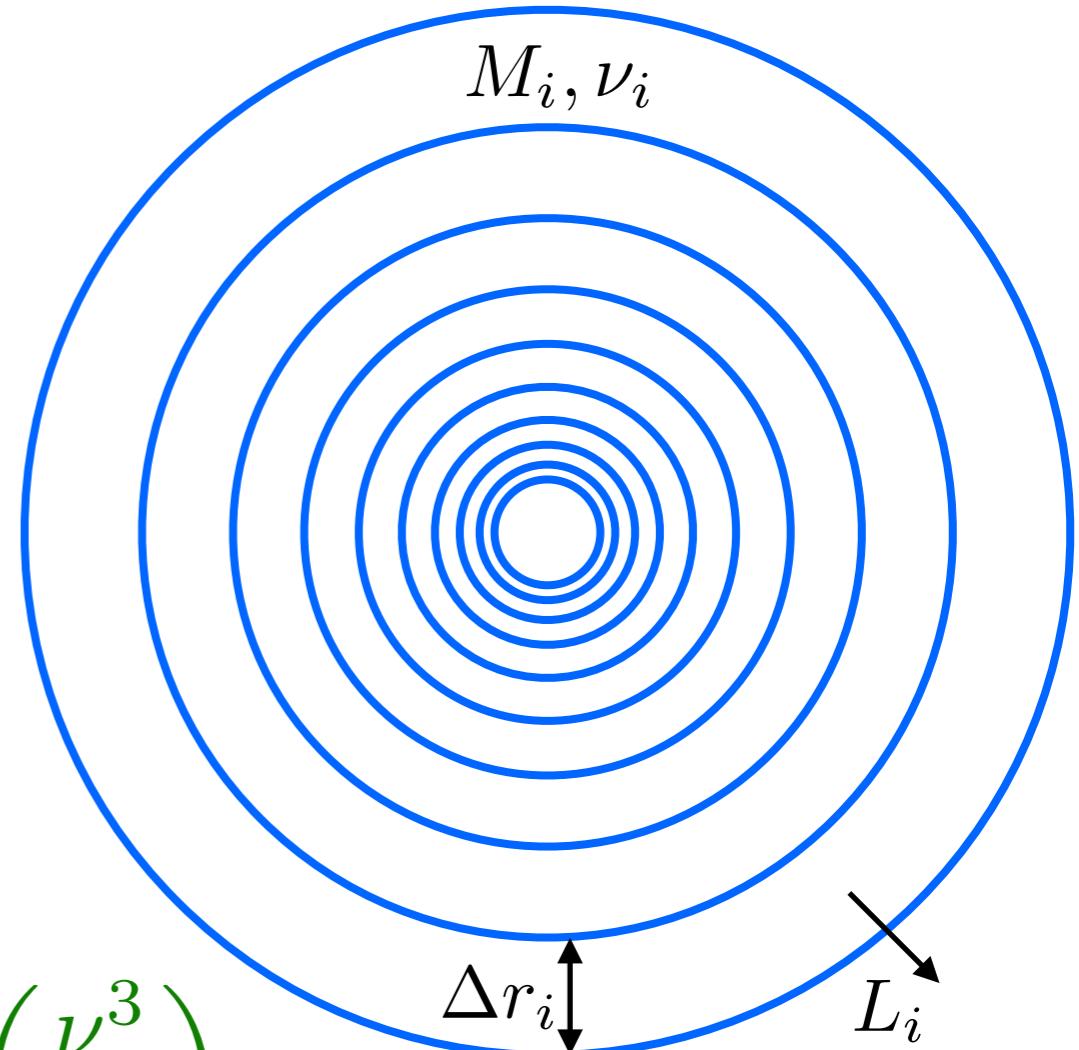
$$\frac{\partial(\rho\nu^2)}{\partial r} = -G \frac{M\rho}{r^2}$$

- Laws of thermodynamics

$$\frac{\partial L}{\partial r} = -4\pi r^2 \rho\nu^2 \left( \frac{\partial}{\partial t} \right)_M \ln \left( \frac{\nu^3}{\rho} \right)$$

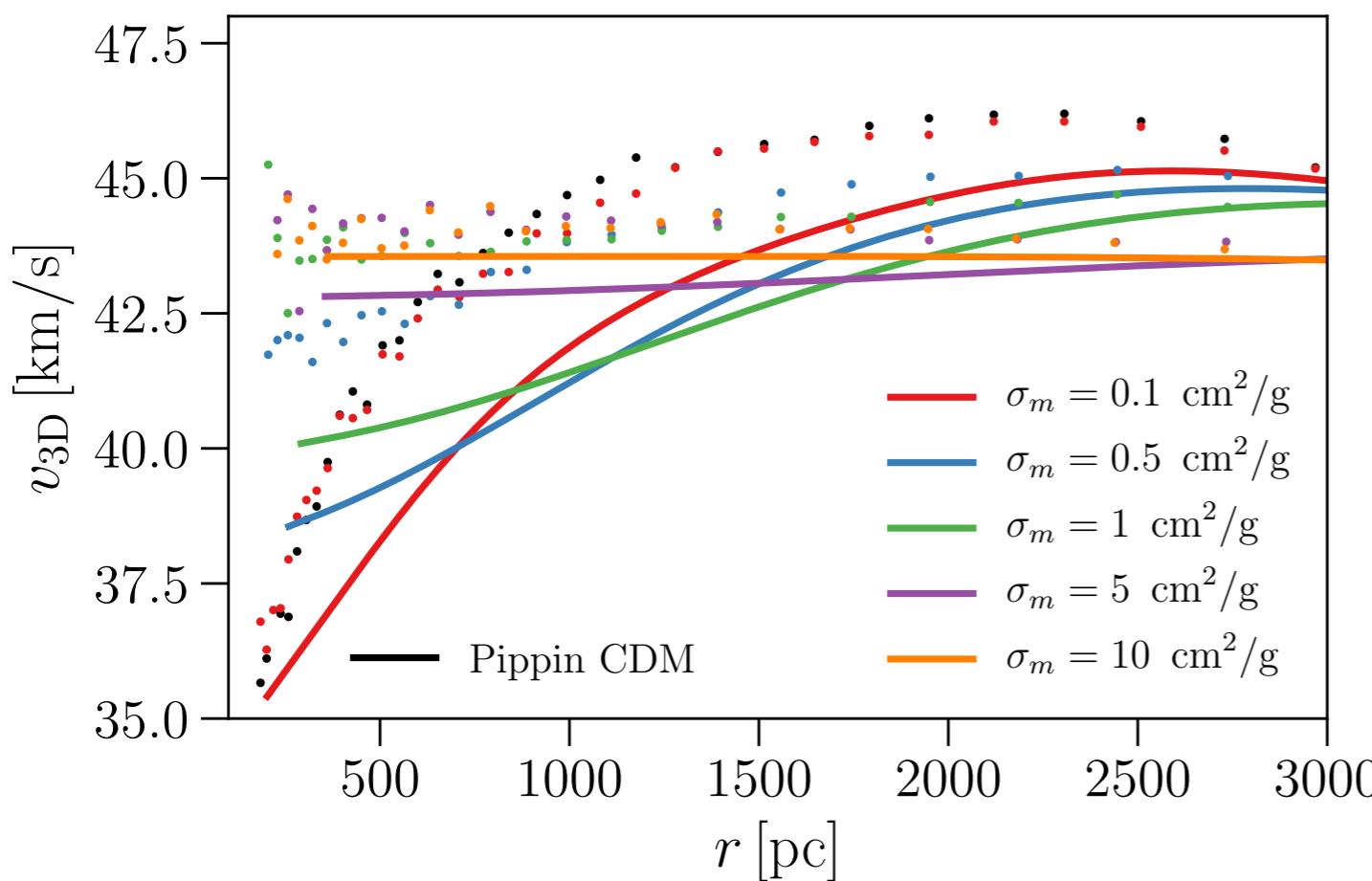
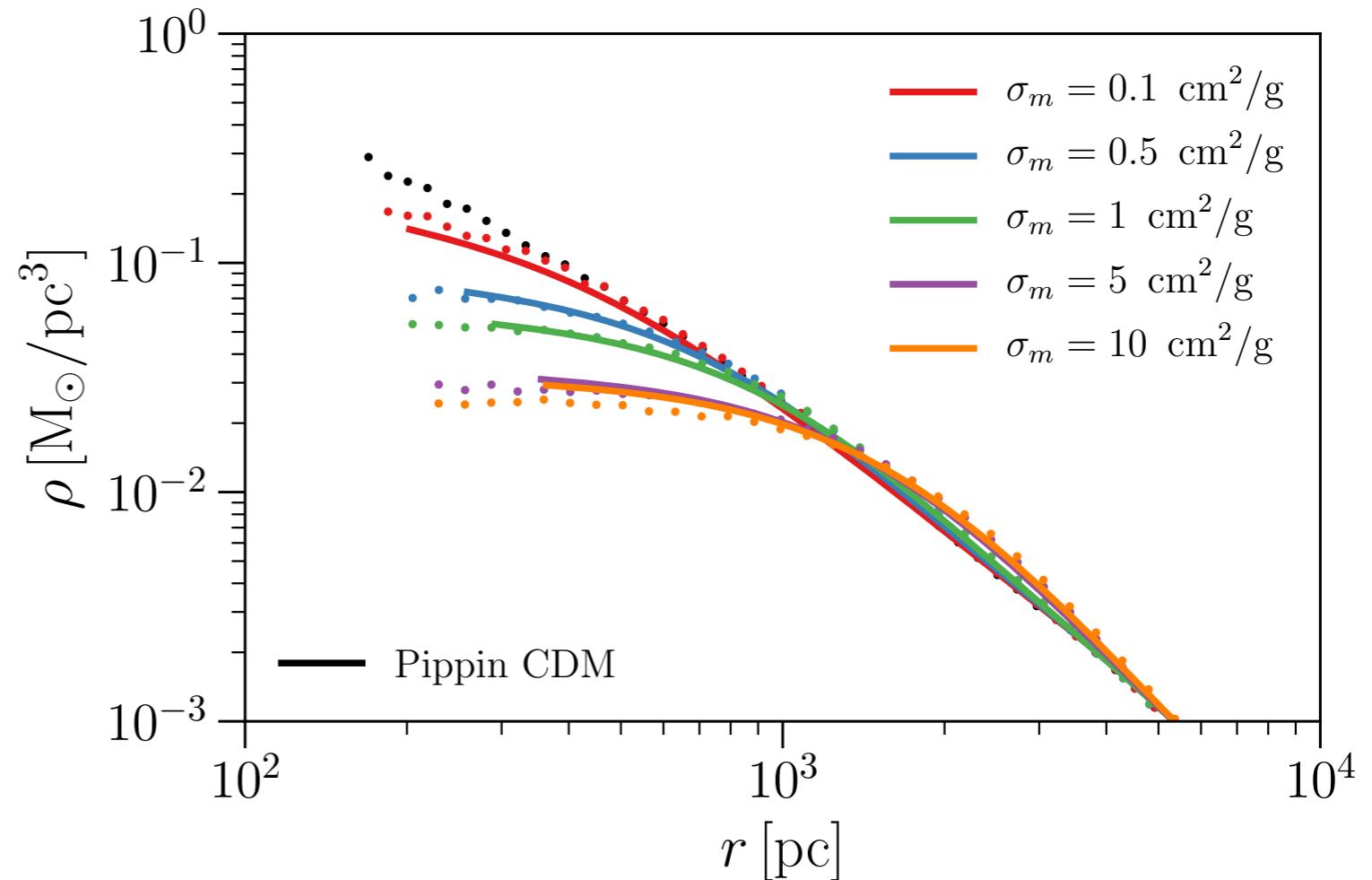
- Heat conduction

$$\frac{L}{4\pi r^2} = -\kappa \frac{\partial T}{\partial r} = -\frac{3}{2} ab\nu \left( \frac{\sigma}{m} \right) \left[ a \left( \frac{\sigma}{m} \right)^2 + \frac{b}{C} \frac{4\pi G}{\rho\nu^2} \right]^{-1} \frac{\partial\nu^2}{\partial r}$$



# Calibration

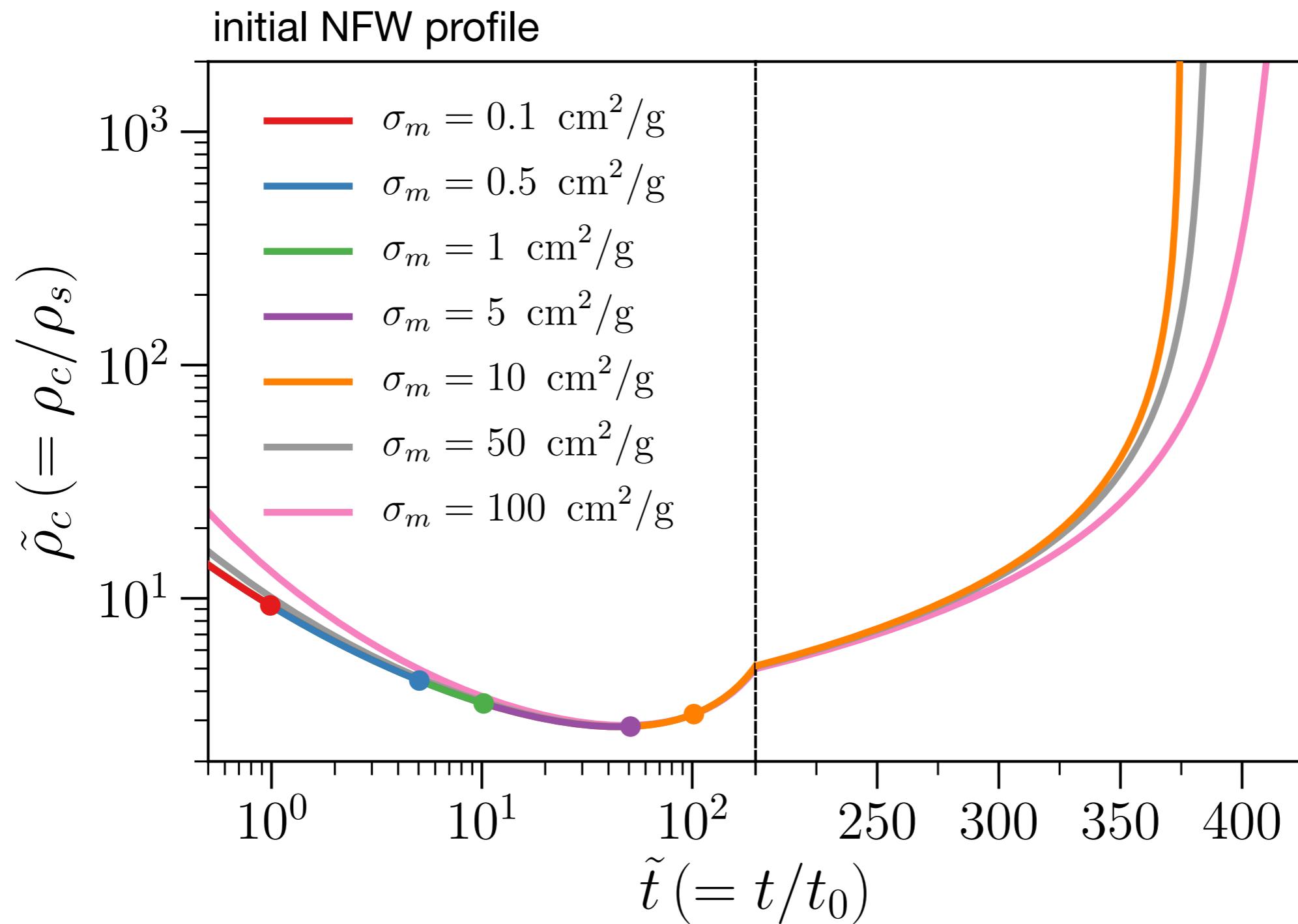
**Matching densities  
works well across a range  
of cross sections**



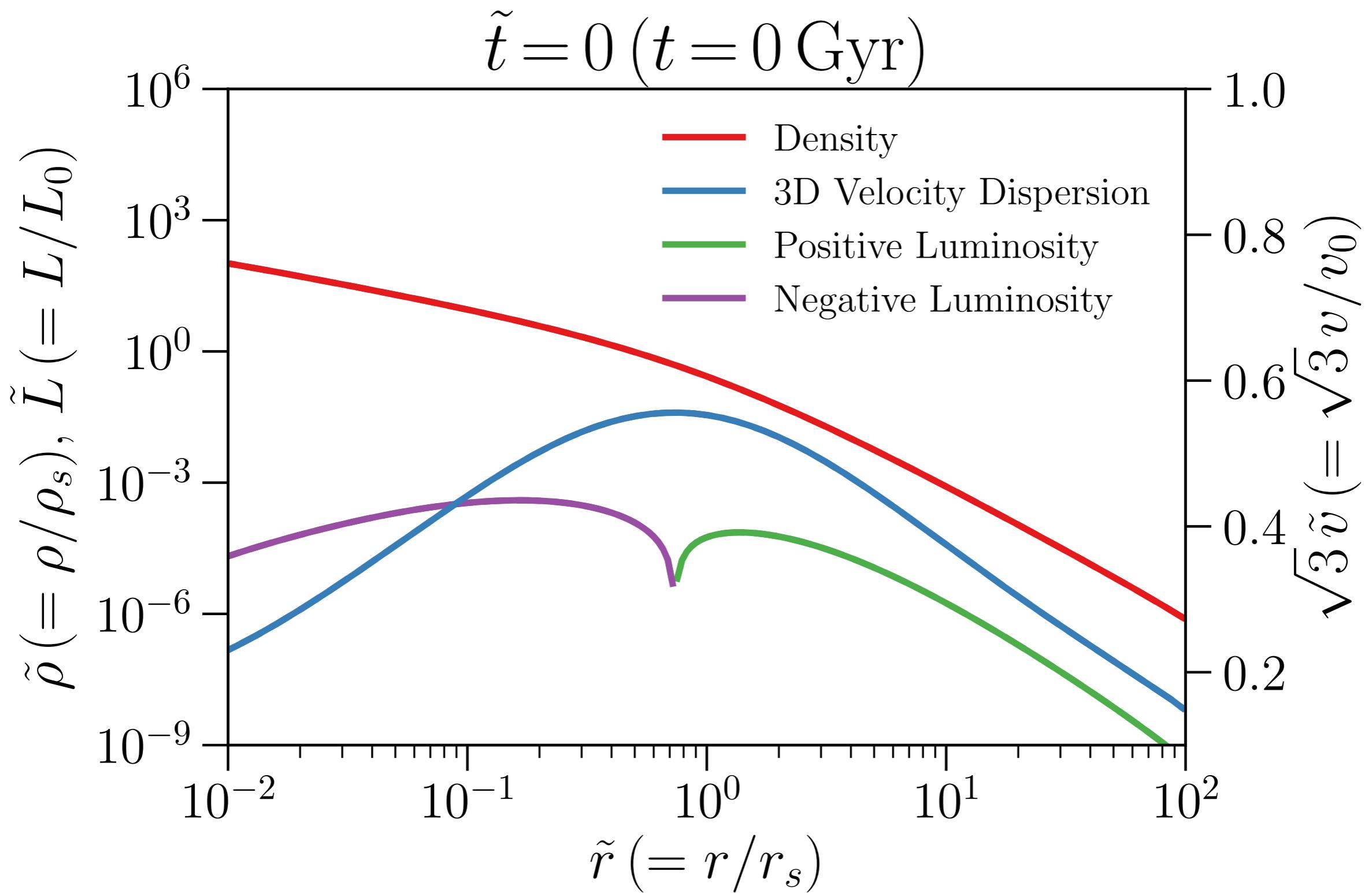
**Matching velocity dispersions  
is more problematic**

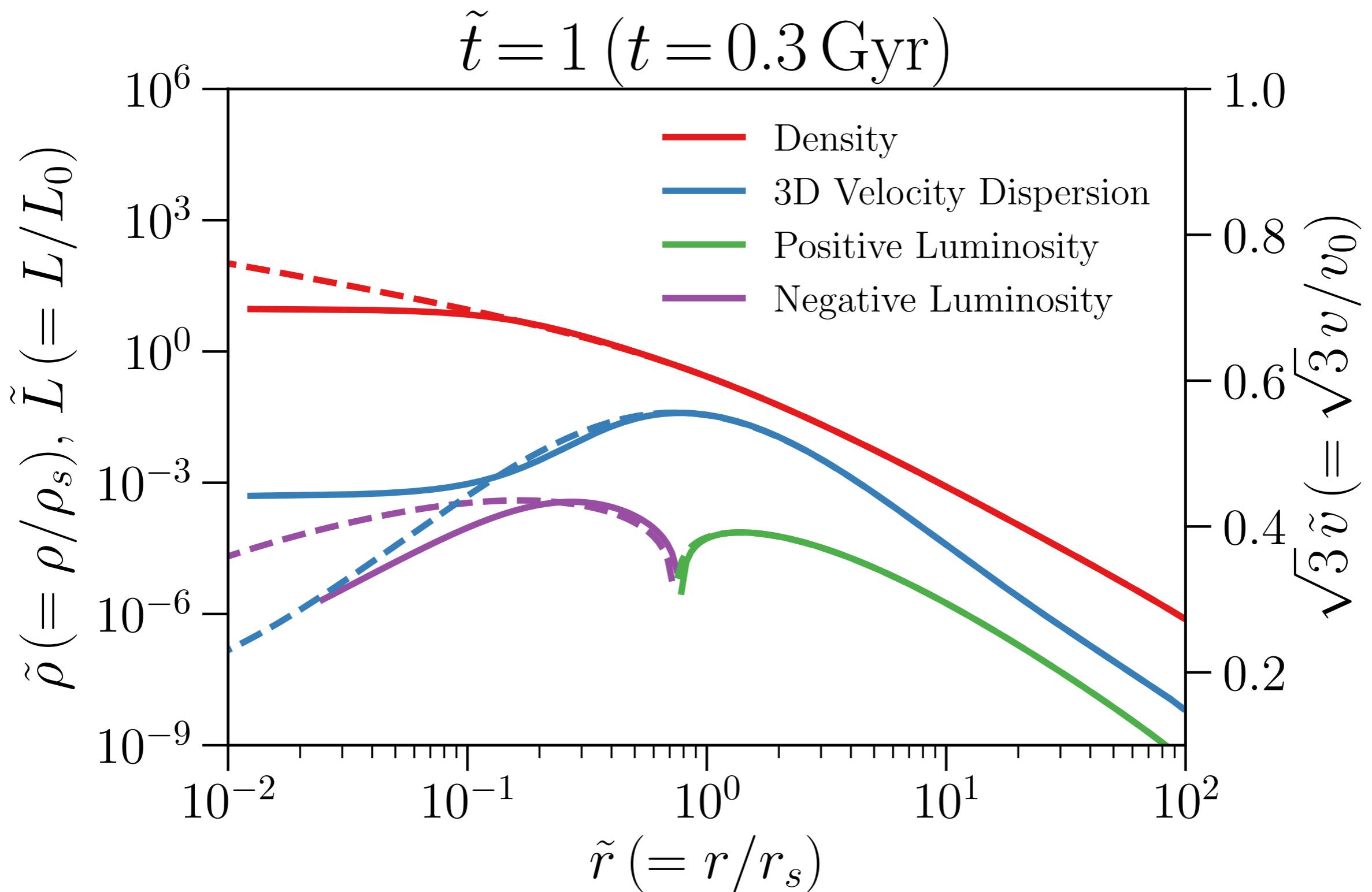
Simulation reference: *Elbert+, MNRAS (2015)*  
*Nishikawa, KB, Kaplinghat (arXiv: 1901.00499)*

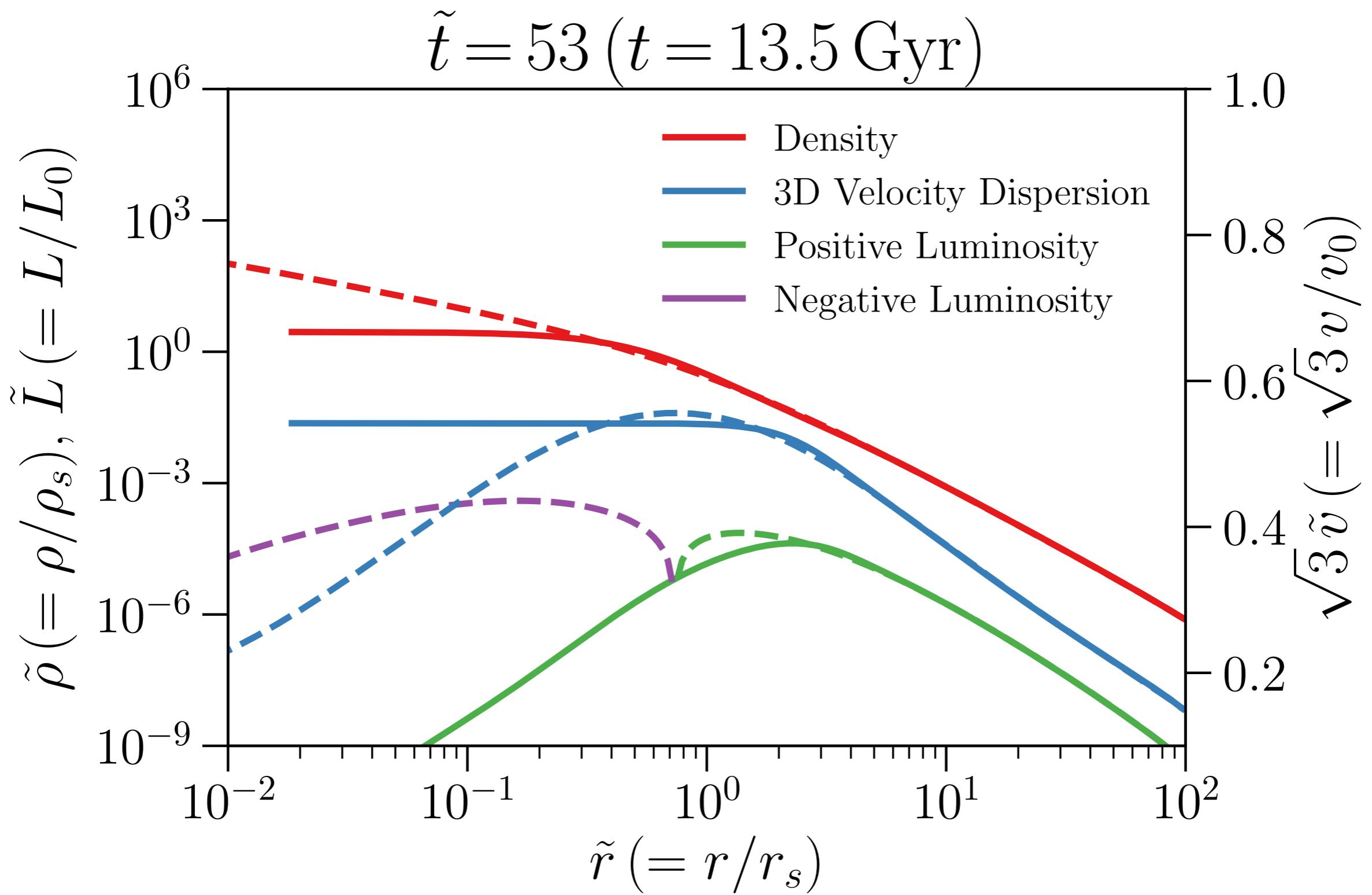
# Central Density

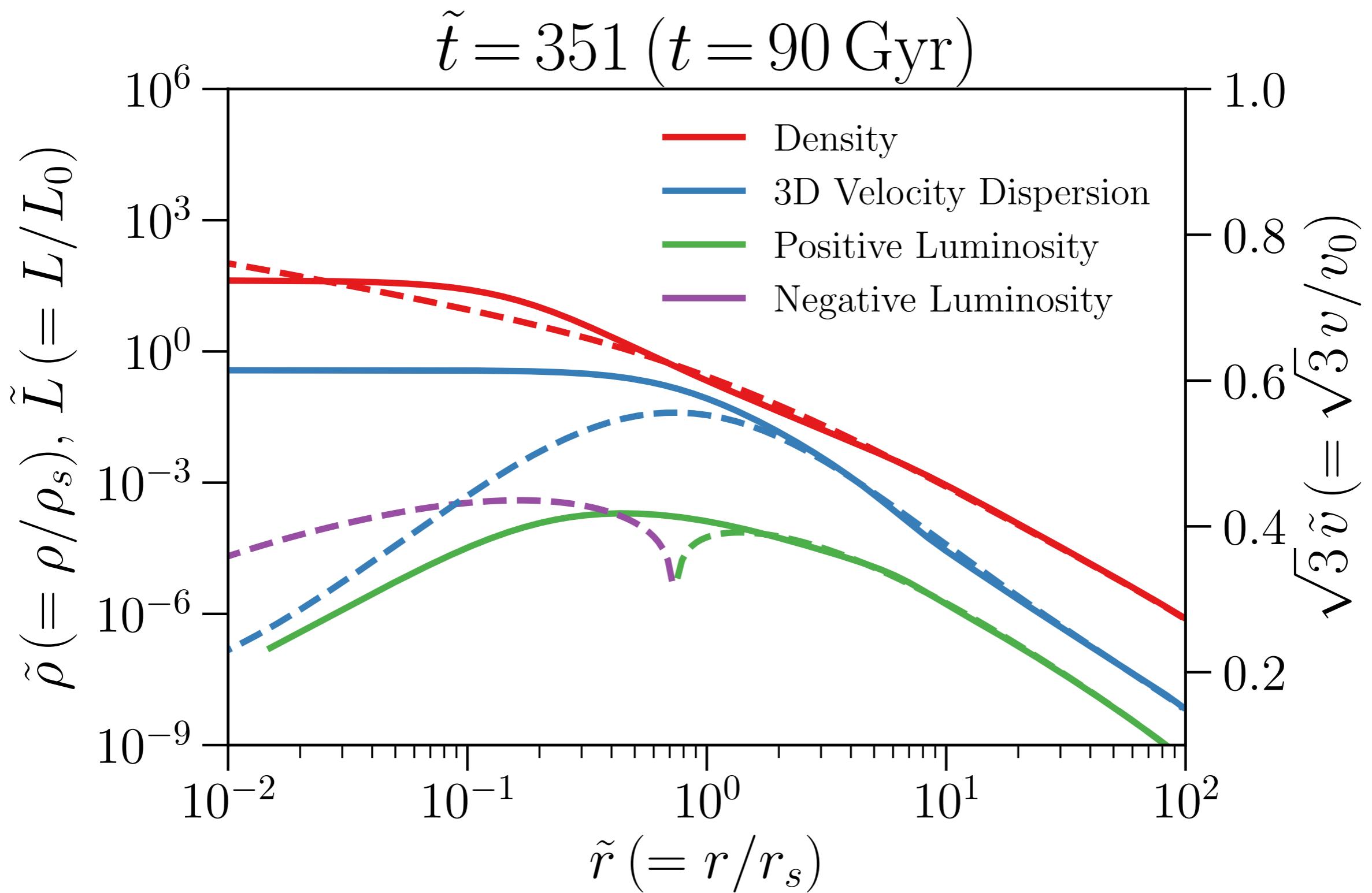


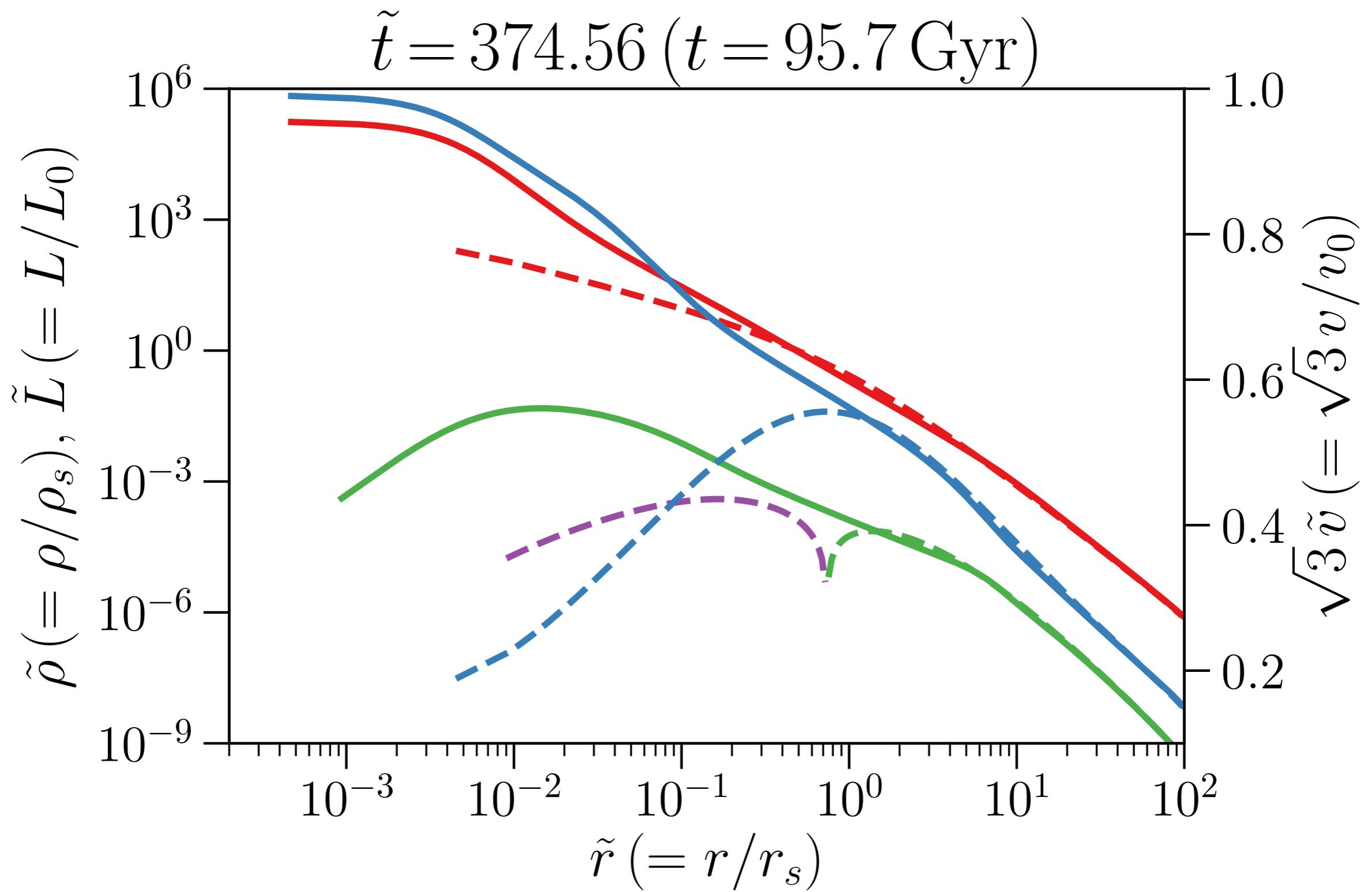
$$t_0^{-1} \sim (\sigma/m) r_s \rho_s^{3/2}$$







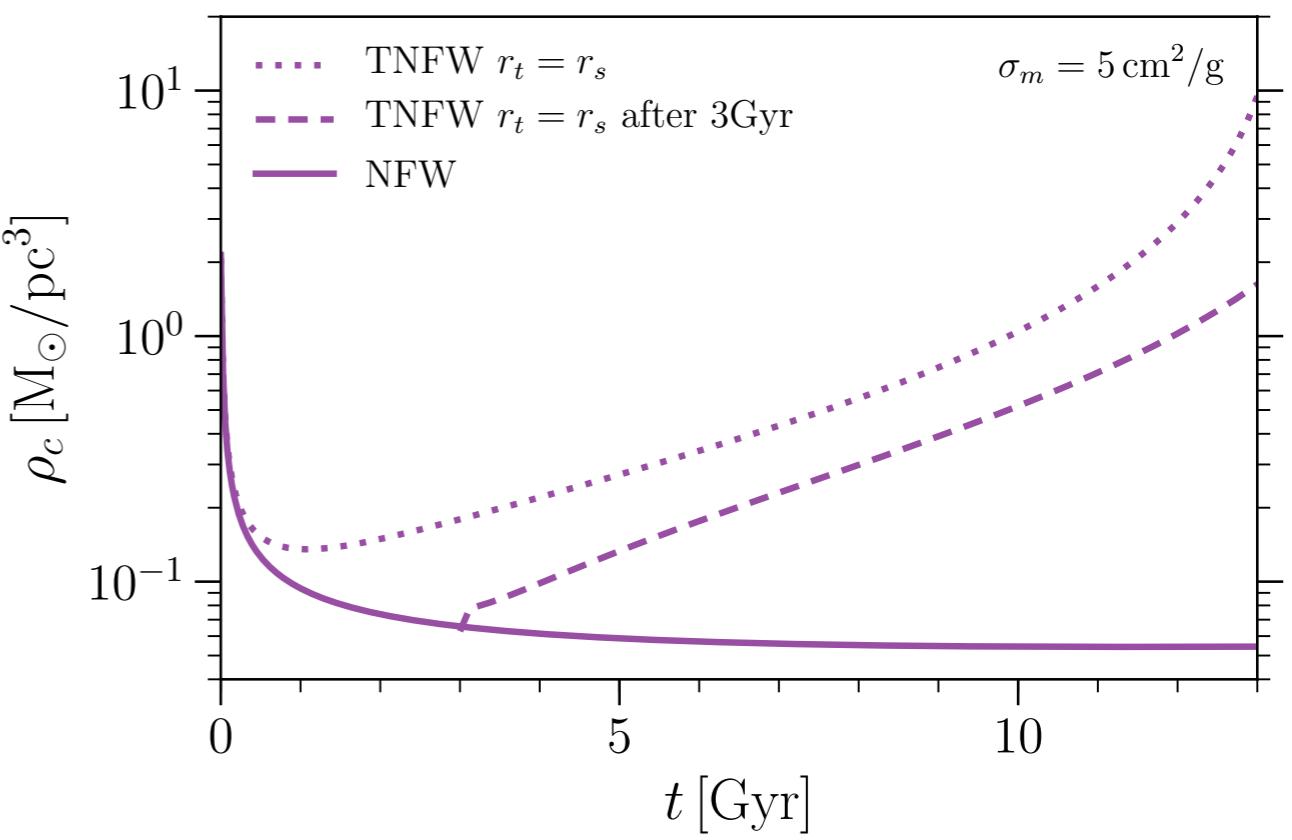
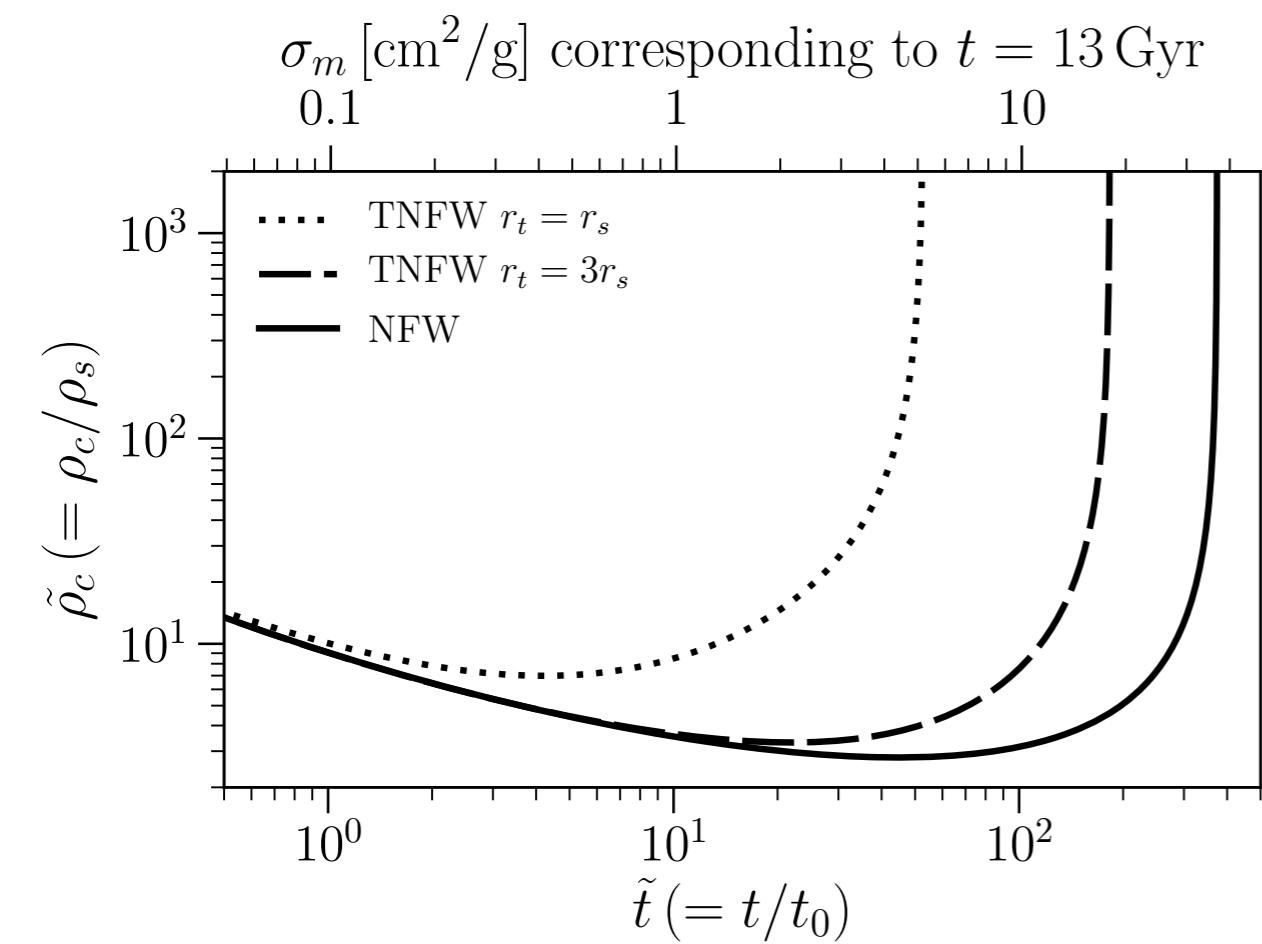




# Tidal Truncation

$$\rho_{\text{NFW}} = \frac{\rho_s}{(r/r_s)[1 + (r/r_s)^2]}$$

$$\rho_{\text{trunc}} = \rho_{\text{NFW}} \times \begin{cases} 1 & r < r_t \\ \frac{1}{(r/r_t)^5} & r > r_t \end{cases}$$

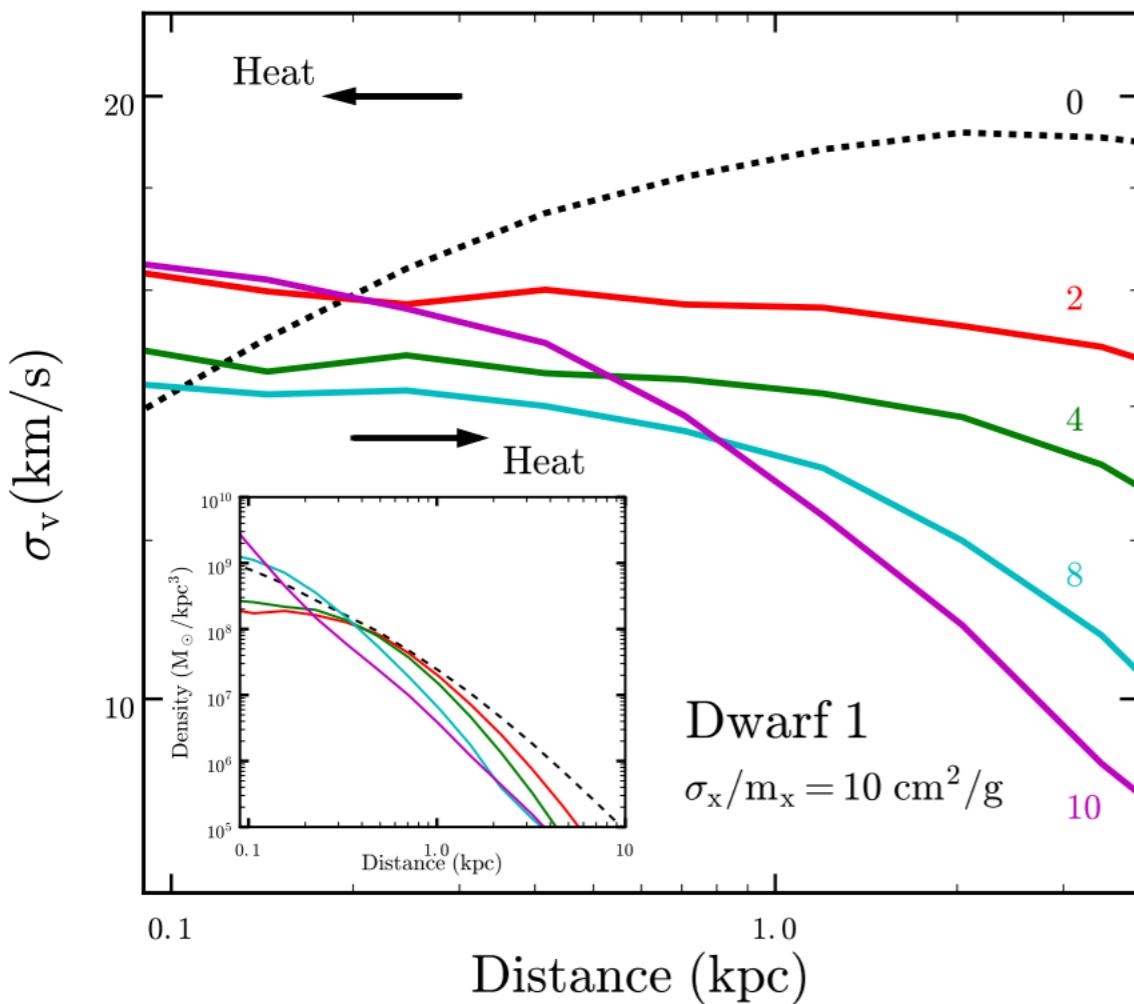


In progress: BH formation

Nishikawa, KB, Kaplinghat (arXiv: 1901.00499)

# Simulations with Infall

Field halos



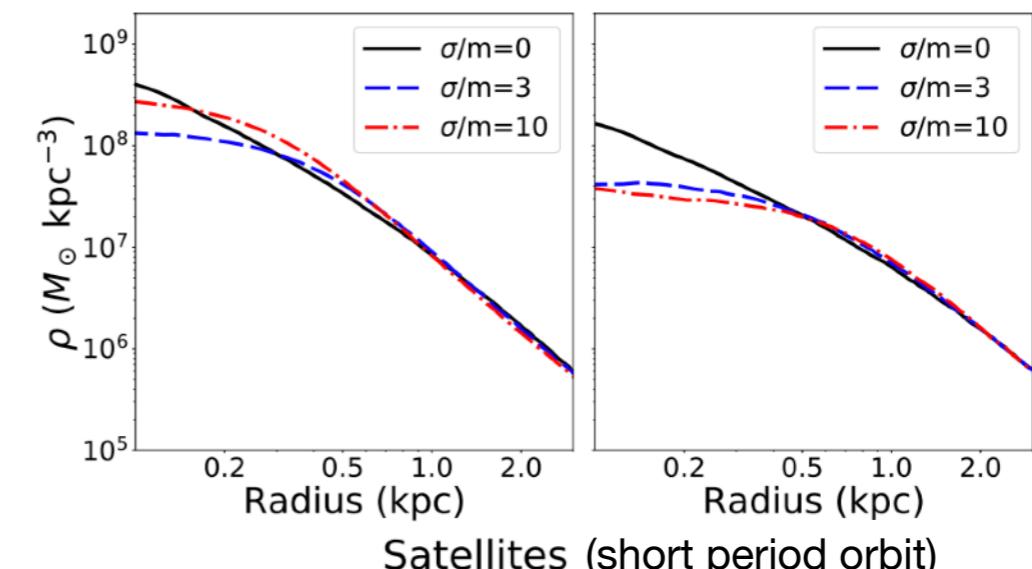
Sameie, Yu, Sales, Vogelsberger, Zavala (1904.07872)

**Can obtain wide diversity of halo profiles (“diversity problem”)**

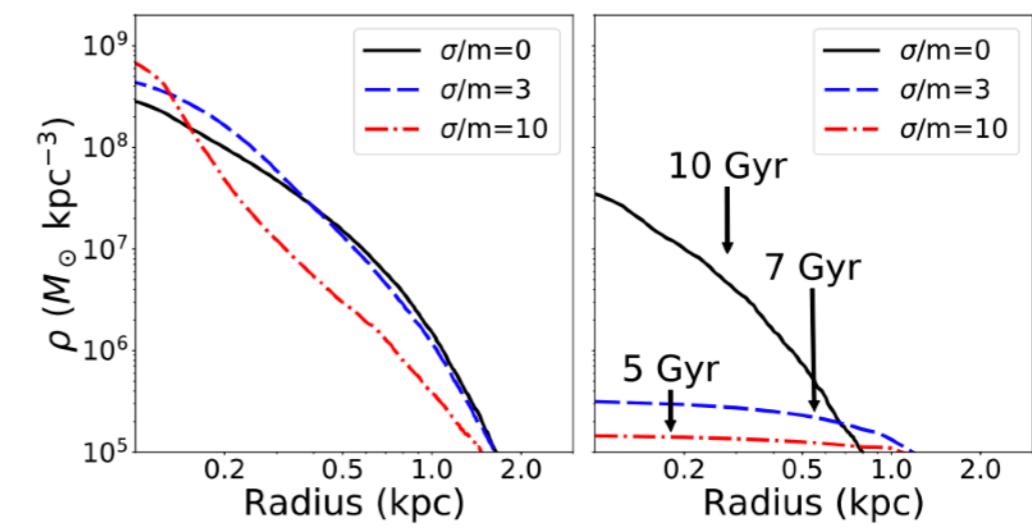
See also:

Zavala, Lovell, Vogelsberger, Burger (1904.09998)

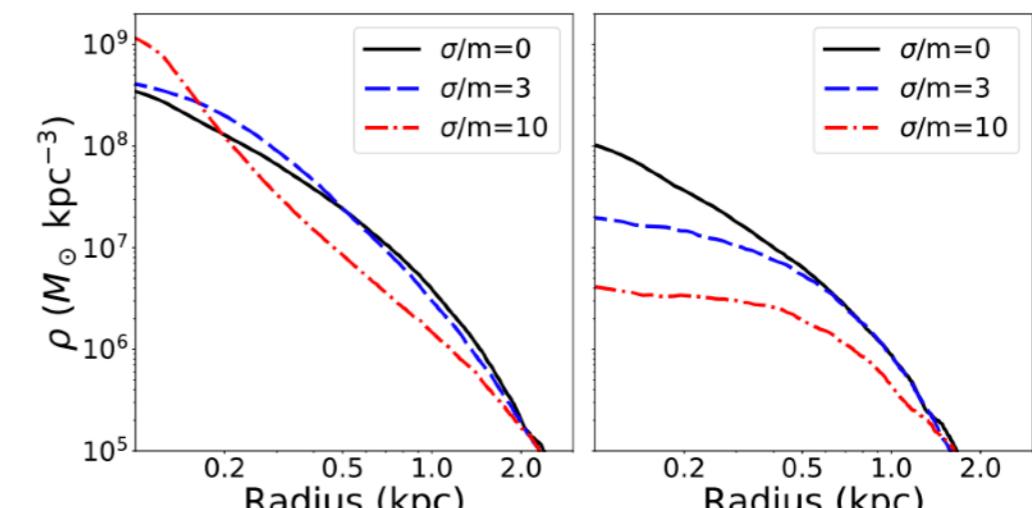
high concentration



Satellites (short period orbit)



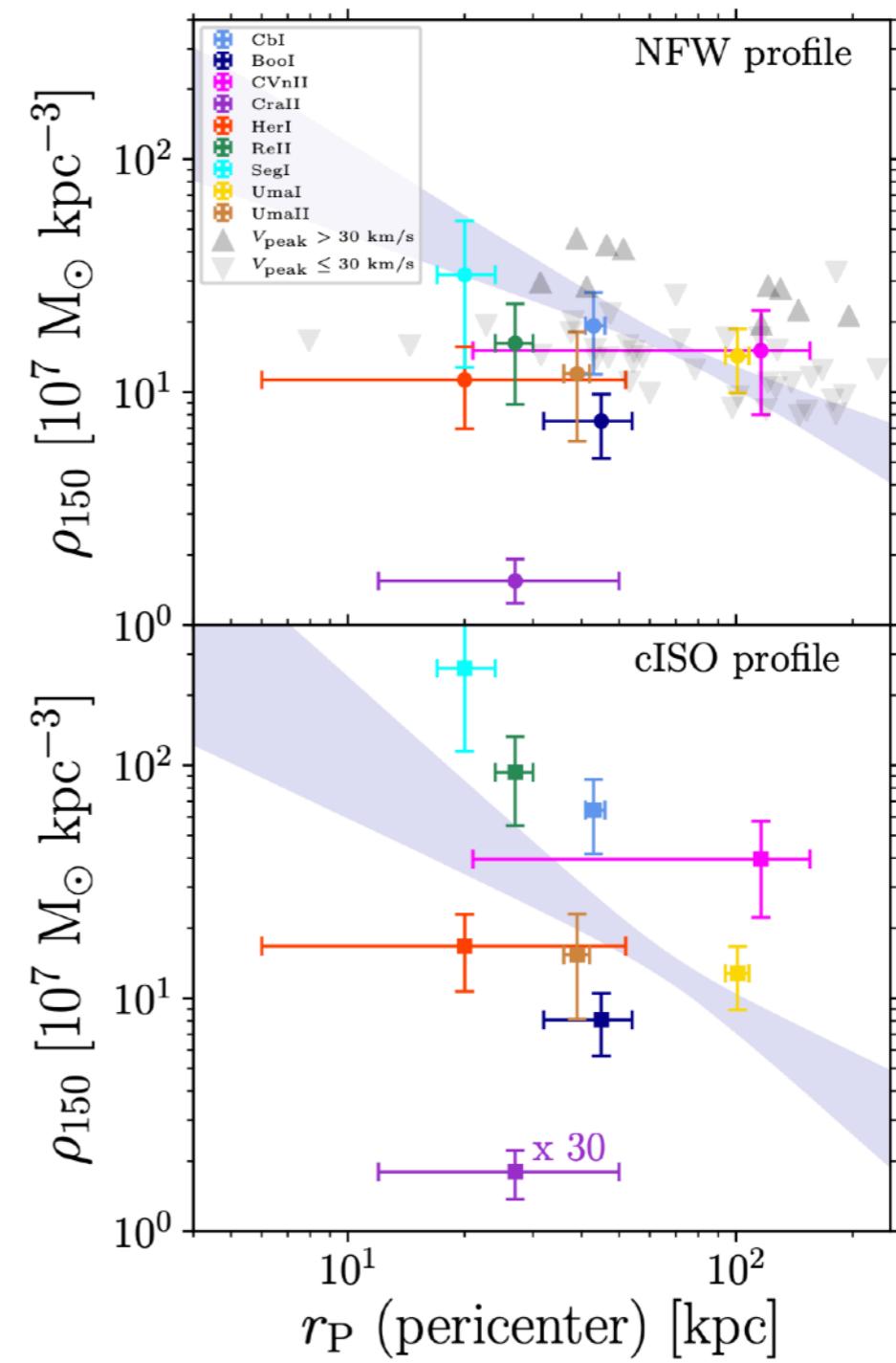
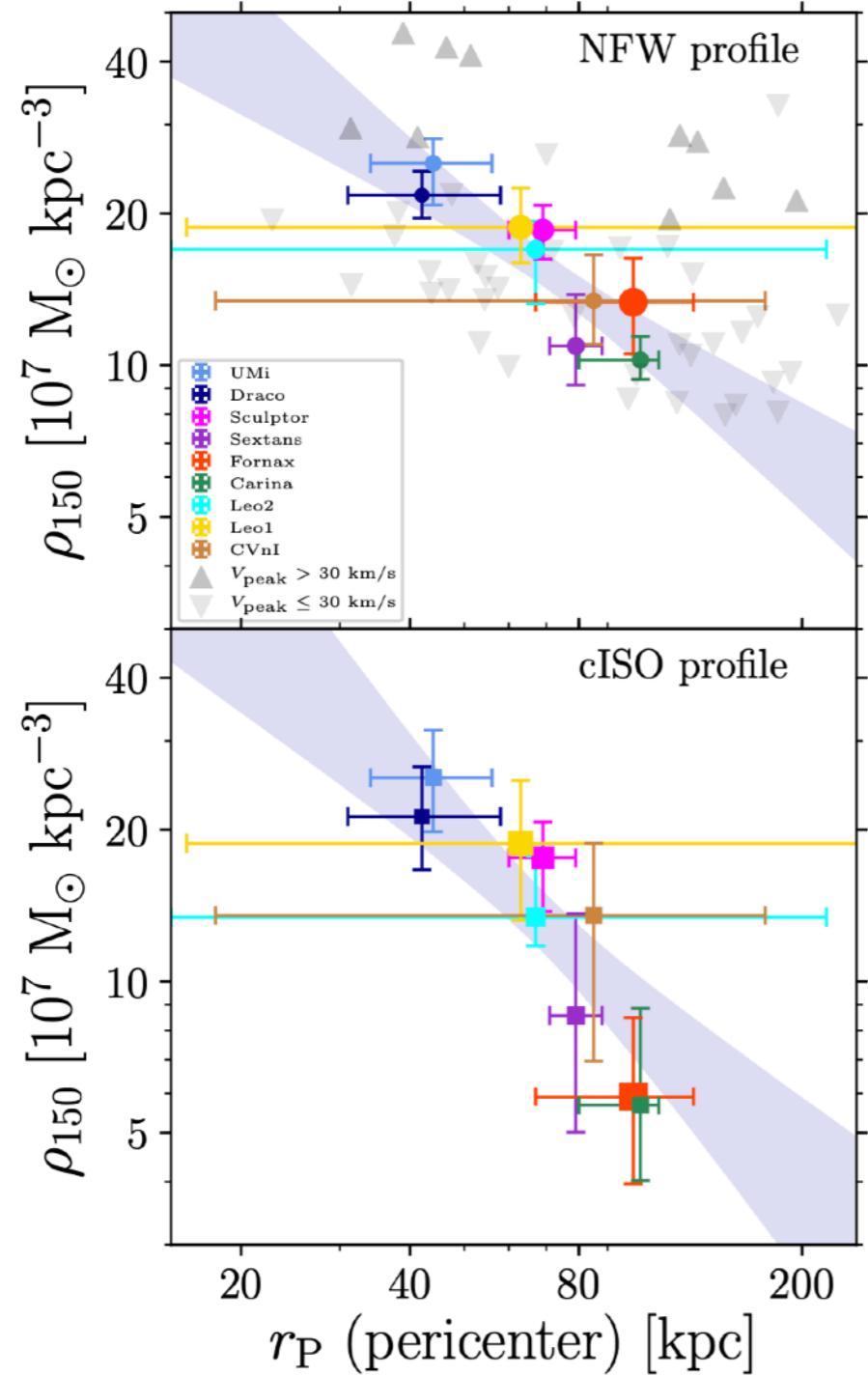
Satellites (long period orbit)



low concentration

Kahlhoefer, Kaplinghat, Slatyer, Wu (1904.10539)

# TBTF Revisited



# LSST Connection

